New exclusion limits on dark gauge forces from proton Bremsstrahlung in beam-dump data

Johannes Blümlein a, *, Jürgen Brunner b

a Deutsches Elektronen-Synchrotron, DESY, Platanenallee 6, D-15738 Zeuthen, Germany
b CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France

A R T I C L E   I N F O
Article history:
Received 15 November 2013
Received in revised form 9 February 2014
Accepted 14 February 2014
Available online 24 February 2014
Editor: L. Rolandi

A B S T R A C T
We re-analyze published proton beam dump data taken at the U70 accelerator at IHEP Serpukhov with the ν-calorimeter I experiment in 1989 to set mass-coupling limits for dark gauge forces. The corresponding data have been used for axion and light Higgs particle searches in Refs. [1,2] before. More recently, limits on dark gauge forces have been derived from this data set, considering a dark photon production from π0-decay [3]. Here we determine extended mass and coupling exclusion bounds for dark gauge bosons ranging to masses mν′ of 624 MeV at admixture parameters ε ≈ 10−6 considering high-energy Bremsstrahlung of the γ′-boson off the initial proton beam and different detection mechanisms.

© 2014 The Authors. Published by Elsevier B.V. Open access under CC BY license Funded by SCOAP3.

1. Introduction

Beyond the forces of the SU3 × SU2 × U1 Standard Model (SM) other U1-fields, very weakly coupling to ordinary matter, may exist [4–11]. The corresponding extended Lagrangian reads [10,12]

\[ \mathcal{L} = \mathcal{L}_{\text{SM}} - \frac{1}{4} X_{\mu \nu} X^{\mu \nu} + \frac{\varepsilon}{2} X_{\mu \nu} F^{\mu \nu} + \varepsilon \phi \Psi \Psi X^{\mu}, \]

with \( X^\mu \) the new vector potential and \( X^{\mu \nu} = \partial^\mu X^\nu - \partial^\nu X^\mu \) the corresponding field strength tensor, and \( F^{\mu \nu} \) the \( U(1)_Y \) field strength tensor. The mixing of the new \( U(1)_X \) and \( U(1)_Y \) of the Standard Model is induced by loops of heavy particles coupling to both fields [5,8]. The particle associated with the new \( U(1)_X \) symmetry is called \( \gamma' \). We assume minimal coupling for \( X^\mu \) to all charged Standard Model fermions \( \psi \), with effective charge \( e_{\psi} \), and \( e_{\phi} \) being the fermionic charge under \( U(1)_X \). For the generation of the mass term we assume the Stueckelberg formalism [13], as one example.[1]

In the mass range of \( m_{\gamma'} \geq 1 \text{ MeV} \) searches for a new \( \gamma' \)-boson have been performed analyzing the anomalous magnetic moments of the electron and muon [14], \( \gamma(3S) \)-decays [15], Belle [16], \( J/\psi \)-decays [17], K-decays [18], data from KLOE-2 [19], A1 [20], APEX [21], HADES [22], as well as searches in electron and proton beam dump experiments, as E774 [23], E141 [24], E137 [25, 26], Orsay [27], KEK [28], ν-CAL I [3], NOMAD and PS191 [29], CHARM [30], SINDRUM [31], and WASA [32]. Furthermore, limits were derived from supernovae cooling [12,33–37] and white dwarfs [38]. Possibilities to search for dark photons in low energy ep- [39] and e+e−-scattering [40] have been explored. The effect of massive photons on the \( \mu \)-content of air showers was studied in [41]. Updated summaries of exclusion limits and reactions have been given in Refs. [42–47]. The present limits in the \( m_{\gamma'}-\epsilon \) plane range from \( \epsilon \in [5 \times 10^{-9}, 10^{-2}] \) and a series of mass regions in \( m_{\gamma'} \in [2 \text{ m}_e, \sim 3 \text{ GeV}] \), with an unexplored range towards lower values of \( \epsilon \) and larger masses.

