



Féeton ($B - L$ gauge boson) dark matter testable in future direct detection experiments

Yu Cheng ^{d,a,b}, Jie Sheng ^{a,b} and Tsutomu T. Yanagida^{c,a,b}

^a*Tsung-Dao Lee Institute & School of Physics and Astronomy, Shanghai Jiao Tong University, Shanghai 200240, China*

^b*Key Laboratory for Particle Astrophysics and Cosmology (MOE) & Shanghai Key Laboratory for Particle Physics and Cosmology, Shanghai Jiao Tong University, Shanghai 200240, China*

^c*Kavli IPMU (WPI), UTIAS, University of Tokyo, Kashiwa, 277-8583, Japan*

^d*Department of Physics, KAIST, Daejeon, 34141, Korea*

E-mail: chengyu@sjtu.edu.cn, shengjie04@sjtu.edu.cn, tsutomu.tyanagida@sjtu.edu.cn

ABSTRACT: In this paper, we revisit the féeton (gauge boson of $U(1)_{B-L}$ symmetry) dark matter scenario, and first point out the $U(1)$ gauge symmetry can be a linear combination of the $B - L$ and the SM hypercharge gauge symmetries. With the redefinition of $B - L$ charge of fermions, the coupling between electron and féeton can be enhanced. After showing the parameter space required from the DM stability and cosmic production, we discuss the potential for verifying them in dark matter direct detection experiments. The results show that future experiments, such as SuperCDMS, have a sensitivity to reach the féeton DM region consistent with its cosmic production.

KEYWORDS: Models for Dark Matter, New Gauge Interactions, New Light Particles

ARXIV EPRINT: [2410.12554](https://arxiv.org/abs/2410.12554)

Contents

1	Introduction	1
2	Stability of the Féeton DM	1
3	Cosmic production of the Féeton DM	3
4	Direct detection of the Féeton DM	4
5	Conclusions and discussions	6

1 Introduction

Many astrophysical observations suggest that 80% of the matter in the universe is dark matter (DM) [1–3]. However, we still do not know what DM is. A widely accepted conjecture is that DM consists of new particles beyond the framework of the standard model (SM) [1–3]. To be well-motivated, models of DM are typically concise extensions of the SM and capable of addressing certain issues within the SM simultaneously. For example, WIMPs predicted from supersymmetry [4, 5], axions proposed to address the Strong CP problem [6–8]. Yet, positive results for the detection of these mainstream candidates are still pending [9–12], leading to other possibilities regarding DM.

The U(1) $B - L$ gauge theory is an attractive theory beyond the standard model. This gauge theory requires three right-handed neutrinos (RHNs) to cancel the gauge anomalies and its spontaneous breaking induces the super heavy Majorana masses for these RHNs [13]. These heavy Majorana RHNs are a key point for generating the observed tiny masses for the active neutrinos (via the seesaw mechanism) [14–17] and for the creation of the baryon-number asymmetry in our Universe (by the leptogenesis) [18, 19]. Furthermore, the $B - L$ gauge boson is an inevitable prediction in this framework, and we have stressed recently that it can be a good candidate for DM [20] called as the féeton DM [21, 22]. In this paper, we revisit the physics and parameter space of the féeton dark matter. For the first time, we point out that this U(1) symmetry can be a linear combination of the $B - L$ and the SM hypercharge gauge symmetries. With a redefinition of $B - L$ charge of fermions, we find some interesting parameter spaces that not only satisfy the stability and cosmological production requirements of DM but can also be tested in future direct detection experiments such as superCDMS.

2 Stability of the Féeton DM

The SM can be extended with a U(1) $_{B-L}$ gauge symmetry and its corresponding gauge boson A' . The related Lagrangian is,

$$\mathcal{L} = (D_\mu \Phi)^\dagger D^\mu \Phi - \frac{1}{4} F'^{\mu\nu} F'_{\mu\nu} - \lambda \left(|\Phi|^2 - \frac{V_{B-L}^2}{2} \right)^2 + g_{B-L} q_{B-L} \bar{f} \gamma^\mu f A'_\mu. \quad (2.1)$$

The covariant derivative D_μ is defined as $D_\mu \equiv \partial_\mu - i2g_{B-L}A'_\mu$ with the gauge coupling g_{B-L} , as the Higgs field Φ has a $B-L$ charge $q_{B-L} = 2$. The spontaneous symmetry breaking gives the Higgs field Φ a vacuum expectation value (vev) V_{B-L} , its mass $m_\phi = \sqrt{2\lambda}V_{B-L}$, and a gauge boson mass $m_{A'} = 2g_{B-L}V_{B-L}$. Any fermions f with a $B-L$ charge q_{B-L} can couple to the gauge boson A' with a universal coupling strength g_{B-L} . The fermions f include not only the SM quarks with $B-L$ charge $q_{B-L} = 1/3$ and leptons with $q_{B-L} = -1$, but also the heavy RHNs with $q_{B-L} = -1$ to cancel the gauge anomalies. Such a framework is self-consistent and well-motivated, as the three RHNs are important ingredients for generating the tiny neutrino masses via see-saw mechanism [13–17] and the baryon asymmetry in our Universe via leptogenesis [18, 19]. In order for the standard leptogenesis to work, the vacuum expectation value V_{B-L} should satisfy $V_{B-L} > 3 \times 10^9$ [18, 19, 23], which gives the upper bound for the coupling g_{B-L} shown as the dashed purple line in figure 1. This upper limit can be greatly relaxed if we consider some other leptogenesis scenarios, such as resonant leptogenesis [24, 25]. Furthermore, the gauge boson A' can be a natural candidate of DM in this minimal framework [20–22], called as féeton.

