A Measurement of the Nuclear Enhancement in High $E_t$ and Jet Event Production

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Abstract

Properties of events produced with high values of transverse energy ($E_T$) in 800 GeV/c proton-nucleus collisions are presented. Both full-azimuth and limited aperture high $E_T$ triggers were used to select events from six targets (H, Be, C, Al, Cu, and Pb). The events were collected using the large acceptance Fermilab multiparticle spectrometer that recorded almost 95% of the incoming beam energy. The $A$ dependence of the cross sections at a given $E_T$ was parameterized as $A^\alpha$. The value of $\alpha$ increases from 0.7 at low $E_T$ to a plateau at high $E_T$ of approximately 1.6. The high $E_T$ value of $\alpha$ is slightly smaller for the limited aperture triggers. A strong dependence of $\alpha$ on the event structure was observed; "jet-like" events exhibit an $A$ dependence consistent with $\alpha=1.0$, while for more isotropic events $\alpha$ is much larger. This observation is consistent with the expected behavior for jet production in pA collisions.

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1. Introduction

High energy collisions of protons with nuclei (pA) have been studied and compared with proton-proton (pp) collisions primarily to measure the effect of interactions of secondaries produced in the initial scatter with other nucleons in the nucleus [1]. These studies have led to a better understanding of the space-time development of the intermediate hadronic matter. Of particular interest are collisions that produce large amounts of transverse energy (Et) relative to the incident beam direction. Two competing mechanisms are believed to be responsible for such collisions: 1) multiple soft-scattering involving many nucleons within the nucleus, and 2) hard-scattering of constituents that can produce high Pt jets which then propagate through the nucleus. Previous experiments [2-6] have found a strong nuclear dependence for the production of high Et events. In this paper results are presented from experiment E557/E672 which expand these measurements and further isolate the hard-scattering component by using a higher beam momentum (800 GeV/c protons, pp \(\sqrt{s}=38.8\) GeV) and larger event samples collected with a variety of triggers and targets.

Data from pp and pA high Et collisions were taken with the large acceptance Fermilab Multiparticle Spectrometer (MPS). Several triggers with different apertures were employed because of their varying efficiencies in collecting hard-scatters and because of their various degrees of bias. Large aperture triggers predominantly select soft collisions whereas small aperture triggers are more likely to be dominated by hard scatters [7]. The transverse event structure in the central region was used to further enhance the hard-scattering component of the event sample. Transverse
event structure was quantified by the planarity variable $P$ (section 5). The high planarity $pp$ events with high $E_t$ in a small aperture predominantly result from hard-scattering[8,9].

In this experiment, energy deposition in the backward, central, and forward rapidity regions was measured. Results from this paper concentrate on particles produced in the central rapidity region (-0.85 $\leq \eta^* \leq$ +0.85, where pseudorapidity $\eta^* = -\ln(\tan \frac{\theta^*}{2})$, and $\theta^*$ is the center of mass polar angle for massless particles). Cross sections as a function of $E_t$ and planarity for several different targets and trigger apertures are presented. The $A$ dependence of these cross sections (per nucleus) is parameterized in the standard $A^{\alpha}$ form. The validity of the $A^{\alpha}$ form for all the cross sections that were measured is discussed; the values of $\alpha$ as a function of $E_t$, and the variation of $\alpha$ with the planarity variable (which is related to the $A$ dependence of hard-scattering in $pA$ interactions) are presented.

This paper is organized as follows: A brief description of the apparatus and the triggers are given in Section 2. Summary of the data sample and cuts on the data are described in Section 3. Cross sections as a function of $E_t$ and their $A$ dependence are presented in Section 4. The $A$ dependence of the event structure as determined by planarity is given in Section 5. Conclusions are presented in Section 6.

