Abstract

The GERDA experiment at the Laboratori Nazionali del Gran Sasso in Italy uses germanium detectors made from material with an enriched $^{76}\text{Ge}$ isotope fraction to search for neutrinoless double beta decay of this nucleus. Applying a blind analysis we find no signal after an exposure of $21.6 \text{ kg yr}$ and a background of about $0.01 \text{ cts (keV kg yr)}^{-1}$. A half-life limit of $T_{\nu \beta}^{0} > 2.1 \times 10^{25} \text{ yr (90\% C.L.)}$ is extracted. The previous claim of a signal for $^{76}\text{Ge}$ is excluded with 99% probability in a model independent way.

Key words: double beta decay
1. Introduction

Lepton number is not conserved in neutrinoless double beta ($0\nu\beta\beta$) decay of isotopes like $^{76}$Ge. This process is predicted to occur by many extensions of the standard model [1, 2, 3, 4]. Consequently, there is large interest to search for this process and a number of experimental programs using different experimental techniques and isotopes are currently taking data or will soon start [5, 6].

The GERDA experiment located at the Laboratori Nazionali del Gran Sasso (LNGS) of INFN in Italy operates germanium diodes as detectors and sources of $0\nu\beta\beta$ decay of $^{76}$Ge. The $^{76}$Ge isotope fraction of the detector material is enriched from 7.8 % to $\approx$86 %. The signature of the decay is a peak at $Q_{\beta\beta} = 2039.061 \pm 0.007$ keV [7] in the measured energy spectrum.

Part of the Heidelberg-Moscow collaboration has claimed to have observed $28.75 \pm 6.86 \, 0\nu\beta\beta$ decay events of $^{76}$Ge [8]. This observation converts to a half-life of $T_{1/2}^{0\nu} = (1.19^{+0.37}_{-0.23}) \cdot 10^{25}$ yr. Later, the pulse shapes of the detector signals have been analyzed to strengthen the significance of the observation [9]. We restrict our comparison to the first publication since there are some problems in the later publication like the missing efficiency correction in the derived half-life [10].

Recently, Kamland-Zen [11] and EXO-200 [12] have report 90 % C.L. half-life limits for $0\nu\beta\beta$ decay of $^{136}$Xe of $1.9 \cdot 10^{25}$ yr and $1.6 \cdot 10^{25}$ yr, respectively. Nuclear matrix element calculations are needed to relate these results to the claim for $^{76}$Ge which complicates the comparison. This is not the case for GERDA since we use the same isotope. We report here about our first result which is published in [13].

2. Experiment and data selection

GERDA operates refurbished semi-coaxial diodes from the Heidelberg-Moscow experiment [14] and from the International GErmanium eXperiment (IGEX) [15, 16]. Here we report results from the first measurement period from November 2011 to May 2013. Five newly produced detectors of BEGe type [17] have been added in July 2012. In addition, we operated one semi-coaxial detector with natural isotope composition. Two semi-coax detectors exhibited a large leakage current soon after the deployment and were not used. The leakage current of all other detectors was stable within 20 pA. One BEGe showed unstable energy
calibration and was therefore also not included in the analysis. A detailed description of the experiment is given in Ref. [18].

The detectors are mounted in low mass copper holders and operated in 64 m³ liquid argon which serves as coolant and as shield against external background radiation. The shielding is complemented by 3 m of water which is instrumented with photo multipliers to detect the Cerenkov light of muons traversing the setup. Fig. 1 shows a model of GERDA.

Each detector signal is read out by a charge sensitive amplifier located at close distance of ≈ 30 cm to the detectors in the liquid argon. The outputs are digitized with 100 MHz Flash ADCs. All event parameters like the deposited energy or the rise time of the detector signal are reconstructed by digital filters offline [19, 20]. Unphysical events triggered e.g. by noise are identified and rejected. A visual scan of all events with energy deposition between 1.3 and 2.7 MeV showed that no real event was rejected and that no unphysical event is kept.