With the coupling to leptons, the féeton with a certain mass will decay. The decay rate is dominant by its decay channel to two active neutrinos as,

$$\Gamma_{A'} \simeq \frac{1}{8\pi} g_{B-L}^2 m_{A'}. \quad (2.2)$$

The required long lifetime for the féeton DM is guaranteed by the extremely small gauge coupling constant g_{B-L} . By conservatively assuming that the lifetime of féeton DM exceeds ten times of the age of the universe, $\tau_{A'} > 150$ Gyr, an upper bound on g_{B-L} can be derived, as shown by the black dashed line in figure 1. Consequently, the grey shaded region is excluded by the requirement of DM stability. Such a constraint on coupling is notably stringent, with $g_{B-L} \leq 10^{-16}$ even for light féeton with a mass $m_{A'} = 1$ eV.

Actually, this extra unknown U(1) gauge symmetry can be in principle a linear combination of the canonical U(1)_{B-L} symmetry and the SM U(1)_Y symmetry, as both them are anomaly-free. All the $B-L$ charges of fermions can be redefined as $q'_{B-L} \equiv q_{B-L} + \alpha Y$ with a rotation factor α [26, 27]. In such a case, the SM Higgs field is charged under this redefined U(1)'_{B-L} with $q'_{B-L} = \alpha/2$ and gives an additional contribution to féeton mass. As a result, we need to re-diagonalize the mass matrix of gauge bosons to obtain their new mass eigenstates and interacting currents. First, we write the mass terms of the gauge bosons on the basis of the U(1)_Y, the neutral component of SU(2)_L and the original U(1)_{B-L} as $V^T \equiv (B \ W^3 \ A')$,

$$\mathcal{L}_m = V^T \begin{pmatrix} \frac{1}{8}g'^2v^2 & -\frac{1}{8}gg'v^2 & \frac{1}{8}g'g_{B-L}v^2\alpha \\ -\frac{1}{8}gg'v^2 & \frac{1}{8}g^2v^2 & -\frac{1}{8}gg_{B-L}v^2\alpha \\ \frac{1}{8}g'g_{B-L}v^2\alpha & -\frac{1}{8}gg_{B-L}v^2\alpha & 2g_{B-L}^2v_{B-L}^2 + \frac{1}{8}g_{B-L}^2v^2\alpha^2 \end{pmatrix} V \quad (2.3)$$

with g (g') being the gauge couplings of the SM SU(2) (U(1)_Y). Then, we utilize the Weinberg angle, $S_w = g'/\sqrt{g^2 + g'^2}$ and $C_w = g/\sqrt{g^2 + g'^2}$, to first diagonalize the B and W^3 field into the photon field \tilde{A} and weak gauge boson \tilde{Z} as an intermediate step,

$$\begin{pmatrix} \tilde{A} \\ \tilde{Z} \\ \tilde{A}' \end{pmatrix} = \begin{pmatrix} C_w & S_w & 0 \\ -S_w & C_w & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} B \\ W^3 \\ A' \end{pmatrix}. \quad (2.4)$$

The mass terms in this intermediate basis $\tilde{V}^T \equiv (\tilde{A} \tilde{Z} \tilde{A}')$ becomes,

$$\mathcal{L}_m = \tilde{V}^T \begin{pmatrix} 0 & 0 & 0 \\ 0 & \frac{1}{8}(g^2 + g'^2)v^2 & -\frac{1}{8}\alpha g_{B-L}\sqrt{g^2 + g'^2}v^2 \\ 0 & -\frac{1}{8}\alpha g_{B-L}\sqrt{g^2 + g'^2}v^2 & 2g_{B-L}^2 v_{B-L}^2 + \frac{1}{8}g_{B-L}^2 v^2 \alpha^2 \end{pmatrix} \tilde{V}. \quad (2.5)$$

One can see that the SM photon remains massless as expected. After the diagonalization of the remaining mass matrix for the intermediate \tilde{Z} and \tilde{A}' , the mass eigenstates Z and A' are defined as,

$$\begin{pmatrix} Z \\ A' \end{pmatrix} \equiv \begin{pmatrix} \cos \xi & \sin \xi \\ -\sin \xi & \cos \xi \end{pmatrix} \begin{pmatrix} \tilde{Z} \\ \tilde{A}' \end{pmatrix} \quad (2.6)$$

with

$$\tan 2\xi = \frac{-\frac{1}{4}\alpha g_{B-L}\sqrt{g^2 + g'^2}v^2}{\frac{1}{8}(g^2 + g'^2)v^2 - 2g_{B-L}^2 v_{B-L}^2 - \frac{1}{8}g_{B-L}^2 v^2 \alpha^2} \sim \frac{-2\alpha g_{B-L}}{\sqrt{g^2 + g'^2}}. \quad (2.7)$$

