

Article

Studies of Deformed Halo Structures of ^{39}Na and ^{42}Mg

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Abstract: **Background:** The recent experimental discovery of drip-line nucleus ^{39}Na has attracted great interest in theoretical studies of exotic nuclear structures in this mass region. **Methods:** We solve the Skyrme–Hartree–Fock–Bogoliubov (Skyrme–HFB) equation within deformed coordinate-spaces. The present approach is suitable for descriptions of weakly bound deformed nuclei with continuum effects and deformed halo structures. **Results:** The systematical two-neutron separation energies are obtained with the SkM*_{ext1} and UNEDF0_{ext1} forces for Na and Mg isotopes close to the neutron drip line. The density distributions show that ^{39}Na and ^{42}Mg have deformed halo structures. Furthermore, there are significant influences of various pairing interactions on halo shapes at large distances. **Conclusions:** Both ^{39}Na and ^{42}Mg are very weakly bound with well prolate deformed cores. However, their surface halo structures are dependent on the choices of pairing interactions. The volume-type pairing interaction tends to predict a prolate deformed halo, while the halo deformations at large distances are reduced by adopting the surface pairing. We demonstrate that ^{39}Na and ^{42}Mg are promising candidates for two-neutron deformed halo nuclei.



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Keywords: deformed halos; Hartree–Fock–Bogoliubov; pairing interaction

1. Introduction

Exploring exotic nuclear structures far away from the β -decay stable line is one of the major scientific goals in rare-isotope beam facilities around the world. Of particular interest is the halo structure, which is characterized by significant extensions of neutron or proton density distributions at nuclear surfaces [1–6]. There were extensive experimental studies to look for halo structures [7]. Some one-neutron and two-neutron halos have been discovered by experiments, which have attracted strong theoretical interests. However, deformed halo structures are rare, and two-neutron deformed halos are still absent in nature.

Recently, the drip-line nuclei ^{31}F and ^{34}Ne have been reconfirmed by experiments in RIKEN [8]. In this experiment, one event of ^{39}Na was also observed. ^{39}Na is mostly likely to be the drip line of sodium isotopes and is a promising two-neutron halo nucleus. Besides, the neighboring ^{40}Mg has been observed [9] and the drip line of magnesium is still not known. Both ^{39}Na and ^{40}Mg have a magic neutron number $N = 28$, but this neutron shell is broken near the neutron drip line [10]. Previous theoretical studies have consistently predicted that ^{40}Mg is a prolate deformed nuclei [10–12]. In deformed weakly bound nuclei, the interplay between continuum, pairing correlations, halo structures and deformations is particularly intriguing.

The suitable microscopic tool for descriptions of weakly bound deformed nuclei in the framework of nuclear density functional theory is the coordinate-space formulation of the Hartree–Fock–Bogoliubov (HFB) method [13,14]. The ab initio methods can also describe weakly bound spherical nuclei, but this is difficult for deformed shapes. The coordinate-space HFB can discretize the quasiparticle continuum and resonances rather precisely and is able to describe deformed halo asymptotics within large boxes. In HFB calculations,

Skyrme forces [15] are commonly adopted as non-relativistic effective nucleon–nucleon interactions. There are many Skyrme parameterizations developed with different physics purposes. For example, SkM* forces [16] are widely used in fission studies for reasonable descriptions of fission barriers. SLy4 force [17] has good isotopic properties towards drip lines and is widely used in descriptions of neutron stars. UNEDF0 force [18] has a very small rms of 1.455 MeV regarding global binding energies. Furthermore, extended Skyrme forces with additional higher-order density dependent terms are expected to improve the global theoretical descriptions [19,20]. Generally, different effective interactions can lead to very different drip-line locations although they all are good at descriptions of stable nuclei.

In the present work, we aim to study deformed halo structures of ^{39}Na and ^{42}Mg . The calculations are performed based on the self-consistent Skyrme-HFB approach in a large, axially symmetric coordinate-space. We expect the two-neutron deformed halos could be confirmed experimentally in the near future.

2. The Theoretical Framework

The Skyrme-HFB calculations are performed with the HFB-AX solver based on the B-spline method in a two-dimensional coordinate space [13]. Such an approach has been successfully used to describe the properties of weakly bound deformed nuclei around the neutron drip line. Generally, with a sufficiently large box and small mesh sizes, the description of the continuum spectrum would be very precise [14]. In present calculations, we adopt a coordinate-space of 21 fm and a maximum lattice mesh of 0.6 fm, respectively.