The energy reconstruction and noise rejection was cross checked with a second completely independent algorithm. The selected event samples around $Q_{\beta\beta}$ were identical and the reconstructed energies agreed with each other within $\sigma = 0.9$ keV.

$0\nu\beta\beta$ decays deposit almost always energy in only one detector. Events with depositions in several detectors or in correlation with a muon candidate (within 8 µs) are therefore not considered. These requirements remove about 40 % of the events around $Q_{\beta\beta}$. Two events within 1 ms in the same detector are most likely from the $^{214}$Bi-$^{214}$Po decay chain and therefore rejected. These cuts cause practically no dead time.

To calibrate the energy, we collect (bi)weekly data sets with $^{228}$Th sources deployed close to the detectors. Fig. 2 (left) shows for the semi-coaxial detectors the drift of the 2615 keV peak relative to the position of the corresponding previous calibration. The gain drifts by typically less than 0.05 % which is small relative to the typical energy resolution of 0.2 % at $Q_{\beta\beta}$ (full width at half maximum, FWHM). Fig. 2 (right) shows the strongest background peak of the physics data from $^{42}$K decays. The fitted resolution (FWHM) of 4.5 keV is only slightly larger than the value of 4.3 keV expected from calibration data. From this comparison and the known extrapolation of the resolution to $Q_{\beta\beta}$ we expect for the semi-coaxial detector an average resolution of 4.8 ± 0.3 keV and 3.2 ± 0.2 keV for the BEGe detectors.

The resolution of all detectors was stable within 0.1 keV during the entire data taking period. All numbers show that the detector performance was sufficiently stable and that the physics data is well calibrated.

We performed a blind analysis. Events in the interval $Q_{\beta\beta} \pm 20$ keV were hidden until the calibration was finalized and all selection cuts were frozen.

Visible $\gamma$ peaks in the energy spectrum (see Fig. 3) are from $^{40}$K and $^{42}$K decays and the decay chains of $^{226}$Ra and $^{232}$Th. Between the trigger threshold of 40-100 keV and 570 keV, the spectrum is dominated
by $^{39}$Ar $\beta$ decays; between 570 keV and 1700 keV the main contribution is from double beta decay with neutrino emission ($2\nu\beta\beta$ decays) [21]. Above 3 MeV we observe $\alpha$ decays on the detector p$^+$ contact surfaces; predominantly from $^{210}$Po but to a smaller extent also from the $^{226}$Ra decay chain. Around 2 MeV, we observe a mixture of contributions [22].

We fit the physics spectrum of the semi-coaxial and the BEGe detectors between 570 and 7500 keV to a background model consisting of the above mentioned contributions at different locations. Despite the fact that the location and composition of the events around $Q_{\beta\beta}$ can not be determined precisely with the available statistics (see Fig. 4), we know that the background

- is largely dominated by sources close to the detectors or on the detector surfaces,
- is not expected to have a peak in the blinded energy window,
- can be well approximated by a constant intensity in the energy window from 1930 - 2190 keV with the exclusion of two intervals at 2104$\pm$5 keV and 2119$\pm$5 keV where we expect sizable contributions from known $\gamma$ peaks. Other lines expected in this window from e.g. $^{214}$Bi decays are too weak ($\ll$ 1 count) to be relevant.

If bremsstrahlung energy loss of electrons in $0\nu\beta\beta$ events is small, all ionization occurs in a small volume of the detector (single site events). Background events from Compton scattered photons deposit often energy in several well separated locations (multi site events). The induced current signal on the readout electrode will in general be different for the two classes. Surface background events also exhibit distinct signal shapes. This feature is used in GERDA to discriminate background events. A detailed description of the algorithms is given in Ref. [23]. Here, we will only discuss them briefly.
Fig. 4. Spectrum of physics data for the semi-coaxial enriched detectors around $Q_{\beta\beta}$ and the composition according to a fit with different possible contributions on a logarithmic scale. The bottom plot shows the model and a flat background on a linear scale. The labels for the location mean “p+” on $p^+$ detector surface, “H” close to the detector, e.g. in the holder, “LAr” homogeneous in the argon, “Ge” inside the Ge detectors [22]. The interval $Q_{\beta\beta} \pm 20$ keV was blinded and not used for the fit. The light grey part of the histogram shows the partially unblinded interval.