2. Apparatus

The layout of the Fermilab MPS facility for the 1084 E557/E672 run is shown in Figure 1. The beam consisted of 800 GeV protons directly extracted to the Fermilab
MT beam line. A typical beam intensity consisted of 20 - 80 x 10^6 protons per 20 second spill which occurred once every minute. For pp data the beam was incident on a 45 cm liquid hydrogen target; for pA data nuclear targets of Be, C, Al, Cu, and Pb replaced the hydrogen target and were constructed of three successive foils thin enough to avoid significant re-scattering (see Table 1). Targets of different atomic number were periodically changed back and forth to check for systematic differences in the interaction and trigger rates. Multiwire proportional chambers (49 planes of 17000 wires) and drift chambers (8 planes of 1472 wires) detected charged particles. Charged particle momenta were measured using a spectrometer magnet that provided a 0.4 GeV/c p_T kick. The proportional chambers and drift chambers were not used in this analysis except in determining the interaction vertex position.

A series of highly segmented calorimeters, denoted by the names Wide Angle (WAN), Insert (INS), Forward (FWD) and Beam (BM) was able to measure 95% of the incident energy. Each of these calorimeters consisted of an electromagnetic section followed immediately downstream by a fully absorptive hadronic section. Parameters for these calorimeters are given in Table 2. The geometry and granularity of the WAN, INS, and FWD calorimeters are shown in Figure 2.

As indicated in Figure 2 and Table 2 the combined geometrical acceptance of the WAN and INS calorimeters was complete in the azimuth in the polar angular range 25° ≤ θ ≤ 135° (-0.85 ≤ η ≤ +1.5) as measured in the pp center of mass frame for massless particles. In addition to the downstream calorimeters, a ver-
tex detector surrounded the target with 236 proportional tubes and 82 lead glass modules in order to detect secondaries produced in the target fragmentation region. Preliminary results from target region data are given in reference [10].

Between the WAN and INS calorimeter and the FWD calorimeter was placed a muon detector, consisting of four proportional chambers and a large, steel-core toroidal magnet (see reference [11] for details). A hole through the chambers and the toroid of approximately 12 mrad in lab polar angle allowed forward-moving particles to reach the FWD and BM calorimeters.

The WAN and INS calorimeters served both as a trigger and a detector of neutral and charged particles. The trigger [12] was based on several conditions:

(i.) An inelastic collision was demanded by requiring a beam proton coincident with a pulse height corresponding to 4 minimum ionizing particles in a scintillation counter (DEDX) located immediately downstream of the target. This "interacting beam" (IB) trigger was sensitive to approximately 90% of the total pp inelastic cross section.

(ii.) The next requirement was that the incident proton be unaccompanied by another beam particle within ± 24 ns. Pulse height information from a scintillation counter was used to discriminate against beam rf buckets containing more than one particle. In order to prevent event pile up within the 125 ns calorimeter ADC integration time, interactions (as defined by DEDX) which occurred within ± 150 ns of another interaction were vetoed.

(iii.) The final level of the trigger required that the $E_T$ detected in a section
(aperture) of the calorimeter exceed a threshold. Thresholds for different apertures were set independently so that data from 22 different calorimeter trigger apertures could be collected simultaneously.

The trigger apertures were defined as combinations of the WAN and INS modules divided into four azimuthal sections and four polar angle sections. Here we present data collected with:

- the global trigger, which covered the central rapidity region.
  
  The global aperture covered the full azimuth and pp CM polar angles $45° < \theta^* < 135° \ (-0.85 < \eta^* < +0.85)$.

- a Reduced Global (RG) trigger, which was restricted to polar angles $60° < \theta^* < 120° \ (-0.55 < \eta^* < +0.55)$.

- a Small Aperture (SA) trigger which covered the same polar region as RG but only one quarter of the full azimuthal angle.

Figure 3 shows the geometry of these three trigger apertures. Various thresholds for each of the calorimeter triggers were selected so that a wide range of $E_t$ was covered for each target and aperture.