The HFB equation in the coordinate-space can be written as [13,21]:

$$\begin{bmatrix} h(r) - \lambda & \Delta(r) \\ \Delta^*(r) & h(r) - \lambda \end{bmatrix} \begin{bmatrix} U_k(r) \\ V_k(r) \end{bmatrix} = E_k \begin{bmatrix} U_k(r) \\ V_k(r) \end{bmatrix}, \quad (1)$$

where h is the single-particle Hamiltonian; λ is the Fermi surface energy or chemical potential; Δ is the pairing potential; U_k and V_k are the upper and lower components of quasi-particle wave functions; and E_k denotes the quasi-particle energy. For the particle-hole interaction channel, the SkM*_{ext1} and UNEDF0_{ext1} [20] forces are adopted in $h(r)$, respectively. Note that SkM*_{ext1} and UNEDF0_{ext1} forces include an additional higher-order density-dependent term as in Ref. [19]. In the particle-particle channel, a density-dependent pairing interaction is adopted as follows [22,23],

$$\Delta(r) = V_0 \left\{ 1 - \eta \left[\frac{\rho(r)}{\rho_0(r)} \right]^\gamma \right\}, \quad (2)$$

where $\rho_0(r)$ is the nuclear saturation density of 0.16 fm^3 and V_0 , η , γ are three adjustable parameters. For different η , γ , there are four types of pairing interactions:

1. Volume pairing: $\eta = 0$;
2. Surface pairing: $\eta = 1, \gamma = 1$;
3. Mix pairing: $\eta = 0.5, \gamma = 1$;
4. New pairing: $\eta = 0.8, \gamma = 0.7$.

With a pairing window of 60 MeV, we adjusted pairing strength V_0 with the SkM*_{ext1} force to regularize the neutron pairing gap of ^{120}Sn to be $\Delta_n = 1.245 \text{ MeV}$. The adjusted pairing strengths V_0 are 146.5 MeV, 467.5 MeV, 233.5 MeV, and 389.8 MeV corresponding to volume, surface, mix, and new pairing types, respectively. Note that results with different pairing interactions are more or less similar for stable nuclei. However, the pairing gaps could be very different towards drip lines by using different pairing interaction forms [23]. The surface pairing would lead to very large pairing gaps towards the neutron drip line, while volume pairing is on the contrary. The mixing pairing and new pairing are between the surface and volume pairings [23].

The particle density $\rho(r)$ and the pairing density $\tilde{\rho}(r)$ of even–even nuclei are expressed as,

$$\begin{aligned}\rho(r) &= 2 \sum_k V_k^*(r) V_k(r), \\ \tilde{\rho}(r) &= -2 \sum_k V_k(r) U_k^*(r),\end{aligned}\quad (3)$$

where in the sum, the quasiparticle energy cutoff is taken as $(60 - \lambda)$ MeV. To describe the odd-mass nuclei, the quasiparticle blocking is invoked. By blocking quasiparticles at the state μ , the density $\rho_B^\mu(r)$ and the pairing density $\tilde{\rho}_B^\mu(r)$ of odd-mass nuclei become [24],

$$\begin{aligned}\rho_B^\mu(r) &= U_\mu(r) U_\mu^*(r) + V_\mu^*(r) V_\mu(r) + 2 \sum_{k \neq \mu} V_k^*(r) V_k(r), \\ \tilde{\rho}_B^\mu(r) &= -2 \sum_{k \neq \mu} V_k(r) U_k^*(r).\end{aligned}\quad (4)$$

Besides, the particle number equation for the odd-mass nuclei has to be modified. The quasiparticle blocking is necessary for descriptions of ^{39}Na .