In the present Letter we derive new exclusion bounds on dark \( \gamma' \)-bosons using proton beam dump data at \( p \sim 70 \text{ GeV} \), based on potential \( \gamma' \)-Bremsstrahlung off the incoming proton beam searching for electromagnetic showers and muon pairs in a neutrino calorimeter [48]. In a previous analysis [3] exclusion limits were derived based on \( \gamma' \)-production in the decay of the \( \pi^0 \)-mesons. These beam-dump data have been used in the axion [49] and light Higgs boson searches, cf. [1,2,50], in the past.

In the following we first derive the production cross section, describe the detection process, the experimental set-up and data taking, and then derive new exclusion limits on the mass and coupling of a hypothetic \( \gamma' \)-boson.

* Corresponding author.
1 Other mechanisms are possible as well, cf. e.g. [3,12].
2. Production cross section

One production channel for a $\gamma'$-boson in a high-energy proton beam dump is given by small-angle initial-state radiation from the incoming proton at large longitudinal momentum, followed by a hard proton–nucleus interaction. The hadronic cross section is used in form of a parameterization of the measured distributions. Corresponding radiator functions may be derived using the Fermi–Williams–Weizsäcker method [51–53] to good approximation.\(^3\)

For the derivation often old-fashioned perturbation theory [58] in the infinite momentum frame is used in the literature, cf. [59–61]. As is well known, the corresponding radiators, beyond the universal contributions being free of mass effects, are no generalized splitting functions and are not process independent.\(^4\) They just describe a factorizing weight-function of a differential cross section $d\sigma_0$ relative to a sub-process given by $d\sigma_0$,\(^5\)

$$d\sigma_0 = w_{ba}(z, p_\perp^2) \, dz \, dp_\perp^2 \, d\sigma_0,$$  \(\text{(2)}\)

cf. Refs. [60,61]. Here $z$ denotes the longitudinal momentum fraction of the emitted $\gamma'$-boson relative to the incident proton beam momentum and $p_\perp$ its transverse momentum w.r.t. the incident beam direction.

The Fermi–Williams–Weizsäcker approximation was also derived using covariant methods, cf. [54] and [57,63]. Here one may consider the splitting-vertex $p \to \gamma' + p'$ only [59–61,63], which will lead to finite fermion mass corrections up to $\sim M^2$ in the fermion mass. Using the method of [61] and accounting for a finite fermion mass one reproduces the results given in [59,60,63].\(^5\)

A more general approach, the generalized Fermi–Williams–Weizsäcker method, relies on the scattering process

$$b + p \to \gamma' + p', \quad (3)$$

with $b$ the boson being exchanged between the incoming fermion and the hadronic target, for which we assume $b$ being a vector, cf. also [63]. Here $p$ and $p'$ denote the proton before and after the emission and $\gamma'$ is the produced new $\gamma'$-boson. Following [57] the contraction of the fermionic tensor $L_{\mu\nu}$ corresponding to (3) with the incoming target momentum $P_{i,\mu}$ is given by

$$\frac{L_{\mu\nu} P_{i,\mu} P_{j,\nu}}{M_t^2} = \frac{q_2^2}{(q_2 - q_0)^2} (L_{00} + L_{zz} - 2L_{0z}) + \frac{q_2^2}{(q_2 - q_0)^2} (\cos^2 \varphi_{Lxx} + \sin^2 \varphi_{Lyy}), \quad (4)$$

where $M_t$ denotes the target mass and $q_z, q_\perp$ are the components of the momentum of the boson $b$. As shown in [57] the terms $L_{00} + L_{zz} - 2L_{0z}$ are strongly suppressive relative to those of the second term. The dominant contribution to (4) stems from the region of very small values of $q_2^2$ and one may rewrite this relation

\(^2\)For a review see [54] and references therein. Early applications are found in [55,56].

\(^3\)Let us stress that the use of the Fermi–Williams–Weizsäcker method determines the corresponding exclusion bounds given in the present Letter. A later more refined theory might possibly change these bounds within the precision of its further improvement. This will apply also to the other foregoing applications of this method, see Refs. [12,57].

\(^4\)Cf. however, Ref. [62].