For BEGe detectors, the ratio of the maximum of the current pulse, $A$, over the deposited energy, $E$, allows for a simple, powerful and robust selection. Double escape peak (DEP) events of 2615 keV photons from $^{208}$Tl decays of the calibration data serve as proxy for the pulse shape of $0\nu\beta\beta$ decays. For the accepted range of $0.965 < A/E < 1.07$ we find a signal efficiency of $0.92 \pm 0.02$ while more than 80 % of the background events around $Q_{\beta\beta}$ are removed. We cross check the signal efficiency with $2\nu\beta\beta$ decays in the interval 1.0 - 1.4 MeV. The value of $0.91 \pm 0.05$ agrees well.

For the semi-coaxial detectors, the neural network algorithm TMlpANN implemented in TMVA [24] is used to identify single site events. The times when the charge pulses reach 1%, 3%, ..., 99% of the maximum are the input variables. Two hidden layers with 51 and 50 neurons are used. For training, DEP events at 1593 keV serve as signal sample and gamma events at 1621 keV from $^{212}$Bi decays serve as multi site event sample. The training is performed for each detector and for three periods of similar conditions. The cut on the classifier output of the neural network is chosen to retain 90 % of the DEP.

To cross check the selection, two independent algorithms based on a projective likelihood method implemented in TMVA and on the current pulse asymmetry have been developed. Of the physics data events between 1930 and 2190 keV (outside the blinded window) about 45 % are rejected by the neural network. All of these events are rejected by at least one other method and about 90 % of them are rejected by both. This gives confidence that the classification of background events by the neural network is meaningful.

We assume that the pulse shape selection efficiency for $0\nu\beta\beta$ decays is the same as for the DEP events used for training. To cross check this assumption, the efficiency for $2\nu\beta\beta$ events in the energy interval 1.0 - 1.3 MeV was measured to be $0.85 \pm 0.02$ for the total data set. A special calibration data set with a $^{56}$Co source was taken since this spectrum has two usable DEPs at 1576 keV and at 2231 keV, see Fig. 5. Applying the neutral network selection we find for the different detectors efficiencies between 83 % and 95 % for the two additional DEPs. In summary, we estimate the efficiency and the systematic uncertainty of the $0\nu\beta\beta$ selection to be $0.90^{+0.05}_{-0.09}$.

Our pulse shape selections are intended to yield the best sensitivity for a $T_{1/2}^{0\nu}$ limit: The expected background counts at $Q_{\beta\beta}$ are low and hence only a moderate rejection is needed while keeping the efficiency high. It is worth to notice that all DEPs reconstruct at the correct energy, independent whether the pulse shape selection is applied or not. Hence we expect that a possible $0\nu\beta\beta$ decay signal reconstructs at $Q_{\beta\beta}$.

3. Results

The data are split into three sets. One contains the BEGe data. A second one (labelled “silver” set) covers a short period of semi-coaxial data with higher background index at the time when the BEGe detectors were
deployed. The rest of the semi-coaxial data is labelled “golden” set. The relevant analysis parameters of all sets are listed in Tab. 1.

After the analysis methods discussed above have been frozen, the events in the blinded window have been processed. The expected background counts and observed number of events are consistent in all sets, with and without pulse shape discrimination (see last two columns of Tab. 1 and Fig. 6). Hence, GERDA sees no indication for a 0νββ decay signal and a half-life limit is extracted. All results are given with pulse shape discrimination applied.