3. Results and Discussion

Figure 1 shows the two-neutron separation energies S_{2n} of sodium isotopes and magnesium isotopes based on the $\text{SkM}_{\text{ext1}}^*$ force and $\text{UNEDF0}_{\text{ext1}}$ force with the new pairing interaction. As expected, calculated S_{2n} decreases gradually towards the drip line. In both calculations, ^{39}Na is the drip line nucleus. In experiments, ^{39}Na is mostly likely to be the drip line since only one event was observed [8]. For magnesium isotopes, $\text{SkM}_{\text{ext1}}^*$ predicts ^{42}Mg as the drip-line nucleus, while $\text{UNEDF0}_{\text{ext1}}$ predicts ^{44}Mg as the drip line. $\text{UNEDF0}_{\text{ext1}}$ also predicts a slightly larger S_{2n} for ^{39}Na than $\text{SkM}_{\text{ext1}}^*$. In fact, the drip-line locations of Na and Mg isotopes are very different by using various mass models. In the macroscopic–microscopic model, the drip line locations are at ^{39}Na and ^{40}Mg [25]. The WS4 model predicts that ^{37}Na and ^{40}Mg are the drip line nuclei [26], which slightly underestimates the neutron drip lines. The Gogny-HFB calculations with the D1S force [27] predict that the drip lines are at ^{35}Na and ^{40}Mg . The HFB-21 calculations [28] predict ^{37}Na and ^{42}Mg . The Relativistic-Hartree–Bogoliubov [29] predict ^{45}Na and ^{46}Mg as the drip lines, which significantly overestimate the neutron drip lines. Thus, ^{39}Na as the drip line provides a stringent constraint on various theoretical models. With this constraint, we can more confidently infer that ^{42}Mg is also weakly bound. However, it is difficult to predict whether ^{44}Mg barely exists or not.

The halo properties of ^{39}Na and ^{42}Mg are dependent on the choices of Skyrme forces. We display the rms radii of neutron distributions in Na and Mg isotopes in Figure 2. As shown in Figure 2, the neutron radii by $\text{UNEDF0}_{\text{ext1}}$ force increase almost linearly with increasing neutron numbers. It can be seen that the neutron radii by $\text{SkM}_{\text{ext1}}^*$ are particularly enhanced for ^{39}Na . Note that $\text{UNEDF0}_{\text{ext1}}$ predicts larger S_{2n} than that by $\text{SkM}_{\text{ext1}}^*$. Thus the larger neutron radii by $\text{UNEDF0}_{\text{ext1}}$ are not due to weakly bound effects, but due to larger deformations.

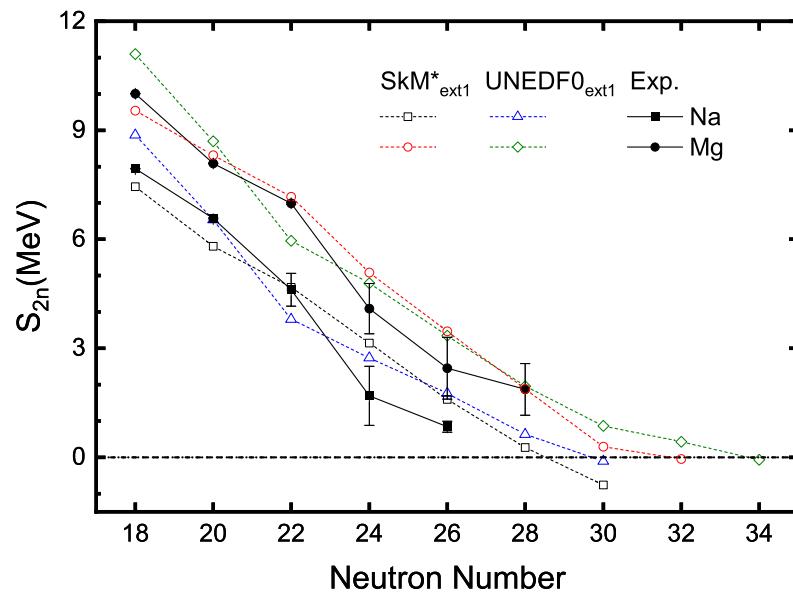


Figure 1. The two-neutron separation energies S_{2n} of Na and Mg isotopes obtained by the $\text{SkM}^*_{\text{ext1}}$ force and $\text{UNEDF0}_{\text{ext1}}$ force with the new pairing interaction. Experimental data labeled by solid symbols are taken from Ref. [30].

