

The Production of Massive Muon Pairs in π^- Nucleus
Collisions

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ABSTRACT

We present measurements of the differential cross section for the production of massive muon pairs in 225 GeV/c π^- -nucleus collisions. We have used the data between the ψ and T resonances in the framework of the Drell-Yan quark-antiquark annihilation model to predict the behavior of the cross section in the high mass ($m_{\mu\mu} > 11$ GeV/c²) region. The data are consistent with this extrapolation provided that a QCD leading $\log m^2$ evolution is included in the structure functions.

Lepton pair production in hadronic collisions has provided important information about the structure of hadrons. In the continuum mass region, experimental results are in qualitatively good agreement with the Drell-Yan model of quark antiquark annihilation.¹ The data do, however, show deviations from this "naive" model. The measured magnitude of the dimuon cross-section is larger than predicted (the K factor), as is the mean transverse momentum of the lepton pair. These effects have prompted the revision of the original model to include QCD corrections, which introduce scaling violations as a function of $m_{\mu\mu}^2$.²

To test these predictions, data on muon pair production are needed over a wide kinematic range. We report here results from an experiment which was designed to be especially sensitive in the high mass region, where "anomalous" scale breaking results have recently been reported.³

The experiment was carried out in the high intensity P-West area at Fermilab. A 225 GeV/c π^- beam was incident on a two interaction-length tungsten target, with the non-interacting beam and most of the hadronic debris from the target passing through a 20 mrad. tapered vacuum pipe to a dump downstream of the apparatus. The typical beam intensity was 5×10^8 pions/pulse. Muons produced in the target were momentum analyzed in a magnetized toroidal iron spectrometer. The beam and detector have been described in detail elsewhere.^{4,5,6} Reference 6 also contains a full description of the data analysis.

The detector was divided azimuthally into eight identical octants, each instrumented with seven planes of scintillation counters for triggering, and fifteen drift chamber planes for track reconstruction. A two level trigger required a target associated muon signature in two distinct octants. In the first level, the selection was made using matrix circuitry which operated on pairs of counter planes in the front half of the detector. The second level accepted a track if the struck counters through the full depth of the detector matched a muon trajectory pattern. The set of acceptable patterns was selected by Monte Carlo study to accept preferentially high transverse momentum target produced muons and reject beam halo muons.

Drift chamber hits associated with struck counters were used to identify and reconstruct tracks in each octant. Potential tracks were fit to two hypotheses. The constrained fit required a track to pass through the target center, while the unconstrained fit removed that requirement so that beam halo muons could be identified. A track was accepted if it had a constrained fit $\chi^2/\text{dof} < 3$, $p\Delta\theta < 1.5$ GeV/c, and $\Delta p/p < 0.3$, where $\Delta\theta$ (Δp) is the difference between the angles (momenta) determined by the constrained and unconstrained fits. The latter two criteria were found very useful in selecting good target associated tracks and rejecting halo muons.

The remaining background, from the accidental coincidence of uncorrelated target produced muons, was

measured using the spectra of target muons from the sample of events containing a target muon and a halo muon. We verified that this method reproduced the shape and normalization of our same sign dimuon data. This background is peaked at low masses, going from $\sim 17\%$ of the signal in the 4.5 to 5.5 GeV/c² mass interval to less than 1% for all masses greater than 7 GeV/c². We measured the background from non-target associated muon pairs with target out runs and found it to be less than 1% of the data.

The efficiency of the counters and the trigger were measured with special runs. A few counters were found to be slightly inefficient, and the Monte Carlo was correspondingly modified. The remaining uncertainties in the trigger efficiency were included in the estimate of the systematic errors. There was evidence of inefficiency in the drift chamber wires closest to the beam in the front of the spectrometer. Tracks going through these regions were eliminated from the final data sample, so that the result would be insensitive to the precise determination of the efficiency. The above cut predominantly affected the low mass region.

The acceptance of the apparatus and the effect of resolution smearing were calculated with a Monte Carlo simulation program. Monte Carlo events were generated with a dimuon mass ($m_{\mu\mu}$) and Feynman x (x_F) dependence given by the Drell-Yan formula:

$$\frac{d^2\sigma}{dm_{\mu\mu} dx_F} = \frac{8\pi\alpha^2}{9m_{\mu\mu}^3 (x_1+x_2)} \left[V^\pi(x_1)G(x_2) + S^\pi(x_1)H(x_2) \right]$$