\(^5\)In case of the representation given in [63] the denominators containing $p_\perp^2$ are obtained from the virtuality $q_2^2$ in the deep-inelastic case for small angles $\alpha^2 < 1$, where $q_2^2 = |M^2x' + (\varphi' - M^2)/4\varphi''|^2 / (1 - z) = -(\varphi'^2 + p_\perp^2) / (1 - z)$, with $A = E(1 + \beta)(1 - z)$, $\beta = (1 - M^2/E^2)^{1/2}$, and $E$ the energy of the incoming fermion beam.

performing the $\varphi$-integral as

$$\frac{1}{2\pi} \int_0^{2\pi} d\varphi \frac{L_{\mu\nu} P_{i,\mu} P_{j,\nu}}{M_t^2} \approx \frac{q_2^2}{(q_2 - q_0)^2} \left( \frac{1}{2} g_{\mu\nu} L_{\mu
u} \right) q_2^2 = q_2^2, \quad (5)$$

since $L_{00} \approx L_{zz}$. In the following the virtuality $q_2^2$ is set effectively to zero.

We consider $b$ as a vector particle and $\gamma'$ as the $\gamma'$-gauge boson with mass $m_{\gamma'}$. The matrix element $|\mathcal{M}|^2$ averaging over the initial state spins is given by

$$|\mathcal{M}|^2 = \frac{1}{8} g_{\mu\nu} L_{\mu\nu} = -\frac{S}{U} - \frac{U}{S} + 2(2M^2 + m_{\gamma'}^2) \left( \frac{1}{S} + \frac{1}{U} \right)$$

$$+ 4M^4 \left( \frac{1}{S} + \frac{1}{U} \right)^2$$

$$+ 2M^2 m_{\gamma'}^2 \left( \frac{1}{S^2} + \frac{1}{U^2} \right) - 2 \frac{m_{\gamma'}^4}{SU}, \quad (6)$$

with the projector $-g_{\mu\nu} + k_\mu k_\nu/m_{\gamma'}^2$, for the polarization sum for the $\gamma'$-boson, is easily calculated using FORM [64]. Since we now refer to the $2 \to 2$ scattering process $\mathcal{M}$ also fermion mass terms up to $\sim M^2$ contribute. Here we have not specified the nature [13,65] of the produced boson. Due to the production of a massive final state boson $\gamma'$ three degrees of polarization contribute. This, however, does not lead to $1/m_{\gamma'}^2$-terms, with $k > 0, k \in N$, in (6).\(^6\) Massive boson production in Bremsstrahlung has also been considered e.g. in [70,71] and for massless fermions in [12].

The invariants $S$ and $U$ in (6) are given by

$$U = u - M^2 = (p - k)^2 - M^2 = m_{\gamma'}^2 - 2p_k, \quad (7)$$

$$S = s - M^2 = (p' + k)^2 - M^2 = m_{\gamma'}^2 + 2p'_k, \quad (8)$$

with $p, p'$ and $k$ the momenta of the incoming, outgoing fermion and produced boson $\gamma'$. From the matrix element in Eq. (6) we derive the splitting probability for the process $P \to \gamma' + P$ and set the momentum of the boson $b$ to $q = 0$. Referring to the infinite momentum frame given by the fast moving incoming fermion of momentum $P$ the 4-momenta are given by [60,61]

$$p = \left( P + \frac{M^2}{2P}; P, 0, 0 \right), \quad (9)$$

$$k = \left( 2zP + \frac{p_\perp^2 + m_{\gamma'}^2}{2Pz}; 2Pz, px, py \right), \quad (10)$$

$$p' = \left( (1 - z)P + \frac{M^2 + p_\perp^2}{2P(1 - z)}; (1 - z)P, -px, -py \right). \quad (11)$$

The invariants read, cf. also [12].

$$U = \frac{1}{z} \left[ (1 - z)m_{\gamma'}^2 + z^2 M^2 + p_\perp^2 \right], \quad S = -\frac{U}{1 - z}. \quad (12)$$