With the above rotations, the interaction currents change as well. The interacting terms of fermions with gauge bosons are,

$$\mathcal{L}_I = J_{em}^\mu A_\mu + \left(\cos \xi J_{\tilde{Z}}^\mu + \sin \xi J_{\tilde{A}'}^\mu \right) Z_\mu + \left(-\sin \xi J_{\tilde{Z}}^\mu + \cos \xi J_{\tilde{A}'}^\mu \right) A'_\mu, \quad (2.8)$$

where $J_{\tilde{Z}}^\mu$ is the Z boson current in SM and $J_{\tilde{A}'}^\mu$ is the original féeton current before the redefinition. Firstly, one can observe that the neutrino-féeton coupling is independent of α ,

$$\mathcal{L}_\nu = \left[-\frac{g}{2C_w} \sin \xi + g_{B-L} \left(-1 - \frac{1}{2}\alpha \right) \cos \xi \right] \bar{\nu}_L \gamma^\mu \nu_L A'_\mu \approx -g_{B-L} \bar{\nu}_L \gamma^\mu \nu_L A'_\mu, \quad (2.9)$$

which means the decay width of féeton and the constraint from DM stability remain unchanged even after the charge redefinition. However, it is important to note that the coupling strength between electron and féeton is dependent of α as,

$$\begin{aligned} \mathcal{L}_e &= \left(g_{B-L} \cos \xi \left(-1 - \frac{1}{2}\alpha \right) - g \sin \xi \frac{-\frac{1}{2} + S_w^2}{C_w} \right) \bar{e}_L \gamma^\mu e_L X_\mu^m \\ &+ \left(g_{B-L} \cos \xi \left(-1 - \alpha \right) - g \sin \xi \frac{S_w^2}{C_w} \right) \bar{e}_R \gamma^\mu e_R X_\mu^m \\ &= \left(-1 - C_w^2 \alpha \right) g_{B-L} \bar{e} \gamma^\mu e A'_\mu. \end{aligned} \quad (2.10)$$

With a typical α , such as $\alpha = 2.6$, the $B - L$ charge of electron changes from -1 to -3 , leading to a enhancement of the féeton-electron interaction cross section by one order of magnitude. Due to this redefinition of the $B - L$ charge, the detection capability of this model will also be enhanced by the DM direct detection experiments, as we will discuss later.

3 Cosmic production of the Féeton DM

However, a crucial issue of the féeton DM is its cosmological production, as it is very difficult to produce the féeton in the early universe due to the small gauge coupling constant. Nevertheless, two natural mechanisms have been proposed for sufficient vector boson DM productions:

the decay of cosmic strings associated with $U(1)$ gauge symmetry breaking [28, 29], and the quantum fluctuations during the inflation [30]. We shall discuss their applications to the féeton DM production as follows.

The féeton DM, as the gauge boson of the $U(1)_{B-L}$ gauge symmetry, gains its mass from the Higgs mechanism. The dark Higgs field Φ obtains a vacuum expectation value V_{B-L} , and the $U(1)_{B-L}$ symmetry is spontaneously broken. Once the symmetry breaking happens after inflation, cosmic string networks appear [31] and their subsequent decay produce the féeton DM relic abundance Ω_f ,

$$\Omega_f \simeq 0.12 \left(\frac{\xi}{5.7} \right) \left(\frac{m_{A'}}{1 \text{ keV}} \right)^{1/2} \left(\frac{V_{B-L}}{1.6 \times 10^{10} \text{ GeV}} \right)^2, \quad (3.1)$$

can be consistent with the observed value. The average string number per Hubble volume ξ can be obtained from simulations [32, 33],

$$\xi = 0.15 \log \left(\frac{m_\Phi}{m_{A'}} \right) = 0.15 \log \left(\frac{\sqrt{2\lambda} V_{B-L}}{m_{A'}} \right) \quad (3.2)$$

The corresponding parameters that generate the correct relic density by taking $\lambda = 1/2$ are shown as the yellow solid line in figure 1. Note that there is an $\mathcal{O}(1)$ uncertainty in the relic density calculation, which arises from the uncertainties in the cosmic string simulation.¹ This means that the parameter space is actually a band centered around the yellow line with a width of one order.

The other possibility for the féeton DM production is the production of massive vector boson from the quantum fluctuations during inflation. The massive vector field is initially sub-horizon and evolves to become super-horizon modes during inflation. Subsequently, they re-enter the horizon during radiation domination to be cosmic relics. In such a scenario, the relic density of féeton is precisely determined by its mass and the Hubble scale of inflation H_I [30],

$$\Omega_{A'} = 0.3 \sqrt{\frac{m_{A'}}{1 \text{ keV}}} \left(\frac{H_I}{10^{12} \text{ GeV}} \right)^2. \quad (3.3)$$

It is required that the spontaneous breaking of $B-L$ gauge symmetry occurs before or during inflation, leading to $V_{B-L} > H_I$. Taking H_I as a lower bound for V_{B-L} , the above relic density formula has an same scaling of $m_{A'}$ and V_{B-L} as the cosmic string case eq. (3.2). As a result, the upper bound line for féeton coupling g_{B-L} as a function of $m_{A'}$ to generate the right relic density (red solid) is parallel to that of the cosmic string production but with around 2 orders smaller. The larger vev V_{B-L} , or equivalently, smaller coupling g_{B-L} area (red shaded region) can also generate the correct DM relic density.

4 Direct detection of the Féeton DM

Although the requirements for stability and relic density have predicted a very small féeton DM coupling, our scenario can still be tested by future direct detection experiments.

¹We would acknowledge the communication with N. Kitajima and K. Nakayama on this point.