where α is the fine structure constant, $x_F = 2p_{||}^*/\sqrt{s}$, and x_1 (x_2) represents the fraction of the beam (target) momentum carried by the annihilating quark. The variables x_1 and x_2 are related to $m_{\mu\mu}$ and x_F by $x_1 x_2 = m_{\mu\mu}^2/s$ and $x_F = x_1 - x_2$. G and H are linear combinations of the nucleon structure functions, for which we have used the EHLQ parameterization.⁸ $V^\pi(x_1)$ and $S^\pi(x_1)$ are the valence and sea structure functions of the pion and for a first iteration were taken from Ref. 7. The dimuon decay was parameterized by a $(1+\cos^2\theta)$ polar angle distribution in the Collins-Soper⁹ frame, and a flat distribution in azimuthal angle. The $p_{\perp}$ spectrum was assumed to be independent of the other variables as given by Ref. 7. The acceptance of the apparatus was found to be insensitive to the details of the model used. For the final extraction of the results, our parameterization for $V^\pi(x)$ and the $p_{\perp}$ distribution were used.

The Monte Carlo simulation included beam momentum spread, Fermi motion¹⁰, absorption in the target, multiple scattering and energy loss in the iron toroids, and the known inefficiencies of the apparatus. The generated events were reconstructed with the same programs used for the data.

We have extracted the pion valence structure function($V^\pi(x)$) from the continuum data below the T in order to study its extrapolation to high mass. The ψ and T resonances were eliminated with the requirement $4.5 < m_{\mu\mu} < 8.5$ GeV/c². To minimize the contribution from the pion sea, x_1

was required to be >0.25 . Figure 1 shows the $m_{\mu\mu}, x_F$ scatter plot of our data with the binning used for the fit. This sample contains 3327 events with an estimated background of 87 ± 10 events.

The structure function was extracted by simultaneously fitting the $m_{\mu\mu}$ and x_F dependence of the cross section given by Eq. 1 using the grid shown in Fig. 1. We used the following parameterization for the structure functions:

$$\begin{aligned} V^\pi(x) &= x^{\alpha^\pi} (1-x)^{\beta^\pi} / B(\alpha^\pi, \beta^\pi + 1) \\ S^\pi(x) &= A(1-x)^{8.5} \end{aligned}$$

where B is Euler's beta function, α^π was set to 0.5, and the normalization constant, A , was determined by the momentum sum rule with the fraction of pion momentum carried by the gluons equal to 0.47.⁷ We used the EHLQ⁸ parameterization for the nucleon structure function for the results presented here, but fits were performed with different formulae to test the sensitivity of our results.

QCD calculations predict that the structure functions should show logarithmic scaling violations. These are described in the leading log approximation by the Altarelli-Parisi¹¹ equations. They were included in the pion valence structure function using the method of Buras and Gaemers,¹² with the $m_{\mu\mu}^2$ dependence of α^π , β^π of the form $\alpha^\pi = \alpha_0^\pi + \alpha_1^\pi \bar{s}$, $\beta^\pi = \beta_0^\pi + \beta_1^\pi \bar{s}$, where $\bar{s} = \ln(\ln(m^2/\Lambda^2)/\ln(m_0^2/\Lambda^2))$, Λ is set to 0.2 GeV/c², and m_0^2 is set to $44 (\text{GeV}/c^2)^2$, the mean mass squared of the data in the region of the fit. The

parameters α_1^π and β_1^π were obtained by solving the Altarelli-Parisi equations. Fits were performed with and without QCD m^2 evolution in the pion valence and nucleon structure functions. An overall normalization constant for the cross section, K , was also included in each fit. The results are shown in Table 1, where the errors indicated are statistical only.

We have examined possible sources of systematic error due to experimental uncertainties which affect the acceptance calculation. We assigned an error of 0.4 to K and 0.18 to β^π resulting from the uncertainties in the mean beam momentum, the magnetic field and the mean energy loss of muons in the toroids, the detector geometry, and the trigger efficiency. In addition, we considered the effect on the result of different parameterizations of the model. We estimated uncertainties in the K factor of 0.4 due to the nucleon structure functions, 0.2 due to the pion sea, and 0.5 due to normalization of the pion structure function. We estimated uncertainties in β^π of 0.02 due to the nucleon structure function and 0.14 due to the pion sea. The $V^\pi(x)$ we obtained is consistent with recent results obtained at CERN.^{7,3}