The observed signal count \( N^\nu_0 \) (or limit) for each data set \( k \) = (golden, silver, BEGe) is related to the half-life \( T^{0\nu}_{1/2} \) by

\[
N^\nu_0 = \frac{\ln 2 \cdot N_A \cdot \epsilon_k \cdot \mathcal{E}_k}{m_A \cdot T^{0\nu}_{1/2}}
\]

where \( N_A \) is Avogadro’s constant, \( \epsilon_k \) is the efficiency, \( \mathcal{E}_k \) the exposure and \( m_A = 0.0756 \) kg the molar mass of the enriched material. \( \epsilon_k \) is the product of the (set dependent) enrichment fraction \( f_{76} \), the active volume fraction of the detectors \( f_{av} \), the fraction of 0νββ events which deposit all energy in the active volume \( f_{ep} \) and the pulse shape selection efficiency discussed above.

We fit each of the energy spectra of the three sets to a normalized function \( f(E | b_k, 1/T^{0\nu}_{1/2}) \) which is the sum of a constant \( b_k \) for the background and a Gaussian for a possible 0νββ signal. The latter is centered at \( Q_{\beta\beta} \pm 0.2 \) keV and has a width \( \sigma_k = \delta E_k/2.35 \) (Tab. 1) given by the known energy resolution. The 240 keV wide background window for the background estimate spans from 1930 keV to 2190 keV without the intervals \( (2104 \pm 5) \) keV and \( (2119 \pm 5) \) keV from known \( \gamma \) lines.

\[
f(E | b_k, 1/T^{0\nu}_{1/2}) = \frac{1}{240 \text{ keV} \cdot b_k + N^\nu_0 (1/T^{0\nu}_{1/2})} \exp \left( \frac{(E - Q_{\beta\beta})^2}{2\sigma_k^2} \right)
\]

with \( N^\nu_0 (1/T^{0\nu}_{1/2}) \) given by Eq. 1.

We perform a profile likelihood fit. The (unbinned extended) likelihood \( L \) is

\[
L(b_k, 1/T^{0\nu}_{1/2}) = \prod_k \frac{\mu_k^{N_k} \cdot e^{-\mu_k}}{N_k!} \prod_{\text{events}} f(E | b_k, 1/T^{0\nu}_{1/2})
\]

with \( N_k \) being the number of observed events in data set \( k \) and \( \mu_k = b_k \cdot 240 \text{ keV} + N^\nu_0 \) the expected number.
Fig. 6. Physics spectrum of all 3 data sets after unblinding without (histogram) and with (solid grey) pulse shape selection [13].

Table 1. List of analysis parameters for the three sets without and with pulse shape discrimination. $\epsilon_k$ is the total $0\nu\beta\beta$ decay detection efficiency. $\delta E_k$ is the energy resolution (FWHM). The total detector mass is used to calculate the “exposure” $E_k$. “bkg” is the number of events in the 1930-2190 keV window (without the intervals (2039 ± 5) keV, (2114 ± 5) keV and (2119 ± 5) keV) and “BI” is the corresponding background index. “ROI exp” is the expected background count in a ±5 keV window around $Q_{\beta\beta}$ and “ROI obs” is observed counts after the unblinding.