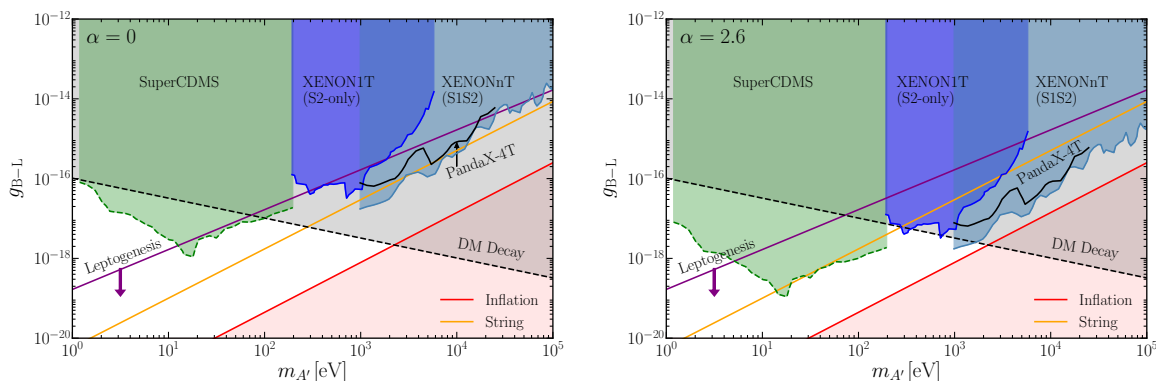


Figure 1. The parameter space of féeton DM for generating the correct relic density via inflation production (red shaded region) and cosmic string decay (orange solid line with one order of uncertainty). The gray shaded region is excluded since the corresponding lifetime of the féeton DM is shorter than ten times of the age of Universe, $\tau_f < 150$ Gyr, due to DM stability. The blue shaded regions are the current constraint from the XENON1T (S2-only) and XENONnT (S1S2) experiments [34–36] while the green region is the projected limit in future SuperCDMS experiments [37]. The black solid line is the constraint from PandaX-4T [38]. All these direct detection constraints are dependent of the charge redefinition parameter α . The left panel corresponds to the case of $\alpha = 0$ and the right panel the case of $\alpha = 2.6$.

The féeton DM can be absorbed by the electron targets in the DM direct detection experiments via the leading process $e + A' \rightarrow e + \gamma$ [39–47]. With the total DM mass transferred into the kinetic energy of the final states, such an absorption process allows a lower mass threshold for DM detection [47–49]. In the Xenon-based DM direct detection experiments, such as Xenon [34–36], PandaX [38, 50], and LZ [51, 52], the most outer layer electrons of Xenon atom has a binding energy of ~ 10 eV. Due to the energy conservation, the féeton DM with a mass larger than 10 eV is allowed to be absorbed and ionized the electrons. Therefore, these experiments place constraints on féeton coupling above the féeton mass $m_{A'} \sim 10$ eV, and become the strongest terrestrial experimental constraints beyond ~ 200 eV. The stringent constraint from XENON1T (S2 only) [34] and XENONnT (S1S2) experiments [36] are shown as the blue regions in the left panel of figure 1. The PandaX-4T experiment currently has a better S2-only sensitivity [53, 54]. Although the experimental testability has reached the Leptogenesis and string production lines, such a parameter space is already disfavored from the stability requirement for DM.

The next-generation SuperCDMS experiment, which will be developed in SNOLAB [37], is expected to have a lower detection threshold and better projected sensitivity in the low mass range. The detection threshold of a phonon detector is determined by the band gap of the materials it is composed of. For germanium (Ge), which is planned to be used in the SuperCDMS project, the threshold can be lowered to 0.67 eV. The projected sensitivity of the SuperCDMS experiment for the féeton absorption process is shown by the green region in the figure 1. It provides the strongest constraints on féeton coupling in the mass range from ~ 1 eV to ~ 200 eV. This projected constraint can reach the féeton DM region below the black dashed line, and surpass the upper limit of canonical leptogenesis as well in the féeton mass range $\sim (10, 100)$ eV.

All these direct detection constraints become stronger if the $U(1)_{B-L}$ symmetry contains a linear combination with the SM $U(1)_Y$ symmetry, where $\alpha \neq 0$. As previously stated, if $\alpha = 2.6$, the charge of the electron, or equivalently, its coupling with féeton, increases by three times. As a result, the cross section of féeton absorption increases by a factor of ~ 10 , thereby strengthening the constraints on the féeton model with this α by an order of magnitude in direct detection experiments. We show these enhanced limits in the right panel of figure 1. One can see the future SuperCDMS can test the féeton DM parameter space which is consistent with the cosmic string production in the mass range $m_{A'} \subset (10, 200)$ eV. The future Xenon-based detectors, with tenfold increased exposure and reduced backgrounds, can even get a better sensitivity [55, 56], having the possibility to test the inflation production of féeton DM with a mass around $m_{A'} \sim 10^3$ eV.

5 Conclusions and discussions

What is dark matter? This is one of the most important questions in modern physics. There is no universal method for the detection of DM; it must rely on the mass and interaction type of DM predicted by DM models. Therefore, clearly defined, theoretically well-motivated DM candidates are of great importance. Currently, our strategy is to search for DM candidates that can address issues in the SM. Among the most popular are WIMPs and the axion. WIMPs can be predicted by a broad range of new physics models. One well-motivated class is supersymmetry model, which was initially proposed to unify all interactions and can address the hierarchy problem in the SM [57–59]. However, so far, no supersymmetric particles have been discovered at colliders, and direct detection of DM has placed strong constraints on WIMPs. On the other hand, the proposal of the axion aimed to theoretically solve the strong CP problem, but it also suffers from more severe high-quality problem [60, 61]. And there are alternative solutions to the strong CP problem that do not require the introduction of the axion [62–68].