One of the more important details of the apparatus was the energy resolution of the calorimeters. The absolute energy scale of the calorimeter modules was set before data taking in a series of calibration runs with an 80 GeV incident beam. Each module’s resolution was measured during the calibration. Calorimeter module energy resolution is given in Table 2 in terms of a resolution coefficient, $K$; where the energy detected in a module has a relative uncertainty of $\sigma(E)/E = K/\sqrt{E}$(GeV).
The calibration was re-checked in another series of runs after the data taking was finished. The shifts in module responses found between the two calibrations were consistent with shifts determined using a laser monitoring system; they were typically less than 10% for modules in the WAN calorimeter. The corresponding shifts in module gains (conversion to energy in GeV) used in this analysis were constantly updated by the laser monitoring system. Another correction to the absolute energy scale was needed because the responses of electromagnetic modules were greater for incident electrons than for hadrons. This effect was measured during calibration and was found to be small for the WAN (16%), medium for the INS lead glass modules (55%) and large for the FWD calorimeter (125%). This effect, combined with the inherent module energy resolution, energy leakage from modules, and the \( p_t \) kick of the spectrometer magnet contributed to a experimental \( E_t \) resolution function for each aperture. These effects were simulated using two Monte Carlo models (ISAJET [13] and a gluon bremsstrahlung model[14]) in order to determine the \( E_t \) resolution. The net effect of the \( E_t \) resolution on the exponentially falling \( E_t \) distributions presented in section 4. was a decrease of 17% in the global aperture \( E_t \) (\( E_t(\text{global}) \) is the \( E_t \) measured within the global aperture) scale, 16% in the RG aperture \( E_t \) (\( E_t(\text{RG}) \) is the \( E_t \) measured within the RG aperture) scale, and 8% in the SA aperture \( E_t \) (\( E_t(\text{SA}) \) is the \( E_t \) measured within the SA aperture) scale. The two Monte Carlo models agreed on the size of the \( E_t \) shifts to within 2%. After including this \( E_t \) shift, the total uncertainty in the \( E_t \) scales was estimated to be 7%.
3. Data

Table 1 summarizes the run statistics for all targets and number of events used in this analysis. Data were collected over a one month running period. The sample of events used to measure the cross sections here was selected based on three types of cuts:

(i.) A vertex cut discarded events with vertices outside the target volume. Figure 4 shows vertex distributions for the hydrogen target and a lead target for both high $E_t(\text{global})$ and low $E_t(\text{global})$ data. In all cases the target outline is clearly identified. For low values of $E_t(\text{global})$, $E_t \lesssim 5$ GeV, half of the interactions in the target were cut due to low charged multiplicity vertex finding inefficiencies. The vertex finding efficiency for events with $E_t(\text{global})$ above 5 GeV increased to 100%. No correction for this vertex finding inefficiency at low $E_t$ has been made. The peaks at the edges of the hydrogen target (outside of the target volume) for the high $E_t$ run were due to the enhanced cross section of the target walls, made of mylar, which have a higher effective A.

(ii.) A cut on total energy ($E_{tot}$) measured in the calorimeters of $400 \text{ GeV} < E_{tot} < 1100 \text{ GeV}$ was applied. Figure 5a shows the distribution of $E_{tot}$ for pp data. The average $E_{tot}$ is 740 GeV (92% of the energy available from the 800 GeV proton beam) and the FWHM of $E_{tot}$ is equal to 150 GeV when the largest fraction of the total energy is deposited in the WAN calorimeter. Figure 5b shows $< E_{tot}>$ as a function of $E_t(\text{global})$. The contributions to $< E_{tot}>$ from individual calorimeters are also shown. The dominant contribution from the FWD and BM calorimeters at low $E_t(\text{global})$ became small at high $E_t$ where the WAN calorimeter detected
most of the energy. On the average the same amount of total energy was measured irrespective of which of the calorimeters provided most of the energy.

(iii.) The final cut required that the observed $E_t$ in a given aperture exceed a predetermined $E_t$ threshold which was slightly greater than the threshold used by the trigger. This cut was designed to eliminate any hardware threshold efficiency effects on the data sample.

After cuts, approximately 30% of the recorded data has been used.