One thus obtains

$$w_{ba}(z, p_\perp^2) \, dz \, dp_\perp^2 = \frac{\alpha'}{2\pi} \left[ 1 + (1 - z)^2 - 2z(1 - z) \left( \frac{2M^2 + m_{\gamma'}^2}{H} - z^2 \frac{2M^4}{H^2} \right) \right]. \quad (13)$$

\(^6\)As has been discussed in the literature extensively [66–69] the transition in scattering cross sections from a massive boson to the massless limit needs not always to be continuous.
\[ + 2z(1-z)[1+((1-z)^2)] \frac{M^2m_\gamma^2}{H^2} \]
\[ + 2z(1-z)^2 \frac{m_\gamma^2}{H^2} \int \frac{dz dp^2}{H}, \]
(13)

with \( \alpha' = \frac{(e^\prime)^2}{(4\pi)} \) and

\[ H(p_\perp, z) = p_\perp^2 + (1-z)m_\gamma^2 + z^2M^2. \]
(14)

The first term in (13) denotes the well-known splitting function \( P_\gamma f(z) \). In the limit \( M^2 \to 0 \), Eq. (13) agrees with a corresponding expression in [12].

The \( p_\perp^2 \)-integral in (13) is regularized by both masses \( m_\gamma \) and \( M \) individually. It is given by

\[ w_{ba}(z)dz = \frac{\alpha'}{2\pi} \frac{1 + (1-z)^2}{z} \ln \left( 1 + \frac{p_{\perp, \text{max}}^2}{A} \right) \]
\[ - 2z(1-z)(2M^2 + m_\gamma^2) \frac{p_{\perp, \text{max}}^2}{A(p_{\perp, \text{max}}^2 + A)} \]
\[ + 2z(1-z)(2z^2M^4 + [1 + (1-z)^2]M^2m_\gamma^2) \]
\[ + (1-z)m_\gamma^2] \frac{p_{\perp, \text{max}}^2}{A^2} \int \frac{dz}{2(p_{\perp, \text{max}}^2 + A)^2}, \]
(15)

with \( A = (1-z)m_\gamma^2 + z^2M^2 \).

The final production cross section reads

\[ \sigma_{p+A \to \gamma' + \chi} = \int_{z_{\text{min}}}^{z_{\text{max}}} \frac{p_{\perp, \text{max}}^2}{A} \]
\[ \times \int \int dp_{\perp}^2 w_{\gamma'p}(z, p_{\perp}^2) \sigma_{pA}(s') \theta(f(z, p_{\perp}^2)), \]
(16)

with \( s' = (M + E_p)^2(1-z) \), \( E_p \) the beam energy of the accelerator, \( \sigma_{pA}(s') \) the hadronic scattering cross section after \( \gamma' \)-boson emission and \( \theta(f(z, p_{\perp}^2)) \) summarizing the experimental cut conditions. The cross section \( \sigma_{pA}(s') \) is related to the \( pN \)-scattering cross section by a function \( f(A) \), which drops out in calculating the event rate. The inelastic scattering cross section \( \sigma_{pp} \) is taken from experimental data, cf. Ref. [72]:

\[ \sigma_{pp}(s') = Z + B \cdot \log \left( \frac{s'}{s_0} \right) + Y_1 \left( \frac{s_1}{s'} \right) \eta_1 \]
\[ - Y_2 \left( \frac{s_2}{s'} \right) \eta_2, \]
(17)

where \( Z = 35.45 \text{ mb} \), \( B = 0.308 \text{ mb} \), \( Y_1 = 42.53 \text{ mb} \), \( Y_2 = 33.34 \text{ mb}, \sqrt{s_0} = 5.38 \text{ GeV}, \sqrt{s_1} = 1 \text{ GeV}, \eta_1 = 0.458 \) and \( \eta_2 = 0.545 \).