Compared to theoretical puzzles like the hierarchy problem and the strong CP problem, phenomena beyond the SM such as neutrino masses and baryon asymmetry pose more concrete phenomenological questions. Within the framework of the seesaw mechanism, which introduces three heavy Majorana RHNs, both of these issues can be effectively addressed. Moreover, this framework can also motivate the existence of a new $B-L$ $U(1)$ gauge symmetry, incorporating the corresponding gauge boson A' . As long as the gauge coupling is sufficiently small to ensure the stability of A' , it can naturally become DM. We call it féeton DM. This DM candidate predicted from the simple and elegant extension of SM deserves more attention.

In this paper, we revisit the physics of féeton DM, and show the viable parameter space required from the stability of DM. After that, we review the cosmic production of féeton DM via cosmic string decay and inflation. In this canonical féeton DM model, the most parameter space the DM direct detection can constrain is already excluded due to the DM decay. The future SuperCDMS, however, can reach the féeton DM region, which is consistent with the canonical leptogenesis with $V_{B-L} > 3 \times 10^9$ GeV. More importantly, we first point out the freedom of the definition of $B-L$ charge, $q'_{B-L} \rightarrow q_{B-L} + \alpha Y$, since this $U(1)$ gauge symmetry can be a linear combination of the $B-L$ and the SM hypercharge gauge symmetries. With this redefinition, the coupling between electron and féeton can be

enhanced, leading to a stronger limit from DM direct detection. In the case of $\alpha = 2.6$, as the example in our paper, all the direct detection constrained is enhanced by one order of magnitude. In such a scenario, the future SuperCDMS will have the capability to test the cosmic string production of féeton DM in the mass range $m_{A'} \in (10, 200)$ eV while the future Xenon-based detectors, such as the Xenon-nT, PandaX, and LZ, have a chance to test the inflation production of féeton DM with a mass $m_{A'} \sim 1$ keV.

For the féeton DM lighter than 1 eV, there are also some experimental proposals, such as the Josephson junction current [69, 70] and molecule excitations [71], to detect them. However, the predicted coupling from DM production is too small to be reached. In even lighter mass ranges, like $m_{A'} < 10^{-5}$ eV, fifth force experiments have imposed very strong constraints [72–76].

Finally, we should comment on the serious difference between the féeton DM model and the dark photon DM model. The dark photon DM couples to the electron only through the kinetic mixing term between the dark photon and the SM photon [77]. Thus, we do not have any prediction for the detection experiments as its kinetic mixing ϵ is a free parameter, which is independent from the DM mass and the vacuum expectation value of the dark gauge symmetry breaking scale. It is crucial the féeton mass is given by $m_{A'} = 2g_{B-L}V_{B-L}$. This is the reason why we have a certain prediction for the detection of the féeton DM in the future direct detection experiments.

Acknowledgments

We thank N. Kitajima and K. Nakayama for discussion on the féeton production from cosmic string decays. We also thank Jianglai Liu for useful discussion on the féeton direct detection. J. S. is supported by the National Natural Science Foundation of China (Nos. 12375101, 12425506, 12090060, 12090064) and the SJTU Double First Class start-up fund WF220442604. T. T. Y. was supported also by the Natural Science Foundation of China (NSFC) under Grant No. 12175134, MEXT KAKENHI Grants No. 24H02244, and World Premier International Research Center Initiative (WPI Initiative), MEXT, Japan.

Data Availability Statement. This article has no associated data or the data will not be deposited.

Code Availability Statement. This article has no associated code or the code will not be deposited.

Open Access. This article is distributed under the terms of the Creative Commons Attribution License ([CC-BY4.0](https://creativecommons.org/licenses/by/4.0/)), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