<table>
<thead>
<tr>
<th>set $k$</th>
<th>$\epsilon_k$</th>
<th>$\delta E_k$</th>
<th>exposure</th>
<th>bkg</th>
<th>$10^{-3}$ cts/(keV·kg·yr)</th>
<th>BI</th>
<th>ROI exp</th>
<th>ROI obs</th>
</tr>
</thead>
<tbody>
<tr>
<td>golden</td>
<td>0.688 ± 0.031</td>
<td>4.8</td>
<td>17.9</td>
<td>76</td>
<td>18 ± 2</td>
<td>3.3</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>silver</td>
<td>0.688 ± 0.031</td>
<td>4.6</td>
<td>1.3</td>
<td>19</td>
<td>63$^{+16}_{-10}$</td>
<td>0.8</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>BEGe</td>
<td>0.720 ± 0.018</td>
<td>3.2</td>
<td>2.4</td>
<td>23</td>
<td>42$^{+4}_{-3}$</td>
<td>1.0</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>golden</td>
<td>0.619$^{+0.044}_{-0.070}$</td>
<td>4.8</td>
<td>17.9</td>
<td>45</td>
<td>11 ± 2</td>
<td>2.0</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>silver</td>
<td>0.619$^{+0.044}_{-0.070}$</td>
<td>4.6</td>
<td>1.3</td>
<td>9</td>
<td>30$^{+11}_{-9}$</td>
<td>0.4</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>BEGe</td>
<td>0.663 ± 0.022</td>
<td>3.2</td>
<td>2.4</td>
<td>3</td>
<td>$5^{+4}_{-3}$</td>
<td>0.1</td>
<td>0</td>
<td></td>
</tr>
</tbody>
</table>

of events. The product for $L$ is over all events in all data sets. The profile likelihood $\lambda(1/T_{1/2}^{0\nu})$ is then

$$\lambda(1/T_{1/2}^{0\nu}) = \frac{\max_{b_k} L(b_k, 1/T_{1/2}^{0\nu})}{\max_{b_k, 1/T_{1/2}^{0\nu}} L(\hat{b}_k, 1/T_{1/2}^{0\nu})}$$

(4)

In the fit we require $1/T_{1/2}^{0\nu} \geq 0$, i.e. $N_{\nu}^{0\nu} \geq 0$. The 90 % coverage limit is defined as the $1/T_{1/2}^{0\nu}$ value for which $-2 \cdot \ln \lambda$ changes by 2.7. We verified with a toy Monte Carlo that the coverage of this method is sufficient. The best fit yields $1/T_{1/2}^{0\nu} = 0$ and the limit is

$$T_{1/2}^{0\nu} > 2.1 \cdot 10^{25} \text{ yr (90 % C.L.)}$$

(5)

Systematic uncertainties on the peak position, the resolution, and all efficiencies are taken into account by a Monte Carlo method: the half-life limit is calculated for 10000 randomly chosen parameter sets according to the known distributions. The quoted limit is the average over all individual limits. Without the systematic uncertainties the limit improves by 1.5 %. The (median) sensitivity is $2.4 \cdot 10^{25}$ yr.
We perform also a Bayesian analysis. A binned likelihood fit and the above mentioned sampling method for the systematic error are used. The fit is performed with the BAT toolkit [25] and a flat prior in $1/T^{0ν}_{1/2}$ between 0 and $10^{-24}$ yr$^{-1}$. The posterior distribution peaks at $1/T^{0ν}_{1/2} = 0$ and the 90% credible limit is $T^{0ν}_{1/2} > 1.9 \cdot 10^{25}$ yr. The (median) sensitivity is $2.0 \cdot 10^{25}$ yr.

The spectral fit can be extended to include the spectra from Heidelberg-Moscow (interval 2000-2080 keV, Fig. 4 of Ref. [14]) and IGEX (interval 2020-2060 keV, Table II of Ref. [15]). We assume that the backgrounds are constant as a function of energy in these intervals. Experimental parameters (exposure, energy resolution, efficiency factors) are obtained from the original references or, when not available, extrapolated from the values used in GERDA. Fig. 7 (left) shows the profile likelihood curves for the individual experiments and the combination. The latter yields