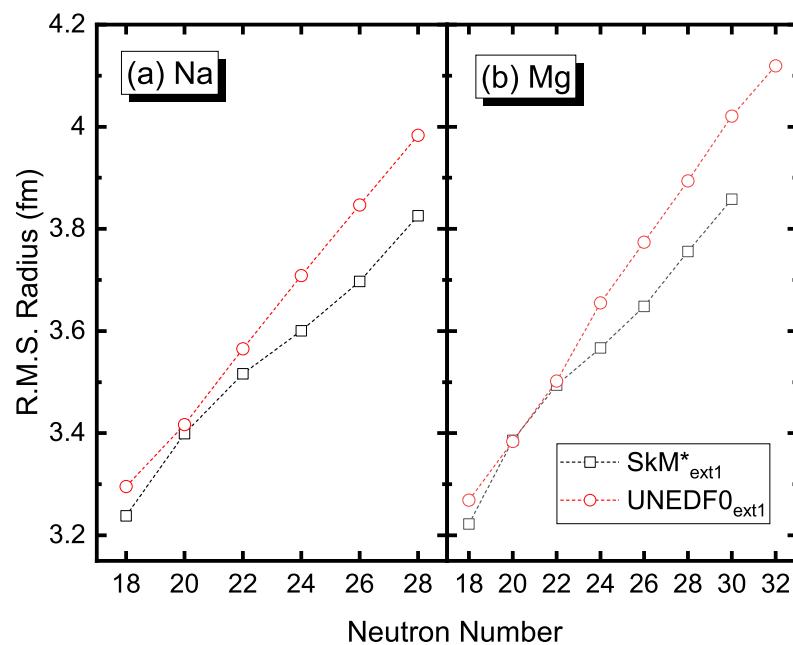


Figure 2. The calculated r.m.s. neutron radius in Na (a) and Mg (b) isotopes. Calculations are performed with $\text{SkM}^*_{\text{ext1}}$ and $\text{UNEDF0}_{\text{ext1}}$ forces, respectively.

It is expected that the pairing is crucial for descriptions of weakly bound nuclei. Presently, four types of pairing interactions are used: volume, surface, mix, and new pairing interactions. For ^{39}Na , the neutron Fermi energy λ_n and two-neutron separation energies S_{2n} are -0.20 MeV (0.82 MeV), -0.48 MeV (0.67 MeV), -0.16 MeV (0.63 MeV), and -0.26 MeV (0.27 MeV), corresponding to volume, surface, mix, and new pairing interactions, respectively. Figure 3 displays the deformed halo structures of density distributions by different pairing interactions and the $\text{SkM}^*_{\text{ext1}}$ force for ^{39}Na . The mixed pairing results in the highest neutron Fermi surface energy λ_n , and it predicts the most significant halo structures. On the contrary, the surface pairing has a lowest λ_n , and it is less weakly bound with a less prominent halo structure. It is understandable that the surface pairing

can bring more binding effects for weakly bound nuclei. The density distributions are shown in the cylindrical coordinates. The differences along z -axis and r -axis reflect the deformation effects in density distributions. We see that all the core density distributions have good prolate deformations. However, the surface halo shapes are very different. The surface pairing leads to the smallest surface deformations, while the volume pairing leads to the largest surface deformations. Hence, the surface halo deformations are very much dependent on the density dependencies of pairing interactions.