References

- [1] B.-L. Young, *A survey of dark matter and related topics in cosmology*, *Front. Phys. (Beijing)* **12** (2017) 121201 [*Erratum ibid.* **12** (2017) 121202] [INSPIRE].
- [2] A. Arbey and F. Mahmoudi, *Dark matter and the early Universe: a review*, *Prog. Part. Nucl. Phys.* **119** (2021) 103865 [arXiv:2104.11488] [INSPIRE].
- [3] M. Cirelli, A. Strumia and J. Zupan, *Dark Matter*, arXiv:2406.01705 [INSPIRE].
- [4] G. Jungman, M. Kamionkowski and K. Griest, *Supersymmetric dark matter*, *Phys. Rept.* **267** (1996) 195 [hep-ph/9506380] [INSPIRE].
- [5] L. Roszkowski, E.M. Sessolo and S. Trojanowski, *WIMP dark matter candidates and searches — current status and future prospects*, *Rept. Prog. Phys.* **81** (2018) 066201 [arXiv:1707.06277] [INSPIRE].
- [6] R.D. Peccei and H.R. Quinn, *CP Conservation in the Presence of Instantons*, *Phys. Rev. Lett.* **38** (1977) 1440 [INSPIRE].
- [7] S. Weinberg, *A New Light Boson?*, *Phys. Rev. Lett.* **40** (1978) 223 [INSPIRE].
- [8] F. Wilczek, *Problem of Strong P and T Invariance in the Presence of Instantons*, *Phys. Rev. Lett.* **40** (1978) 279 [INSPIRE].
- [9] ADMX collaboration, *Axion Dark Matter Experiment: detailed design and operations*, *Rev. Sci. Instrum.* **92** (2021) 124502 [arXiv:2010.00169] [INSPIRE].
- [10] PANDAX-4T collaboration, *Dark Matter Search Results from the PandaX-4T Commissioning Run*, *Phys. Rev. Lett.* **127** (2021) 261802 [arXiv:2107.13438] [INSPIRE].
- [11] LZ collaboration, *First Dark Matter Search Results from the LUX-ZEPLIN (LZ) Experiment*, *Phys. Rev. Lett.* **131** (2023) 041002 [arXiv:2207.03764] [INSPIRE].
- [12] XENON collaboration, *First Dark Matter Search with Nuclear Recoils from the XENONnT Experiment*, *Phys. Rev. Lett.* **131** (2023) 041003 [arXiv:2303.14729] [INSPIRE].
- [13] F. Wilczek, *Unification of Fundamental Forces*, in proceedings of *Lepton-Photon Conference*, Fermi National Accelerator Laboratory, Batavia, Illinois, 23–29 August (1979), *eConf C* **790823** (1979) 437, <https://lss.fnal.gov/conf/C790823/openingpages.pdf> [INSPIRE].
- [14] P. Minkowski, *$\mu \rightarrow e\gamma$ at a Rate of One Out of 10^9 Muon Decays?*, *Phys. Lett. B* **67** (1977) 421 [INSPIRE].
- [15] T. Yanagida, *Horizontal gauge symmetry and masses of neutrinos*, in the proceedings of the *Workshop on the Unified Theories and the Baryon Number in the Universe*, *Conf. Proc. C* **7902131** (1979) 95 [INSPIRE].
- [16] T. Yanagida, *Horizontal Symmetry and Mass of the Top Quark*, *Phys. Rev. D* **20** (1979) 2986 [INSPIRE].
- [17] M. Gell-Mann, P. Ramond and R. Slansky, *Complex Spinors and Unified Theories*, *Conf. Proc. C* **790927** (1979) 315 [arXiv:1306.4669] [INSPIRE].
- [18] M. Fukugita and T. Yanagida, *Baryogenesis Without Grand Unification*, *Phys. Lett. B* **174** (1986) 45 [INSPIRE].
- [19] W. Buchmuller, R.D. Peccei and T. Yanagida, *Leptogenesis as the origin of matter*, *Ann. Rev. Nucl. Part. Sci.* **55** (2005) 311 [hep-ph/0502169] [INSPIRE].

- [20] G. Choi, T.T. Yanagida and N. Yokozaki, *Feebly interacting $U(1)_{B-L}$ gauge boson warm dark matter and XENON1T anomaly*, *Phys. Lett. B* **810** (2020) 135836 [[arXiv:2007.04278](#)] [[INSPIRE](#)].
- [21] W. Lin, L. Visinelli, D. Xu and T.T. Yanagida, *Neutrino astronomy as a probe of physics beyond the Standard Model: decay of sub-MeV $B-L$ gauge boson dark matter*, *Phys. Rev. D* **106** (2022) 075011 [[arXiv:2202.04496](#)] [[INSPIRE](#)].
- [22] J. Sheng, Y. Cheng, W. Lin and T.T. Yanagida, *Féeton ($B-L$ gauge boson) dark matter for the 511-keV gamma-ray excess and the prediction of low-energy neutrino flux*, *Chin. Phys. C* **48** (2024) 083104 [[arXiv:2310.05420](#)] [[INSPIRE](#)].
- [23] S. Davidson, E. Nardi and Y. Nir, *Leptogenesis*, *Phys. Rept.* **466** (2008) 105 [[arXiv:0802.2962](#)] [[INSPIRE](#)].
- [24] A. Pilaftsis and T.E.J. Underwood, *Resonant leptogenesis*, *Nucl. Phys. B* **692** (2004) 303 [[hep-ph/0309342](#)] [[INSPIRE](#)].
- [25] A. Pilaftsis and T.E.J. Underwood, *Electroweak-scale resonant leptogenesis*, *Phys. Rev. D* **72** (2005) 113001 [[hep-ph/0506107](#)] [[INSPIRE](#)].
- [26] H.-S. Lee and S. Yun, *Mini force: the $(B - L) + xY$ gauge interaction with a light mediator*, *Phys. Rev. D* **93** (2016) 115028 [[arXiv:1604.01213](#)] [[INSPIRE](#)].
- [27] T. Hayashi, S. Matsumoto, Y. Watanabe and T.T. Yanagida, *Féeton dark matter above the e^-e^+ threshold*, [arXiv:2408.12155](#) [[INSPIRE](#)].
- [28] A.J. Long and L.-T. Wang, *Dark Photon Dark Matter from a Network of Cosmic Strings*, *Phys. Rev. D* **99** (2019) 063529 [[arXiv:1901.03312](#)] [[INSPIRE](#)].
- [29] N. Kitajima and K. Nakayama, *Dark photon dark matter from cosmic strings and gravitational wave background*, *JHEP* **08** (2023) 068 [[arXiv:2212.13573](#)] [[INSPIRE](#)].
- [30] P.W. Graham, J. Mardon and S. Rajendran, *Vector Dark Matter from Inflationary Fluctuations*, *Phys. Rev. D* **93** (2016) 103520 [[arXiv:1504.02102](#)] [[INSPIRE](#)].
- [31] N. Kitajima and K. Nakayama, *Nanohertz gravitational waves from cosmic strings and dark photon dark matter*, *Phys. Lett. B* **846** (2023) 138213 [[arXiv:2306.17390](#)] [[INSPIRE](#)].
- [32] M. Gorghetto, E. Hardy and G. Villadoro, *Axions from Strings: the Attractive Solution*, *JHEP* **07** (2018) 151 [[arXiv:1806.04677](#)] [[INSPIRE](#)].
- [33] M. Gorghetto, E. Hardy and G. Villadoro, *More axions from strings*, *SciPost Phys.* **10** (2021) 050 [[arXiv:2007.04990](#)] [[INSPIRE](#)].
- [34] XENON collaboration, *Light Dark Matter Search with Ionization Signals in XENON1T*, *Phys. Rev. Lett.* **123** (2019) 251801 [[arXiv:1907.11485](#)] [[INSPIRE](#)].
- [35] XENON collaboration, *Excess electronic recoil events in XENON1T*, *Phys. Rev. D* **102** (2020) 072004 [[arXiv:2006.09721](#)] [[INSPIRE](#)].
- [36] XENON collaboration, *Search for New Physics in Electronic Recoil Data from XENONnT*, *Phys. Rev. Lett.* **129** (2022) 161805 [[arXiv:2207.11330](#)] [[INSPIRE](#)].
- [37] SUPERCDMS collaboration, *A Strategy for Low-Mass Dark Matter Searches with Cryogenic Detectors in the SuperCDMS SNOLAB Facility*, in the proceedings of the *Snowmass 2021*, Seattle, U.S.A., July 17–26 (2022) [[arXiv:2203.08463](#)] [[INSPIRE](#)].
- [38] PANDAX collaboration, *Exploring New Physics with PandaX-4T Low Energy Electronic Recoil Data*, [arXiv:2408.07641](#) [[INSPIRE](#)].