4. Cross Sections

The interacting beam (IB) cross sections were calculated using scalar counts of beam and interactions and corrected for the target thickness. Empty target rates were subtracted directly so no vertex or energy cuts were used to calculate the IB cross sections. The pulse threshold of the DEDX counter was set to a signal corresponding to approximately four charged particles. The measured pp IB cross section, $29.1 \pm 2$ mb, corresponded to 90% of the total inelastic pp cross section, $32.1 \pm 0.7$ mb [15]. This difference in cross sections is consistent with bubble chamber measurements [15] of topological cross sections for 2, 4, and more charged particles. Figure 6 shows a plot of the IB cross sections as a function of atomic number $A$. For comparison, values of the total inelastic pA cross sections taken from reference [15,16] are also shown. The pA data were fitted to a $\sigma_{IB} = \sigma_0 A^\alpha$ parameterization. The fit gives $\sigma_0 = 37.6 \pm 0.5$ mb and $\alpha = 0.71 \pm 0.05$, in agreement with previous measurements at lower energy [16].

Sample $d\sigma/dE_t$ differential cross sections are plotted as a function of $A$ in
Figure 7 for three $E_t(globa1)$ bins. Data from several high $E_t(globa1)$ triggers and the IB trigger were combined to obtain the $d\sigma/dE_t$ cross sections. Figure 7 shows that the $A^\alpha$ parameterization fit the data well. Values of $\alpha$ at the given $E_t(globa1)$ bin were the slopes of the $\log(d\sigma/dE_t)$ vs. $\log(A)$ plots. Hydrogen was not included in the slope calculation (Hydrogen points usually lay below the pA fitted line so that the value of $\alpha$ would increase slightly if hydrogen were included in the $A^\alpha$ fit).

The $d\sigma/dE_t$ cross sections for the entire range of $E_t(globa1)$ is shown in Figure 8a for all targets. The integrated pp cross section from Figure 8a was approximately half of the total IB cross sections plotted in Figure 6. This loss was a result of the 50% vertex finding efficiency at low $E_t$ discussed in the previous section. Values of $d\sigma/dE_t$ for events with $E_t(globa1) \geq 5$ GeV show no significant vertex finding problem due to their higher charged multiplicity at high $E_t$. Fitted values of $\alpha$ from all $E_t$ bins are plotted vs. $E_t(globa1)$ in Figure 8b; $\alpha(E_t)$ rises from 0.7 at low $E_t$ to a plateau value of 1.6 at $E_t$ around 20 GeV.

In comparison with more recent p-Pb data from reference [17] the p-Pb $d\sigma/dE_t$ cross section presented here Figure 8a had an extremely low probability (less than $10^{-7}$) of exceeding the pp kinematic limit (38.8 GeV). This is due to the difference between the kinematic regions covered by the two experiments. The acceptance of the calorimeter in reference [17] covered the backward rapidity region and the p-Pb $d\sigma/dE_t$ cross section presented here covered only the central rapidity region.

Results for the reduced global (RG) trigger and the small aperture (SA) trigger are plotted in Figure 9a and Figure 10a. The corresponding $\alpha$ vs. $E_t(RG)$ and
vs. \( E_t(\text{SA}) \) plots show a similar tendency to rise and level off as the global trigger data. In the case of the small aperture trigger the plateau value of \( \alpha \) is significantly lower (by 0.2) than that obtained using the global aperture. This lower value of \( \alpha \) may be due to a difference in the processes that dominate the global trigger and the smaller aperture trigger event samples. This possibility is discussed in section 5.

The \( E_t \) scale correction, determined by Monte Carlo simulation (section 3.), may \textit{a priori} have had some \( A \) dependence due to differences in the event structure for various \( pA \) interactions. In order to check this possibility, the energy averaged polar angle in the global aperture, \( \langle E_t/E \rangle \), as a function of \( E_t(\text{global}) \) for several targets was plotted in Figure 11. At any given value of \( E_t(\text{global}) \), the energy weighted average polar angle in the global aperture differed by less than 5% when lead events were compared with carbon events. Therefore there was little \( A \) dependence of the polar event structure in the central rapidity region (this effect is discussed in more detail in reference [10]). It is estimated that the small differences in \( \langle E_t/E \rangle \) in the nuclear data could result in a systematic shift in \( \alpha \) of \( +0.05 \). Systematic effects of the vertex finding efficiency on the values of \( \alpha \) at low \( E_t(\text{global}) \) were estimated to be less than \( \pm0.2 \); the low \( E_t \) values of \( \alpha \) were consistent with the interacting beam \( A \) dependence with \( \alpha \approx 0.7 \).

