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Emily Frame ^{1,*}, Afnan Al Marzouk ¹ , Oksana Chubenko ¹ , Scott Doran ², Philippe Piot ^{1,2} , John Power ² and Eric Wisniewski ²

¹ Northern Illinois Center for Accelerator & Detector Development and Department of Physics, Northern Illinois University, DeKalb, IL 60115, USA; aalmarzouk1@niu.edu (A.A.M.); chubenko@niu.edu (O.C.); ppiot@niu.edu (P.P.)

² Argonne National Laboratory, Lemont, IL 60439, USA; sdoran@anl.gov (S.D.); jp@anl.gov (J.P.); ewisniew@anl.gov (E.W.)

* Correspondence: eframe@anl.gov

Abstract: Bright electron beams have played a critical role in many recent advances in accelerator technology. Producing bright beams via photo-emission is ultimately limited by the mean transverse energy (MTE), which is determined by the photocathode. This paper discusses the opportunity to generate bright electron beams using an upgraded version of the Argonne Wakefield Accelerator (AWA) photo-injector. The focus of this study is to examine the optimal configurations of the AWA photo-injector to produce 100 pC with a ~ 100 nm transverse emittance (corresponding to a 5D brightness $\mathcal{B}_5 \geq 10^{15} \text{ A} \cdot \text{m}^{-2}$). The numerical optimization of the AWA photo-injector operating point, including realistic electromagnetic field maps, is presented for the different types of photocathodes under consideration.

Keywords: electron source; photo-emission; bright electron beams



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1. Introduction

High-quality, high-brightness electron beams have played an important role in many recent developments in accelerator technology, including free electron lasers (FELs) and ultrafast electron diffraction (UED) or microscopy (UEM) applications. The beam brightness is $\mathcal{B}_6 = Q/\varepsilon_6$, where Q is the beam charge, and ε_6 is the emittance for the combined three degrees of freedom (DOF), which, for uncoupled motion, can be written as the product of emittances associated with one DOF as $\varepsilon_6 = \varepsilon_x \varepsilon_y \varepsilon_z$ with $\varepsilon_i \equiv 1/(mc) \times [\langle i^2 \rangle \langle p_i^2 \rangle - \langle ip_i \rangle^2]^{1/2}$ for $i \in [x, y, z]$, with p_i being the momentum conjugated to position i . The quantities m and c are the electron mass and the speed of light, respectively.

Often, one can consider a reduced brightness in 5D (ignoring the impact of energy spread), defined as $\mathcal{B}_5 \equiv \hat{I}/(\varepsilon_x \varepsilon_y)$, where \hat{I} is the peak current associated with the bunch. In practice, assuming a cylindrical-symmetric bunch, the smallest achievable emittance is set by the thermal emittance, which is limited by the cathode mean transverse energy (MTE) following $\varepsilon_{\perp,c} \equiv \varepsilon_x = \varepsilon_y = \sigma_{\perp,c} \sqrt{\text{MTE}/(mc^2)}$. Consequently, the 5D brightness is ultimately limited by

$$\mathcal{B}_5 \equiv \frac{\hat{I}}{\varepsilon_{\perp,c}^2} \leq \frac{\hat{I}}{\varepsilon_{\perp,c}^2} = \frac{mc^2 \hat{I}}{\sigma_{\perp,c}^2 \text{MTE}}, \quad (1)$$

where $\sigma_{\perp,c}$ is the laser's rms transverse size on the photocathode surface, \hat{I} is the peak current, and $\varepsilon_{\perp} \geq \varepsilon_{\perp,c}$ is the transverse emittance. In practice, the equality in Equation (1) is never achieved for electron bunches as collective effects (e.g., space-charged and image-charged effects during the emission and low-energy transport) along with beamline imperfection (aberrations and misalignments), which yields final emittances larger than the intrinsic emittances set by the MTE.

In this paper, we explore the formation of a 100 pC electron bunch using the Argonne Wakefield Accelerator (AWA) photo-injector [1]. The focus is to understand the compromise between the final electron bunch duration σ_t and transverse emittance ε_{\perp} , considering the impact of the MTE associated with several photocathodes under consideration. These optimizations were performed using an upgraded version of the AWA photo-injector, which is planned for operation within the next couple of years.