Finally we would like to briefly summarize the condition of use for the Fermi–Williams–Weizsäcker approximation given in [57,73] for the present set-up. These are

\[ E^2 \gg (p + k)^2, M^2 \]
(18)
\[ E_\gamma \gg M_{\gamma'} \]
(19)
\[ E - E_\gamma \gg \Delta, M, \sqrt{p_\perp^2}, \frac{1}{M}[M^2 - p^2]. \]
(20)

with \( \Delta = (M^2 - M_f^2)/(2M) \) and \( M \equiv M \). In case of a quasi-elastic emission of the \( \gamma' \)-boson one expects the hadronic mass \( M_f = \sqrt{p_\perp^2} \) of similar size than the nucleon mass \( M \). The conditions translate into

\[ p_\perp^2 \gg zM^2 + \frac{1}{z}[p_{\perp, \text{max}}^2 + (1-z)m_\gamma^2]. \]
(21)
\[ p_\perp^2 \gg M^2 \]
(22)
\[ (1-z)P + \frac{p_{\perp, \text{max}}^2 + m_\gamma^2}{2P(1-z)} \gg m_\gamma^2 \]
(23)
\[ m_\gamma^2 \gg \frac{P^2 + P_{\perp, \text{max}}^2}{2P}. \]
(24)

Again, for quasi-elastic splitting one has \( \sqrt{p_\perp^2} \sim M \). While (22) is fulfilled automatically at high energy accelerators, (21), (23), (24) set constraints on \( z \) in dependence of the values of \( p_{\perp, \text{max}}^2 \) and \( m_\gamma \), and have to be tested accordingly. These conditions may be summarized by

\[ E_p, E_\gamma', E_p - E_\gamma' \gg M, m_\gamma^2, \sqrt{p_{\perp, \text{max}}^2}. \]
(25)

From the experimental setup one obtains \( E_p = 70 \text{ GeV} \) and \( p_{\perp, \text{max}}^2 < 1 \text{ GeV}^2 \) (see below). Further we only test masses \( m_\gamma < 10 \text{ GeV} \) and we restrict to the energy range \( 10 \text{ GeV} < E_\gamma < 60 \text{ GeV} \), which corresponds to the condition \( 0.14 < z < 0.86 \).

This combination of constraints ensures the validity of the approximations used according to the conditions of Eq. (25).

The event rates in the detector are calculated using the differential \( \gamma' \)-rate per proton interaction

\[ \frac{dN}{dE_\gamma'} = \frac{1}{E_p} \frac{\sigma_{pA}(s')}{\sigma_{pA}(s)} \int_0^{p_{\perp, \text{max}}^2} \frac{dz}{2\pi} \int \frac{dp_{\perp}^2}{2\pi} w_{ba}(z, p_{\perp}^2), \]
(26)

where \( s' = 2M(E_p - E_\gamma') \) is the reduced center-of-mass energy after the emission of the \( \gamma' \) and \( s = 2ME_p \). The resulting \( \gamma' \)-rate is shown in Fig. 1 for five values of \( m_\gamma \) between 0 and 800 MeV and \( \varepsilon = 1 \).

3. The detection processes

In Ref. [3] we restricted the analysis to the mass range \( 2m_e < m_\gamma < m_{\pi^0} \). Here the only relevant decay channel is \( \gamma' \to e^+e^- \). However, the Bremsstrahlung process can produce particles with \( m_\gamma > m_{\pi^0} \). Therefore we consider here as well the decay channels
\[ \gamma' \rightarrow \mu^+\mu^- \quad \text{and} \quad \gamma' \rightarrow \text{hadrons}. \]

The partial decay width of the \( \gamma' \)-boson into a lepton pair is given by [10]

\[ \Gamma(\gamma' \rightarrow l^+l^-) = \frac{1}{3} \alpha_{\text{QED}} m_{\gamma'} e^2 \left( 1 - \frac{4m_e^2}{m_{\gamma'}^2} \right) \left( 1 + \frac{2m_l^2}{m_{\gamma'}^2} \right), \quad (27) \]

where \( l \) indicates either a muon or an electron. The partial decay width into hadrons is determined following the approach having been proposed in [12]

\[ \Gamma(\gamma' \rightarrow \text{hadrons}) = \frac{1}{3} \alpha_{\text{QED}} m_{\gamma'} e^2 \sigma(\mu^+\mu^- \rightarrow \text{hadrons}) / \sigma(\mu^+\mu^- \rightarrow l^-l^+) \cdot \Gamma(l^-l^+ \rightarrow \text{hadrons}), \quad (28) \]

where the ratio of the hadron production cross section with respect to muons is taken from [72]. The resulting branching ratios for the three channels are shown in Fig. 2. For \( m_{\gamma'} < 2m_\mu \), only the decay into \( \mu^+\mu^- \) is allowed. For \( 2m_\mu < m_{\gamma'} < 400 \text{ MeV} \), the suppression of the muon channel compared to the electron channel due to the kinematic factor in Eq. (27) is visible. For \( m_{\gamma'} > 600 \text{ MeV} \), the hadronic decay starts to dominate.