A similar nuclear enhancement of \( d\sigma/dE_t \) cross sections at high \( E_t \) has been observed in previous experiments [2-6]. These previous measurements have been expanded here to higher energy using improved statistics that have enabled systematic
studies of the aperture dependence. Asymptotic values of $\alpha$ at high $E_t$ presented here (1.4 for SA and 1.6 for global) are somewhat higher than those previously published. The initial rise of $\alpha$ with $E_t$ is expected from known low $p_t$ multiplicity distributions for $pA$ collisions [18]. More sophisticated models for soft hadron-nucleus involving multiple collisions have been constructed that successfully agree with $\alpha(E_t)$ data at lower beam energies [19]. These new results for the $A$ dependence of cross sections at high $E_t$ can be used to discriminate between detailed hadron-nucleus interaction models.

5. Event Structure

The difference in $\alpha$ for high $E_t$(SA) and high $E_t$(global) may be due to a difference in the fraction of hard-scatter events and soft-scatter events in the two samples. Transverse event structure in the central region can be used to isolate the “jet-like” events that are expected to arise from a hard-scattering mechanism. Transverse structure is often characterized by the planarity variable [20],

$$P = \text{MAX} \left( \frac{\sum p_t^2 - \sum p_{t \perp}^2}{\sum p_t^2 + \sum p_{t \perp}^2} \right).$$

where,

$P_t \perp$, $(P_t \parallel)$ ... is the perpendicular (parallel) component of a particle’s transverse momentum relative to an arbitrary transverse axis.

The axis in the transverse plane is chosen so that $P$ is maximized. Calorimeter module energies and positions are used to calculate $P_t$; only modules from the
global aperture contributed to the calculation. For back-to-back jet-like structures P approaches one; while for high multiplicity isotropic event structure P approaches zero. Figure 12a shows the planarity distribution for events with \( E_t(\text{global}) \) greater than 23 GeV. The resulting cross sections in a given planarity range are then plotted against A and the slope, \( \alpha(P) \), calculated. As before, hydrogen points were not included. For example, Figure 13 shows the results of these fits for three bins of planarity for high \( E_t(\text{SA}) \). The \( A^\alpha \) form once again is consistent with the data. As seen from Figure 12b, the values of \( \alpha(P) \) for events with \( E_t(\text{global}) \) above 23 GeV are consistent with 1.6 for all planarities.

Cross sections for the reduced global trigger (\( E_t(\text{RG}) \) > 16 GeV) and the small aperture trigger (\( E_t(\text{SA}) \) > 8 GeV) as a function of planarity are shown in Figure 14a and Figure 15a; the corresponding \( \alpha \) as a function of planarity is shown in Figure 14b and Figure 15b. The shapes of the \( d\sigma/dP \) cross section plots for obtained using reduced global and small aperture triggers were strongly dependent on the target; the small aperture trigger planarity distribution for Pb had an average planarity of \( <P> = 0.65\pm0.02 \) and for hydrogen the planarity distribution has \( <P> = 0.85\pm0.02 \). Consequently the values of \( \alpha \) show a significant drop from 1.6 for \( P< 0.7 \) to approximately \( 1.0 \pm 0.1 \) at planarity approaching one. This decrease could be a result of hard-scatters dominating the cross section at high planarity with high \( E_t \) in a small aperture. Similar values of \( \alpha \) have been measured in high \( P_t \) single particle experiments [21,22] and an A dependence consistent with \( \alpha \approx 1.0 \) is also seen in reference [23] for highly planar events.
Several predictions for the $A$ dependence of hard scattering have been made. Values of $\alpha$ near or slightly above one are expected because the cross section should be proportional to the number of constituents within the nucleus. Corrections due to the structure of the nucleus [24], Fermi motion [25], and jet re-scattering [26], increase the predicted value of $\alpha$ for the hard scattering cross section to 1.1 or 1.2. The result presented here is the most direct indication of the $A$ dependence of a hard scattering cross section measured in a calorimeter/jet experiment to date.