2. The AWA Upgraded Photoinjector

The AWA drive beam accelerator consists of a 1.3 GHz, $1 + \frac{1}{2}$ cell radiofrequency (RF) gun with a Cs₂Te photocathode mounted on its backplate. The photo-emission is triggered by a 292 nm ultraviolet laser pulse with a radially uniform distribution and a nominal temporal shape, with a ~ 400 fs (RMS) Gaussian distribution. An optical pulse stacker allows for the stacking of 32 laser pulses to form a 6 ps duration flat-top pulse. The RF gun is followed by a linear accelerator comprised of six accelerating cavities, boosting the beam energy to ~ 70 MeV; see the diagram in Figure 1. The accelerator can accommodate a wide range of bunch charges: $Q \in [0.1, 100]$ nC. High-charge bunches are usually employed to explore two-beam acceleration concepts and test high-gradient accelerating structures, whereas lower-charge bunches are used in beam dynamics experiments related to, e.g., beam shaping or emittance control. Most recently, there has been interest in exploring the possible use of the AWA facility to support the generation of low-charge (100 pC) bright bunches with transverse emittance $\varepsilon_{\perp} \sim 100$ nm. In the process, the beamline will be upgraded with a new RF gun (with a symmetrized RF field to mitigate head-tail emittance growth due to a time-dependent transverse dipole-like field). Likewise, the linac cavities C1 and C2 will be upgraded with symmetrized cavities designed for the APEX project [2]. It is anticipated that such an upgraded beamline will support the generation of low-emittance bunches, possibly leveraging low-MTE photocathodes under development [3].

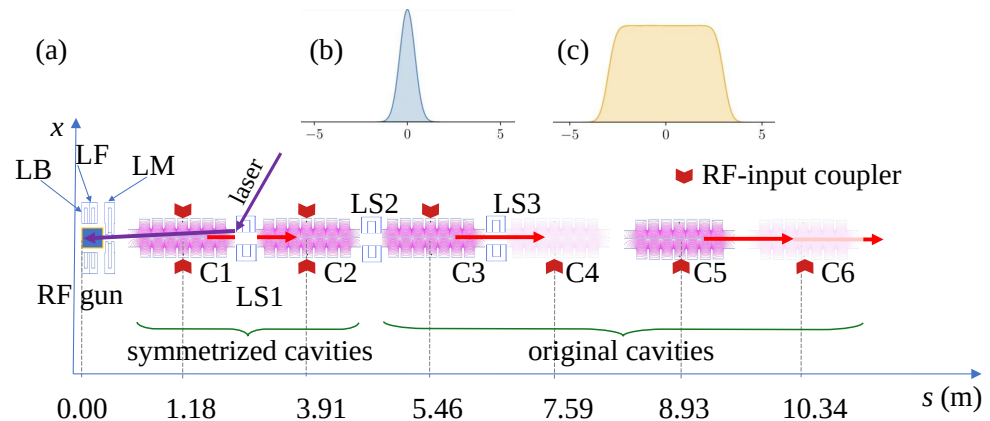


Figure 1. Diagram of the AWA photo-injector (a) and available Gaussian (b) and flat-top (c) temporal laser pulse distributions (the horizontal scale is in ps). In (a), the labels LB, LF, LM, and LS i represent solenoids, and C i represents the accelerating cavities. The red chevron symbols indicate the direction of the RF input couplers.

3. Beam Brightness Optimization

3.1. Methods

Throughout this paper, we investigate the lowest attainable emittance for a bunch charge of 100 pC using the beamline recently designed to improve the transport of a high bunch charge ($Q \geq 1$ nC) [4]. The operating points of this beamline were optimized using the DEAP [5] multi-objective optimization framework interfaced with the ASTRA beam dynamics program [6]. The DEAP framework can simultaneously optimize multiple objective functions when given a set of control parameters using a nondominated sorting technique. Nondominated points are solutions where further improvement in one objective

function degrades another objective function [7]. The tradeoff between the objective functions is referred to as a Pareto front. In our investigation, the objective functions are the transverse emittance ε_{\perp} and bunch duration σ_t . The set of control parameters is summarized in Table 1, along with their allowable range.