- [39] M. Pospelov, A. Ritz and M.B. Voloshin, *Bosonic super-WIMPs as keV-scale dark matter*, *Phys. Rev. D* **78** (2008) 115012 [[arXiv:0807.3279](#)] [[INSPIRE](#)].
- [40] H. An, M. Pospelov and J. Pradler, *Dark Matter Detectors as Dark Photon Helioscopes*, *Phys. Rev. Lett.* **111** (2013) 041302 [[arXiv:1304.3461](#)] [[INSPIRE](#)].
- [41] H. An, M. Pospelov, J. Pradler and A. Ritz, *Direct Detection Constraints on Dark Photon Dark Matter*, *Phys. Lett. B* **747** (2015) 331 [[arXiv:1412.8378](#)] [[INSPIRE](#)].
- [42] Y. Hochberg, T. Lin and K.M. Zurek, *Detecting Ultralight Bosonic Dark Matter via Absorption in Superconductors*, *Phys. Rev. D* **94** (2016) 015019 [[arXiv:1604.06800](#)] [[INSPIRE](#)].
- [43] I.M. Bloch et al., *Searching for Dark Absorption with Direct Detection Experiments*, *JHEP* **06** (2017) 087 [[arXiv:1608.02123](#)] [[INSPIRE](#)].
- [44] Y. Hochberg, T. Lin and K.M. Zurek, *Absorption of light dark matter in semiconductors*, *Phys. Rev. D* **95** (2017) 023013 [[arXiv:1608.01994](#)] [[INSPIRE](#)].
- [45] H. An, M. Pospelov, J. Pradler and A. Ritz, *New limits on dark photons from solar emission and keV scale dark matter*, *Phys. Rev. D* **102** (2020) 115022 [[arXiv:2006.13929](#)] [[INSPIRE](#)].
- [46] A. Caputo, A.J. Millar, C.A.J. O'Hare and E. Vitagliano, *Dark photon limits: a handbook*, *Phys. Rev. D* **104** (2021) 095029 [[arXiv:2105.04565](#)] [[INSPIRE](#)].
- [47] S.-F. Ge, X.-G. He, X.-D. Ma and J. Sheng, *Revisiting the fermionic dark matter absorption on electron target*, *JHEP* **05** (2022) 191 [[arXiv:2201.11497](#)] [[INSPIRE](#)].
- [48] J.A. Dror, G. Elor, R. McGehee and T.-T. Yu, *Absorption of sub-MeV fermionic dark matter by electron targets*, *Phys. Rev. D* **103** (2021) 035001 [*Erratum ibid.* **105** (2022) 119903] [[arXiv:2011.01940](#)] [[INSPIRE](#)].
- [49] PANDAX collaboration, *Search for Light Fermionic Dark Matter Absorption on Electrons in PandaX-4T*, *Phys. Rev. Lett.* **129** (2022) 161804 [[arXiv:2206.02339](#)] [[INSPIRE](#)].
- [50] PANDAX collaboration, *Searching for MeV-scale Axion-like Particles and Dark Photons with PandaX-4T*, [arXiv:2409.00773](#) [[INSPIRE](#)].
- [51] LZ collaboration, *Projected sensitivities of the LUX-ZEPLIN experiment to new physics via low-energy electron recoils*, *Phys. Rev. D* **104** (2021) 092009 [[arXiv:2102.11740](#)] [[INSPIRE](#)].
- [52] LZ collaboration, *Search for new physics in low-energy electron recoils from the first LZ exposure*, *Phys. Rev. D* **108** (2023) 072006 [[arXiv:2307.15753](#)] [[INSPIRE](#)].
- [53] PANDAX collaboration, *Search for Light Dark Matter with Ionization Signals in the PandaX-4T Experiment*, *Phys. Rev. Lett.* **130** (2023) 261001 [[arXiv:2212.10067](#)] [[INSPIRE](#)].
- [54] PANDAX collaboration, *First Indication of Solar B8 Neutrinos through Coherent Elastic Neutrino-Nucleus Scattering in PandaX-4T*, *Phys. Rev. Lett.* **133** (2024) 191001 [[arXiv:2407.10892](#)] [[INSPIRE](#)].
- [55] X. Wang et al., *Design, construction and commissioning of the PandaX-30T liquid xenon management system*, *2023 JINST* **18** P05028 [[arXiv:2301.06044](#)] [[INSPIRE](#)].
- [56] XLZD collaboration, *The XLZD Design Book: Towards the Next-Generation Liquid Xenon Observatory for Dark Matter and Neutrino Physics*, [arXiv:2410.17137](#) [[INSPIRE](#)].
- [57] S. Dimopoulos and S. Raby, *Supercolor*, *Nucl. Phys. B* **192** (1981) 353 [[INSPIRE](#)].
- [58] S. Dimopoulos and H. Georgi, *Softly Broken Supersymmetry and SU(5)*, *Nucl. Phys. B* **193** (1981) 150 [[INSPIRE](#)].