6. Conclusions

High $E_t$ interactions of incident 800 GeV/c protons with nuclear and hydrogen targets were detected by a system of calorimeters that covered $\approx 90\%$ of the CM solid angle. The $d\sigma/dE_t$ differential cross sections vs. $E_t$ for various triggering apertures and targets have been measured and the nuclear $A$ dependence extracted. The $A$ dependence of the cross sections are described well by the $A^\alpha$ parameterization. Values of $\alpha$ rose from 0.8 at low $E_t$ to 1.6 at high $E_t$(global) and to 1.4 for high $E_t$(SA) in a small aperture. In order to enhance the hard scatter component of the cross section the planarity variable was used to tag jet-like events. The $d\sigma/dP$ differential cross sections for the high $E_t$ events production have been measured as a function of planarity and their $A$ dependence once again was consistent with the $A^\alpha$ parameterization. The value of $\alpha$ decreased with increasing planarity for small aperture triggered events, while for global triggers it did not show a significant dependence on planarity. The value of $\alpha$ for the production of jet-like events approached $1.1 \pm 0.1$ in agreement with various predictions for the
A dependence of hard scattering.

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<table>
<thead>
<tr>
<th>Target</th>
<th>Thickness (g/cm²)</th>
<th>Events recorded</th>
<th>Events used</th>
<th>Luminosity (nb⁻¹)</th>
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<tr>
<td>Hydrogen</td>
<td>3.24</td>
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<td>138×10⁵</td>
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### TABLE 1.

<table>
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<th>Calorimeter type</th>
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<th>pp CM acceptance</th>
<th>Absorption lengths</th>
<th>Radiation lengths</th>
<th>Resolution Coeff.</th>
<th>number of modules</th>
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<td>145→ 45</td>
<td>-1.1 → 0.8</td>
<td>0.8</td>
<td>16</td>
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<td>-1.1 → 0.8</td>
<td>3.8</td>
<td>32</td>
<td>0.9</td>
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<td>Fe-scint</td>
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<td>18</td>
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<tr>
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<td>1.3 → 3.1</td>
<td>10</td>
<td>97</td>
<td>1.5</td>
</tr>
<tr>
<td>BEAM E/M</td>
<td>Pb-scint</td>
<td>5→ 0</td>
<td>&gt; 3.1</td>
<td>0.8</td>
<td>15</td>
<td>0.4</td>
</tr>
<tr>
<td>BEAM hadronic</td>
<td>Fe-scint</td>
<td>5→ 0</td>
<td>&gt; 3.1</td>
<td>10</td>
<td>100</td>
<td>1.5</td>
</tr>
<tr>
<td>TOTAL</td>
<td></td>
<td>145→ 0</td>
<td>&gt; -1.1</td>
<td>*</td>
<td>*</td>
<td>*</td>
</tr>
</tbody>
</table>

### TABLE 2.
Figure 1. Apparatus layout for the E557/E672 1984 run.

Figure 2. Calorimeter granularity and center of mass angle coverage for massless particles.

a. Wide angle (WAN) and insert (INS) electromagnetic calorimeters. Circles represent polar angles of 45°, 90°, and 135° in the CM frame.

b. Forward (FWD) EM calorimeter. Circles represent polar angles of 10°, 20°, and 30° in the CM.
Figure 3. Trigger apertures in the WAN and INS calorimeters. Circles represent the same polar angles as in Figure 2a. 
   a. Global aperture,  b. Reduced Global (RG) aperture,  c. Small Aperture (SA); one out of the four SA apertures.

Figure 4. Vertex distributions for the hydrogen and lead targets. The solid lines are for triggers with high 
   $E_k$ thresholds and the dashed lines are for IB triggers (with no $E_k$ thresholds).
   a. Liquid hydrogen target. Events with $-1.85m < z < -1.55m$ survive the vertex cut.
   b. Lead target foils. Events with $-1.85m < z < -1.45m$ survive the vertex cut.
Figure 5. Total energy measured in the calorimeters.

a. Total energy ($E_{\text{tot}}$) distribution for pp data. Events with $400 \text{ GeV} < E_{\text{tot}} < 1100 \text{ GeV}$ survive the energy cut.

b. Average $E_{\text{tot}}$ vs. $E_t$ (global) for pp data. $E_t$ (global) is the transverse energy measured in the global trigger aperture. Also shown in the plot are the contributions to the total energy of individual calorimeters.