The data are not sensitive to QCD scaling violations in the mass region between the ψ and the T . We have therefore extended the test by comparing the data above the T with the extrapolated prediction of the Drell-Yan model. We have

used both our structure function and a world average given by $\alpha^\pi = .41$ and $\beta^\pi = .99$ at $m_{\mu\mu}^2 = 25(\text{GeV}/c^2)^2$. The two forms give virtually identical results. Figure 2 shows $d\sigma/dm_{\mu\mu}$ from the data along with the predictions of the model, with and without QCD leading log scaling violations. Our data favor the former, with the "naive" Drell-Yan model overestimating the cross section at high masses. The chisquare for $m_{\mu\mu} > 11 \text{ GeV}/c^2$ is 39/10 d.o.f. for the "naive" model and 6.3/10 d.o.f. for the model which includes scaling violations. This model also successfully predicts $d\sigma/dx_F$ for $m_{\mu\mu} > 11 \text{ GeV}/c^2$, as is shown in Fig. 3. We do not observe the "anomalous" scaling violations in $d\sigma/dx_F$ reported by NA10.³

We wish to thank the staff of the Proton Lab of Fermilab, members of the Elementary Particles Lab at Princeton University, and the electronic and engineering support groups of the Enrico Fermi Institute for much help in the design, building and operation of the experiment. We also thank N.D. Giokaris, J.M. Green, G. Hanson, R.M. Rohm, and C. Whitmer for help in various phases of the experiment. This experiment was supported by the Department of Energy and the National Science Foundation.

REFERENCES

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Figure Captions

Fig 1. Scatter plot of events in mass versus x_F . The binning used in the structure function analysis is superimposed.

Fig 2. The $d\sigma/dm_{\mu\mu}$ distribution. The solid line is the prediction of the Drell-Yan model, incorporating QCD leading log scaling violations in the structure functions and using our pion structure function. The dashed curve is the prediction of the "naive" Drell-Yan model.

Fig 3. The $d\sigma/dx_F$ distribution for $m_{\mu\mu} > 11 \text{ GeV}/c^2$. It is compared with the prediction of the Drell-Yan model including QCD leading log scaling violations.