For this set of optimizations, the beamline model implemented in ASTRA considers cylindrical-symmetric external fields for the solenoid lenses and accelerating cavities. Such an approximation allows for the field to be described solely by its on-axis longitudinal component, e.g., $E_z(z, r = 0)$ for a TM_{010} cavity. The transverse fields are computed within ASTRA using the paraxial approximation up to the third order in the radial displacement r .

Table 1. Parameters considered during the optimization with their range of values.

Parameter	Range
Laser rms spot size	0.02–5 mm
Laser launch phase	−40–40°
Peak field on photocathode	40–80 MV/m
Linac C1 and C2 phase	−50–50°
Linac C1 and C2 amplitude	10–20 MV/m
Solenoid LB peak magnetic field	0–0.4 T
Solenoid LF peak magnetic field	−0.4–0 T
Solenoid LM peak magnetic field	−0.4–0 T
Solenoid LS1 peak magnetic field	0–0.5 T

Additionally, the ASTRA simulations were performed with $Q = 100$ pC for only four out of the six accelerating cavities turned on to reflect one of the nominal operation modes of AWA, resulting in a final energy of ~ 40 MeV.

In order to quantify how the final beam parameters are impacted by different types of photocathodes, the optimizations were performed for three values of the MTEs: (i) 250 meV, corresponding to a Cs_2Te photocathode, which is currently used at AWA, (ii) 60 meV, which is expected from Cs_3Sb photocathodes [3], and (iii) 5 meV, corresponding to the case of an atomically flat copper crystal [8]. It should be stressed that the latter value was selected as an idealized limit as its implementation requires cryogenic cooling, which would not be possible at AWA.

3.2. Results

The Pareto fronts for rms normalized transverse emittance, ε_{\perp} , and bunch duration, σ_t , appear in Figure 2. The lowest emittances were attained for the flat-top photocathode laser pulse, culminating with $\varepsilon_{\perp} = 190$ nm for the 250-meV MTE, $\varepsilon_{\perp} = 170$ nm for the 60-meV MTE, and $\varepsilon_{\perp} = 112$ nm for the 5-meV MTE. The Pareto fronts associated with a Gaussian laser pulse indicate worse emittance values. In general, the flat-top laser pulse favors smaller emittance at the expense of an increase in bunch duration.

Some of the operating points on the Pareto front were examined in more detail. Table 2 summarizes the optimized operating parameters and resulting beam parameters for the three flat-top laser-distribution cases mentioned previously (which gives brighter bunches compared to the short laser-pulse distribution). Figure 3 compares the transverse emittance evolution along the accelerator for the two laser configurations for each of the three MTEs, confirming that the flat-top photocathode laser pulse consistently provides superior performances, with emittances of \sim two-fold smaller than the Gaussian laser pulse. This can partially be explained by the short pulse laser and low charge involved, resulting in a condition for the blow-out regime to be marginally satisfied [9]. Figure 4 depicts the transverse rms beam sizes (σ_x and σ_y) and longitudinal rms length, σ_z , for the flat-top laser pulse case. It is worth noting that in these configurations, the bunch length decreases during acceleration in the first two cavities via velocity bunching. Additionally, the lower MTE generally leads to a working point that favors shorter bunch lengths. For lower MTEs, the longitudinal phase-space distribution has more prominent nonlinear correlations that

become more pronounced (resulting in a “S” shape correlation) as the MTE is lowered; see Figures 4g–i. This effect most likely originates from the finite rise- and fall-time associated with the flat-top laser distribution (see Figure 1c) and increases as the MTE decreases due to longitudinal space charge increases coming from the shorter bunch length explored by the optimizer.