Figure 6. A dependence for the interacting beam (IB) cross sections. The dashed line represents a fit to the $A^\alpha$ parameterisation (not including hydrogen). Different target thicknesses yielded consistent cross sections and were averaged in this plot. Also shown in the plot are data from references [15,16].
Figure 7. $d\sigma/dE_t$ cross sections vs. $A$ for three sample $E_t$ (global) bins. Solid lines represent fits of the $A^\alpha$ parameterization to the Be, C, Al, Cu, and Pb data. Hydrogen is not used in the fit.

a. $6.5 < E_t < 7.0$ GeV  
   $\alpha = 1.04 \pm 0.1$

b. $21.0 < E_t < 21.5$ GeV  
   $\alpha = 1.66 \pm 0.1$

c. $25.0 < E_t < 25.5$ GeV  
   $\alpha = 1.66 \pm 0.2$
Figure 8. Global trigger cross sections. The $E_t$ scale in these plots have been corrected 17% for the calorimeter resolution discussed in the text. Error bars are statistical only; any run dependent systematic errors are not included.

a. $d\sigma/dE_t$ vs. $E_{t\text{ (global)}}$ for all targets. Al and Cu data were taken only at high $E_t$.

b. $\alpha$ vs. $E_t$. Only pA data (not hydrogen) data is used in the $A^{\alpha}$ fit for this plot and all consequent $\alpha$ vs. $E_t$ plots.
Figure 9. Reduced global trigger cross sections. The $E_t(RG)$ scale has been corrected 16% for calorimeter resolution.

a. $d\sigma/dE_t$ vs. $E_t(RG)$ for all targets. b. $\alpha$ vs. $E_t(RG)$.
Figure 10. Small aperture trigger cross sections. The $E_t(SA)$ scale has been corrected 8% for calorimeter resolution.

a. $d\sigma/dE_t$ vs. $E_t(SA)$ for all targets.  
b. $\alpha$ vs. $E_t(SA)$.  

$H_2$, $Be$, $C$, $Al$, $Cu$, $Pb$
Figure 11. Average global $E_T/E$ vs. $E_T$ (global) for several targets. Atomic number $A$ dependence in the energy averaged polar angle within the global aperture, $<E_T/E>$, could result in an $A$ dependence for the calorimeter $E_T$ resolution. The $A$ dependence of $<E_T/E>$ at low values of $E_T$ may be affected by a run dependent systematic error.
Figure 12. Global trigger planarity for high $E_T$ (global) events. Planarity is measured using modules in the global trigger aperture.

a. $d\sigma/dP$ for $E_T$ (global) $> 23$ GeV. Beryllium data is not shown in this plot (as well as the RG and SA plots), due to large statistical errors.

b. $\alpha$ vs. $P$ from the global cross sections. Be, C, Al, Cu, and Pb data (not hydrogen) was used in the $A^\alpha$ fit.
Figure 13. Three sample $d\sigma/dP$ differential cross sections vs. $A$ for $E_t(SA)> 8$ GeV. Solid lines represent fits to
the $A^\alpha$ parameterisation
a. Planarity 0.4 to 0.45.
b. Planarity 0.7 to 0.75.
c. Planarity 0.9 to 0.95.
Figure 14. Reduced global trigger planarity for high $E_t(RG)$. Planarity is measured using modules in the global trigger aperture.

a. $d\sigma/dP$ at $E_t(RG) > 16$ GeV.

b. $\alpha$ vs. $P$ from the reduced global cross sections. pA data (not hydrogen) has been used in the $A^\alpha$ fit.
Figure 16. Planarity distributions for high $E_t$(SA). Planarity is measured using modules in the global trigger aperture.

a. $d\sigma/dP$ at small aperture $E_t$(SA) > 8 GeV.
b. $\alpha$ vs. $P$ from the small aperture cross sections. Hydrogen data has not been used in the $A^\alpha$ fit.