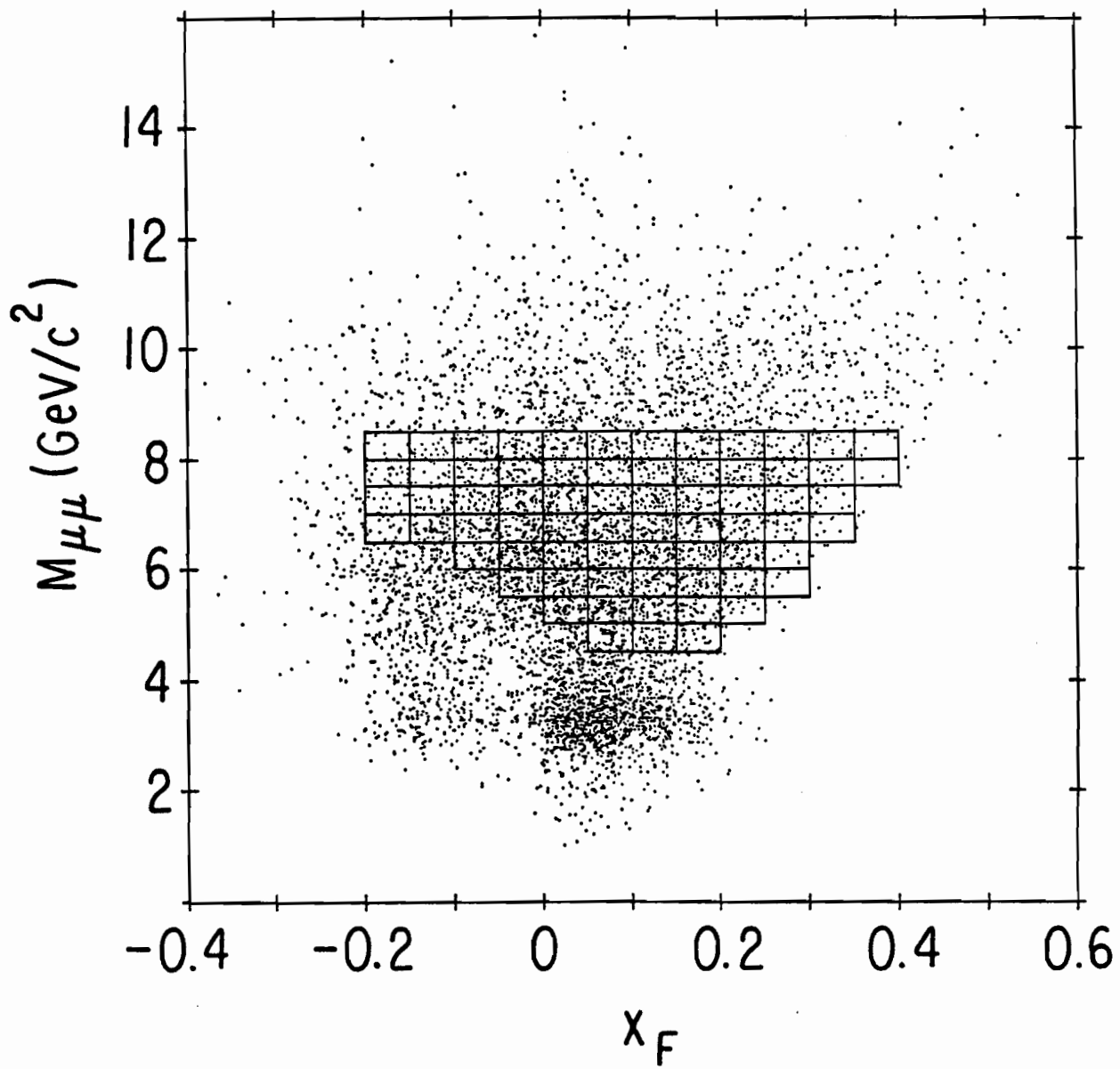


Fig. 1

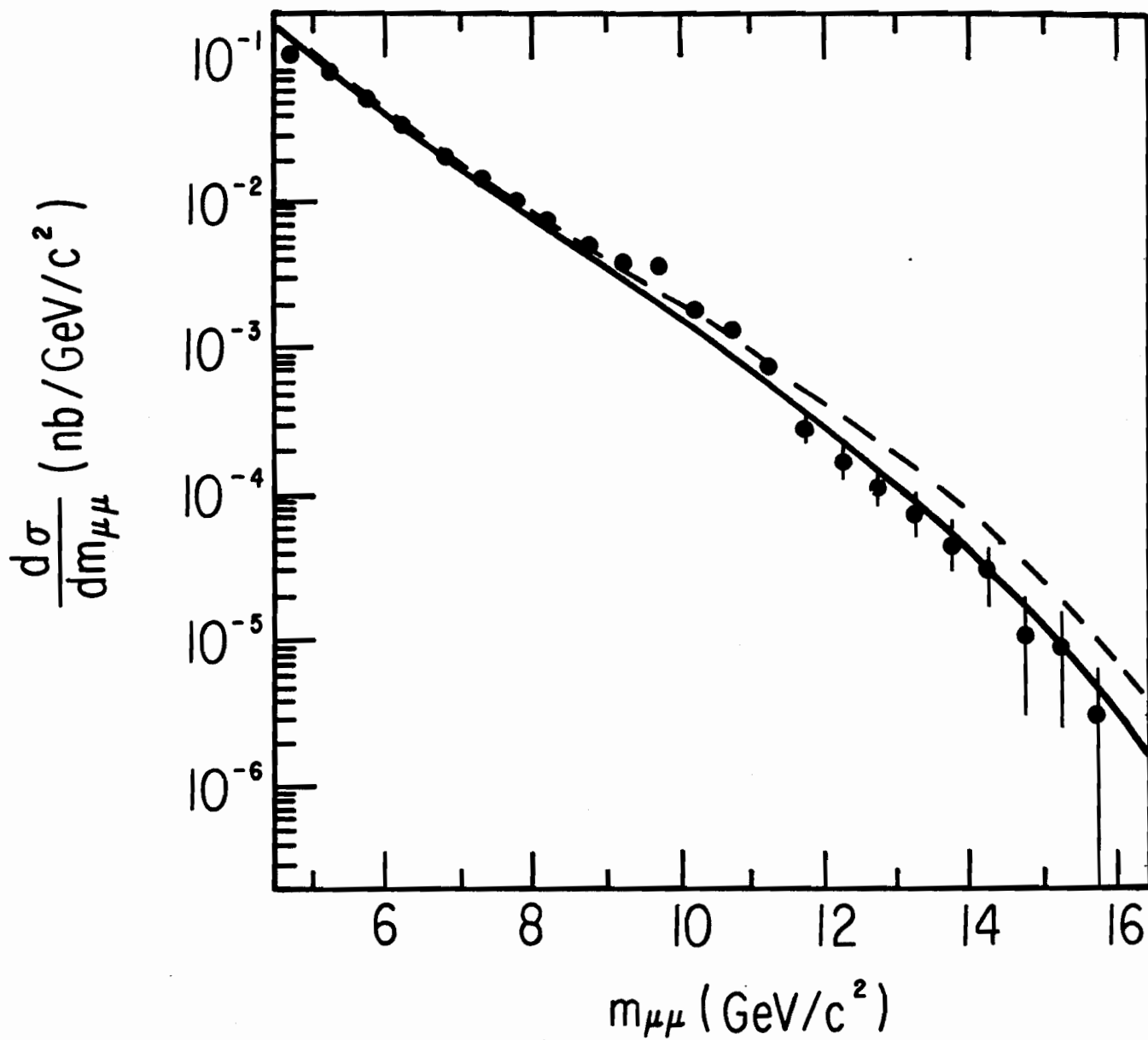