$$T^{0ν}_{1/2} > 3.0 \cdot 10^{25} \text{ yr} \quad (90 \% \text{ C.L.}).$$

### 4. Comparison to other experiments

We perform a hypothesis test using the $0νββ$ half-life of the claimed signal [8] (hypothesis $H_1$). In this case we would expect $5.9 \pm 1.4$ signal events in the energy interval of $Q_{ββ} \pm 2\sigma_k$ above a background of $2.0 \pm 0.3$ counts. In a frequentist analysis we generate 10000 toy experimental spectra for each of the three data sets with Poisson distributed background and signal strength. Fig. 7 (right) shows for each realization the best fitted inverse half-life $1/T^{0ν}_{1/2}$ from the profile likelihood fit. Only 1% of the realizations yield our experimental result $1/T^{0ν}_{1/2} = 0$. In case the restriction $1/T^{0ν}_{1/2} \geq 0$ is dropped in the fit, only 0.6% of the realizations yield $\sum_k N_k \leq 0$. Thus we reject the claim with 99% probability.

In a Bayesian analysis we calculate the Bayes factor, i.e. the probability ratio $p(\text{data}|H_1)/p(\text{data}|H_0)$ with $H_0$ being the background only hypothesis. The Bayes factor is 0.024. It includes all uncertainties and clearly favors the background-only hypothesis.

Our limit can be compared to the recent results for the isotope $^{136}$Xe. Neither EXO-200 nor Kamland-Zen observe a signal and they place 90% confidence level limits of $1.6 \cdot 10^{25}$ yr [12] and $1.9 \cdot 10^{25}$ yr [11] for the half-life, respectively. The sensitivities are $1.0 \cdot 10^{25}$ yr for Kamland-Zen [11] and $0.7 \cdot 10^{25}$ yr for EXO-200 [26].

Fig. 8 shows the experimental limits together with a selection of different nuclear matrix element calculations for the case of light neutrino exchange.

For the sensitivity estimate, the product of the background index and the energy resolution divided by the signal detection efficiency enters. This quantity is for GERDA $0.006$ cts/(mol-yr-$δE$) (normalized to mole

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1At the time of writing EXO announced an updated result [27] based on a 3.8-fold exposure. The sensitivity is $1.9 \cdot 10^{25}$ yr (90% C.L.) however the limit is only $T^{0ν}_{1/2} > 1.1 \cdot 10^{25}$ yr (90% C.L.). We restrict our discussion to the published value.
Fig. 8. Comparison of recent $T_{1/2}^{0\nu}$ limits for $^{76}$Ge and $^{136}$Xe and correlations of the two half-lives for different matrix element calculations (assuming light neutrino exchange). The calculations are from Ref. [28] (EDF), [29] (ISM), [30] (IBM), [31] (pnQRPA), [32] (QRPA) and [33] (SKM-HFB-QRPA). No axial vector quenching is assumed, i.e. $g_A = 1.25$. $m_{ee}$ denotes the effective neutrino mass and values of 0.2 eV (diamonds), 0.3 eV (dots) and 0.4 eV (stars) are marked on all axes.

instead of kg), for EXO-200 about 0.044 cts/(mol·yr·$\delta E$) and for Kamland-Zen about 0.19 cts/(mol·yr·$\delta E$). This comparison explains why despite our lower exposure, GERDA reaches a half-life sensitivity which is a factor of 2 better compared to the published EXO-200 and Kamland-Zen values. However, for the calculation of physics parameters like the effective neutrino mass, also phase space factors and nuclear matrix elements enter which favor $^{136}$Xe (see Fig. 8). Note, that quenching of the axial vector coupling could change the conversion strongly and heavier nuclei are typically more affected [30].

5. Summary

GERDA collected in a first phase of data taking 21.6 kg·yr of exposure with a background of about 0.01 cts/(keV·kg·yr) (after pulse shape discrimination). We performed a blind analysis and found no signal of $0\nu\beta\beta$ decay. Hence we place a limit of $T_{1/2}^{0\nu} > 2.1 \cdot 10^{25}$ yr for $^{76}$Ge at 90% C.L. The claimed $0\nu\beta\beta$ signal is ruled out with 99% probability in a model independent way.

In a second phase, the experiment aims to improve the background to a level of 0.001 cts/(keV·kg·yr).

References