The decay probability \( w_{\text{dec}} \) inside the fiducial volume of the detector for a leptonic decay \( \gamma' \rightarrow l^+l^- \) is given by

\[ w_{\text{dec}} = Br(\gamma' \rightarrow l^+l^-) \exp \left( \frac{-l_{\text{dum}} m_{\gamma'}}{c \tau(\gamma')} \left( \sqrt{k} \right) \right) \times \left[ 1 - \exp \left( -\frac{l_{\text{had}} m_{\gamma'}}{c \tau(\gamma')} \left( \sqrt{k} \right) \right) \right], \quad (29) \]

with \( \tau(\gamma') \) the lifetime of the \( \gamma' \) for a given mass (i.e., the inverse of the total decay width), \( c \) the velocity of light, \( m_{\gamma'} \) and \( k \) are the mass and 3-momentum of the \( \gamma' \)-boson. \( l_{\text{dum}} \) and \( l_{\text{had}} \) denote the distance of the fiducial volume from the beam dump and fiducial volume itself.

### 4. The experimental setup and data taking

The beam dump experiment was carried out at the U70 accelerator at JHEP Serpukhov during a three months exposure in 1989. Data have been taken with the \( \nu \)-CAL I experiment, a neutrino detector. All technical details of this experiment have been described in [1] and a detailed description of the detector was given in [48]. Here we only summarize the key numbers which are crucial for the present analysis.

The target part of the detector is used as a fiducial volume to detect the decays of the \( \gamma' \)-boson. It has a modular structure and consists of 36 identical modules along the beam direction. Each of the modules is composed of a 5 cm thick aluminum plate, a pair of drift chambers to allow for three dimensional tracking and a 20 cm thick liquid scintillator plane to measure the energy deposit of charged particles.

For the beam dump experiment a fiducial volume of 30 modules with a total length of \( l_{\text{fid}} = 23 \text{ m} \) is chosen, starting with the fourth module at a distance of \( l_{\text{dump}} = 64 \text{ m} \) downstream of the beam dump. Three modules in front of the fiducial volume are used as a veto in addition to a passive 54 m long iron shielding.

The lateral extension of the fiducial volume is \( 2 \times 2.6 \text{ m} \) in diameter at the end of the fiducial volume, i.e. at a distance of \( 87 \text{ m} \) from the dump. This leads to the following simple fiducial volume cut

\[ (p_\perp/p_\ell)_{\text{lab}} < 1.3/87 = 0.015. \quad (30) \]

During the three months exposure time in 1989 \( N_{\text{tot}} = 1.71 \times 10^{18} \) protons on target had been accumulated [1]. The signature of event candidates from \( \gamma' \rightarrow e^+e^- \) is a single electromagnetic shower in beam direction. This signature is identical to the one from the axion or light Higgs particle decay search which was performed in [1]. Electromagnetic showers with energies larger than 10 GeV are detected with an efficiency \( \epsilon_e = 70\% \) [1]. From the total data sample of 3880 reconstructed events, 1 isolated shower with \( E > 10 \text{ GeV} \) is selected, which is compatible with a background estimate of 0.3 events from the simulation of \( \nu_e \) and \( \ell_e \) interactions in the detector.

In [2] the same data set is searched for a decay signature of light Higgs or axions into \( \mu^+\mu^- \). Again this signature is identical to the corresponding decay of a \( \gamma' \) into a muon pair. For \( E_{\mu_1} + E_{\mu_2} > 10 \text{ GeV} \) the detection efficiency is found to be \( \epsilon_\mu = 80\% \) [2]. From the total data sample, one muon pair with \( E_{\mu_1} + E_{\mu_2} > 10 \text{ GeV} \) is selected, which is compatible with a background estimate of 0.7 events.