Fig. 2

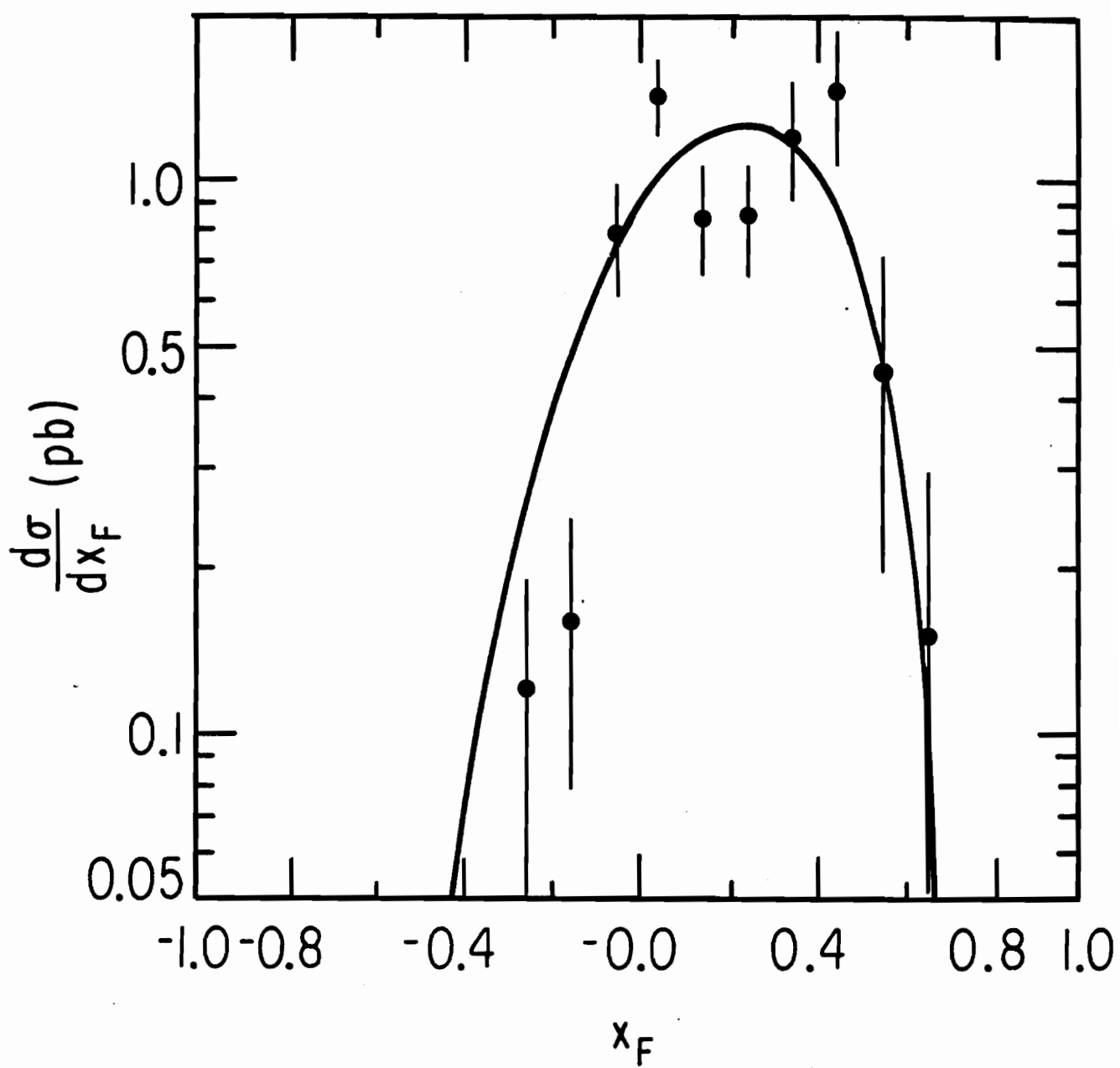


Fig. 3