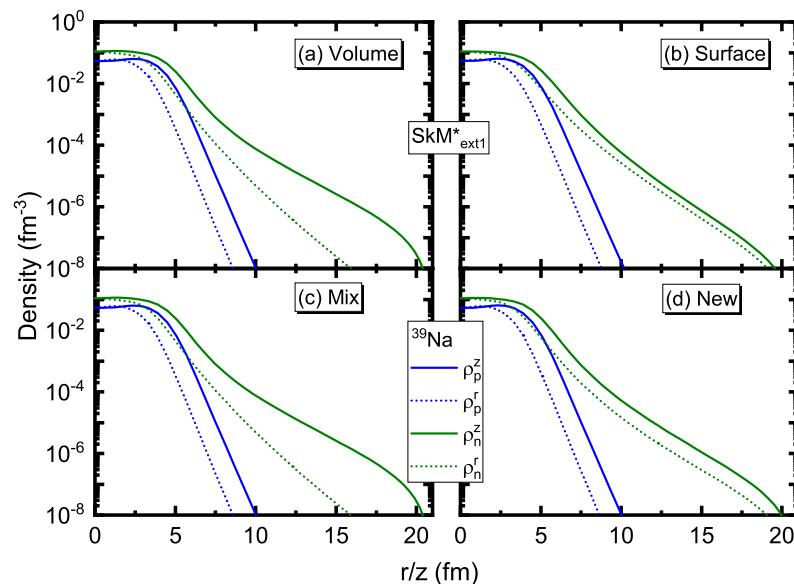


Figure 3. The density distributions of ^{39}Na obtained with various pairing interactions in the cylindrical coordinate spaces $\rho(r, z)$. Panel lists as (a) volume, (b) surface, (c) mix, and (d) new pairing interactions. The solid lines and dotted lines denote the density profiles along z -axis and r -axis.

Figure 4 shows the density distributions of ^{42}Mg by calculations with the $\text{SkM}^*_{\text{ext1}}$ force and various pairing interactions. Note that ^{42}Mg is slightly unbound with volume and mixing pairing interactions. For ^{42}Mg , the neutron Fermi energy λ_n (and two-neutron separation energies S_{2n}) is -0.43 MeV (-0.20 MeV), -0.50 MeV (0.66 MeV), -0.37 MeV (-0.12 MeV), and -0.32 MeV (0.29 MeV), corresponding to volume, surface, mix, and new pairing interactions, respectively. It is consistent with ^{39}Na that the surface pairing results in more binding energies and could slightly extend the neutron drip line. The core densities all have good prolate deformations. However, the surface halos by surface pairing and new pairing are almost spherical. This is similar to the situation of ^{39}Na . The different deformation between the core and the halo in weakly bound nuclei is called shape decoupling effect. Exotic shape decoupling effects in deformed halo nuclei are of strong interest [31]. The pygmy dipole resonance is a possible probe of shape decoupling effects [23].

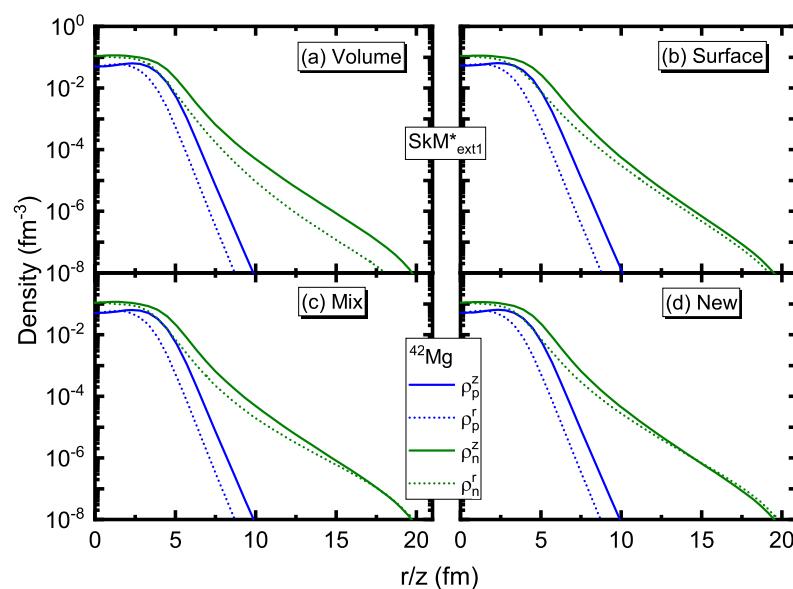


Figure 4. Similar to Figure 3, but for ^{42}Mg .

4. Conclusions

We have studied the deformed halo structures of drip-line nuclei ^{39}Na and ^{42}Mg , based on coordinate-space Skyrme-HFB calculations. The experimental discovery of ^{39}Na provides a stringent constraint on various theoretical models. With this constraint, we infer that ^{42}Mg is weakly bound. The problem is quite interesting because two-neutron deformed halos have still not been discovered yet. Both ^{39}Na and ^{42}Mg have a prolate deformed core, but their halo deformations could be different by adopting different pairing interactions. The surface pairing can bring more binding energies to weakly bound nuclei and tends to obtain spherical halos. The volume pairing results in significant deformed halos. In conclusion, the surface halo shapes are very much dependent on the density dependencies of pairing interactions.

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