- [59] S.P. Martin, *A Supersymmetry primer*, *Adv. Ser. Direct. High Energy Phys.* **18** (1998) 1 [[hep-ph/9709356](#)] [[INSPIRE](#)].
- [60] M. Kamionkowski and J. March-Russell, *Planck scale physics and the Peccei-Quinn mechanism*, *Phys. Lett. B* **282** (1992) 137 [[hep-th/9202003](#)] [[INSPIRE](#)].
- [61] R. Holman et al., *Solutions to the strong CP problem in a world with gravity*, *Phys. Lett. B* **282** (1992) 132 [[hep-ph/9203206](#)] [[INSPIRE](#)].
- [62] A.E. Nelson, *Naturally Weak CP Violation*, *Phys. Lett. B* **136** (1984) 387 [[INSPIRE](#)].
- [63] S.M. Barr, *Solving the Strong CP Problem Without the Peccei-Quinn Symmetry*, *Phys. Rev. Lett.* **53** (1984) 329 [[INSPIRE](#)].
- [64] A.E. Nelson, *Calculation of θ Barr*, *Phys. Lett. B* **143** (1984) 165 [[INSPIRE](#)].
- [65] G. Choi and T.T. Yanagida, *Solving the strong CP problem with horizontal gauge symmetry*, *Phys. Rev. D* **100** (2019) 095023 [[arXiv:1909.04317](#)] [[INSPIRE](#)].
- [66] F. Feruglio, A. Strumia and A. Titov, *Modular invariance and the QCD angle*, *JHEP* **07** (2023) 027 [[arXiv:2305.08908](#)] [[INSPIRE](#)].
- [67] F. Feruglio, M. Parriciatu, A. Strumia and A. Titov, *Solving the strong CP problem without axions*, *JHEP* **08** (2024) 214 [[arXiv:2406.01689](#)] [[INSPIRE](#)].
- [68] Q. Liang, R. Okabe and T.T. Yanagida, *Three-zero texture of quark-mass matrices as a solution to the strong CP problem*, *Phys. Lett. B* **859** (2024) 139123 [[arXiv:2408.12146](#)] [[INSPIRE](#)].
- [69] Y. Cheng, J. Sheng and T.T. Yanagida, *Detecting a fifth-force gauge boson via superconducting Josephson junctions*, *Phys. Lett. B* **860** (2025) 139156 [[arXiv:2402.14514](#)] [[INSPIRE](#)].
- [70] Y. Cheng, J. Lin, J. Sheng and T.T. Yanagida, *Proposal for a Quantum Mechanical Test of Gravity at Millimeter Scale*, [arXiv:2405.16222](#) [[INSPIRE](#)].
- [71] A. Arvanitaki, S. Dimopoulos and K. Van Tilburg, *Resonant absorption of bosonic dark matter in molecules*, *Phys. Rev. X* **8** (2018) 041001 [[arXiv:1709.05354](#)] [[INSPIRE](#)].
- [72] E.G. Adelberger et al., *Torsion balance experiments: a low-energy frontier of particle physics*, *Prog. Part. Nucl. Phys.* **62** (2009) 102 [[INSPIRE](#)].
- [73] T.A. Wagner, S. Schlamminger, J.H. Gundlach and E.G. Adelberger, *Torsion-balance tests of the weak equivalence principle*, *Class. Quant. Grav.* **29** (2012) 184002 [[arXiv:1207.2442](#)] [[INSPIRE](#)].
- [74] LIGO SCIENTIFIC et al. collaborations, *Constraints on dark photon dark matter using data from LIGO's and Virgo's third observing run*, *Phys. Rev. D* **105** (2022) 063030 [Erratum *ibid.* **109** (2024) 089902] [[arXiv:2105.13085](#)] [[INSPIRE](#)].
- [75] A.L. Miller and L. Mendes, *First search for ultralight dark matter with a space-based gravitational-wave antenna: LISA Pathfinder*, *Phys. Rev. D* **107** (2023) 063015 [[arXiv:2301.08736](#)] [[INSPIRE](#)].
- [76] J. Frerick, J. Jaeckel, F. Kahlhoefer and K. Schmidt-Hoberg, *Riding the dark matter wave: novel limits on general dark photons from LISA Pathfinder*, *Phys. Lett. B* **848** (2024) 138328 [[arXiv:2310.06017](#)] [[INSPIRE](#)].
- [77] M. Fabbrichesi, E. Gabrielli and G. Lanfranchi, *The Dark Photon*, [arXiv:2005.01515](#) [[DOI:10.1007/978-3-030-62519-1](#)] [[INSPIRE](#)].