### 5. Results

The total number of expected signal events can be calculated as

\[ N_{\text{sig}} = N_{\text{tot}} \times \varepsilon_1 \int dE dN_{\text{dec}}(E), \quad (31) \]

where \( \varepsilon_1 \) denotes the detection efficiency for an electromagnetic shower (\( l = e \)) or a muon pair (\( l = \mu \)) as introduced above. The integration is carried out over the energies of the \( \gamma' \) in the range 10–60 GeV. The dependence of \( N_{\text{sig}} \) on \( m_{\gamma'} \) and \( \varepsilon \) for the two decay channels is shown in Fig. 3.

The overall shape of the contour is similar to the one obtained in [3]. The maximal event numbers are about two orders of magnitude below the values found in [3] and the contour is narrower, both due to the lower flux from Bremsstrahlung with respect to production from \( \pi^0 \)-decays. However the present contour is not limited to \( m_{\gamma'} < m_{\pi^0} \) and indeed events are expected for masses as high as \( \sim 600 \text{ MeV} \). The muon channel contributes with maximally few tens events at \( m_{\gamma'} = 250 \text{ MeV} \) and \( \varepsilon = 3 \cdot 10^{-6} \). For \( m_{\gamma'} > 2m_\mu \) both electron and muon channels contribute about equally, therefore the combination of these two channels will improve the sensitivity in this mass range.

The leading systematic uncertainty of the measurement is due to the background estimate from neutrino interactions. Its impact on the result is evaluated below. Other systematic effects such
and \( b \) values Eq. (32) allow one to determine the signal level. For a given confidence level, if \( k \) different channels are combined such as the decays into electrons and muons Eq. (32) modifies to

\[
c = 1 - \prod_{k=1}^{K} \left[ \sum_{n=0}^{N} P(n, s_k + b_k) \right] / \prod_{k=1}^{K} \left[ \sum_{n=0}^{N} P(n, b_k) \right].
\]

This relation is used to calculate the corresponding event numbers for both muon and electron signatures at the 95\% C.L. for the mass range where both channels contribute.

The new corresponding exclusion region is shown as red area and line in comparison with the limit from [3] (blue line) and limits from other experiments in Fig. 4.

At large values of \( \varepsilon \) studies of the anomalous magnetic moments of the muon and electron [14], of rare decays of heavy mesons [15], and results from MAMI [20], put stringent limits. For \( 10^{-3} < \varepsilon < 10^{-7} \) beam dump experiments [32–37] give the best sensitivity. For even smaller values of \( \varepsilon \) limits can be derived by studying the dynamics of supernovae cooling [33].

### 6. Conclusions

We have re-analyzed proton beam dump data taken at the U70 accelerator at IHEP Serpukhov with the \( \nu \)-calorimeter I experiment in 1989 [1,2] to set mass and coupling limits for dark gauge forces. The search is based on \( \gamma'\)-Bremsstrahlung off the incoming proton beam searching for electromagnetic showers and muon pairs in a neutrino calorimeter [48]. Recently published limits based on the same dataset [3] could be extended towards larger gauge boson masses, excluding a new area in the \( m_{\gamma'}-\varepsilon \) plane. The present analysis extends the region excluded by a recently published limit based on the same dataset [3] towards larger masses \( m_{\gamma'} \in [m_{\pi^0}, 0.63 \text{ GeV}] \) for values in the mixing parameter \( \varepsilon \approx 10^{-6} \). In future experiments signals from dark gauge forces will be searched for in the yet unexplored regions shown in Fig. 4, see e.g. Ref. [8] for proposals.

---

1 We thank S. Andreas for designing this graph. The exclusion curves for the electron-beam dump have been recalculated in [42] and are shown here. Note a difference to [12] in case of E137.
[71] A.A. Akhundov, D.Yu. Bardin, JINR-P2-9587.