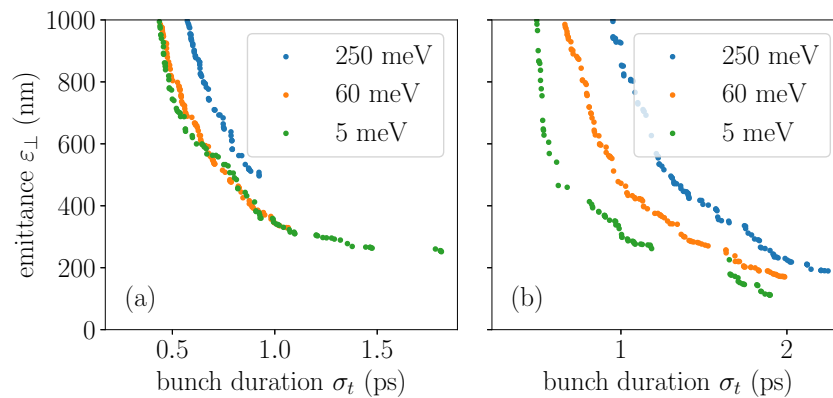


Figure 2. Pareto fronts of transverse normalized emittance and bunch duration for different MTEs using a Gaussian laser pulse (a) and a flat-top laser pulse (b). The optimization considers a 100 pC bunch charge.

Table 2. Values of optimized parameters “Beamline Settings” for the optimized flat-top cases for each photocathode MTE along with the resulting final beam parameters “Beam Parameters”.

Photocathode MTE (meV)	250	60	5
Beamline Settings			
Laser rms spot size $\sigma_{\perp,c}$ (mm)	0.146	0.239	0.255
Laser launch phase (°)	−2.88	5.30	−3.08
Peak field on photocathode (MV/m)	75.12	64.62	72.37
Cavity C1 phase (°)	−49.82	−43.17	−49.52
Cavity C1 amplitude (MV/m)	19.96	17.73	19.97
Cavity C2 phase (°)	−49.96	−48.25	11.21
Cavity C2 amplitude (MV/m)	10.18	11.01	13.53
LB peak magnetic field (T)	0.34	0.25	0.32
LF peak magnetic field (T)	−0.34	−0.26	−0.32
LM peak magnetic field (T)	−0.25	−0.25	−0.24
LS1 peak magnetic field (T)	0.02	0.04	0.08
Beam parameters			
Kinetic energy K (MeV)	37.53	36.71	39.96
Transverse emittance ε_{\perp} (μm)	0.190	0.170	0.112
Bunch length σ_z (mm)	0.674	0.596	0.570
Peak current \hat{I} (A)	16.85	17.43	16.95
Brightness B_{5d} (TA·m ^{−2})	466.63	603.16	1350.93

These optimizations are promising as they indicate that sub-200 nm transverse emittances can be attained using the AWA. However, the model assumes the fields are cylindrical-symmetric. A significant source of emittance dilution is the impact of the asymmetric RF-field topology due to the RF-input ports located in the middle cell of the cavities. Generally, we expect the transverse emittance to grow due to the corresponding time-dependent transverse kick. Such an effect is also expected to scale linearly with bunch length [10].

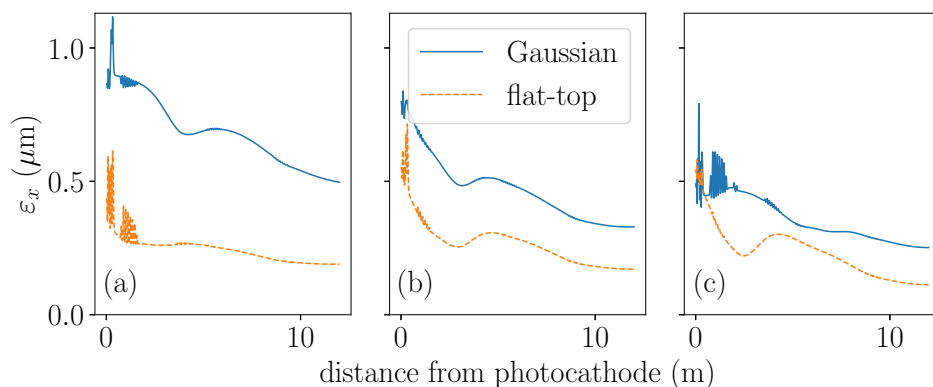


Figure 3. Emittance evolution along the AWA beamline for an MTE value of 250 (a), 60 (b), and 5 meV (c). The solid and dash traces correspond, respectively, to the case of a Gaussian and flat-top temporal shape for the photocathode laser pulse.

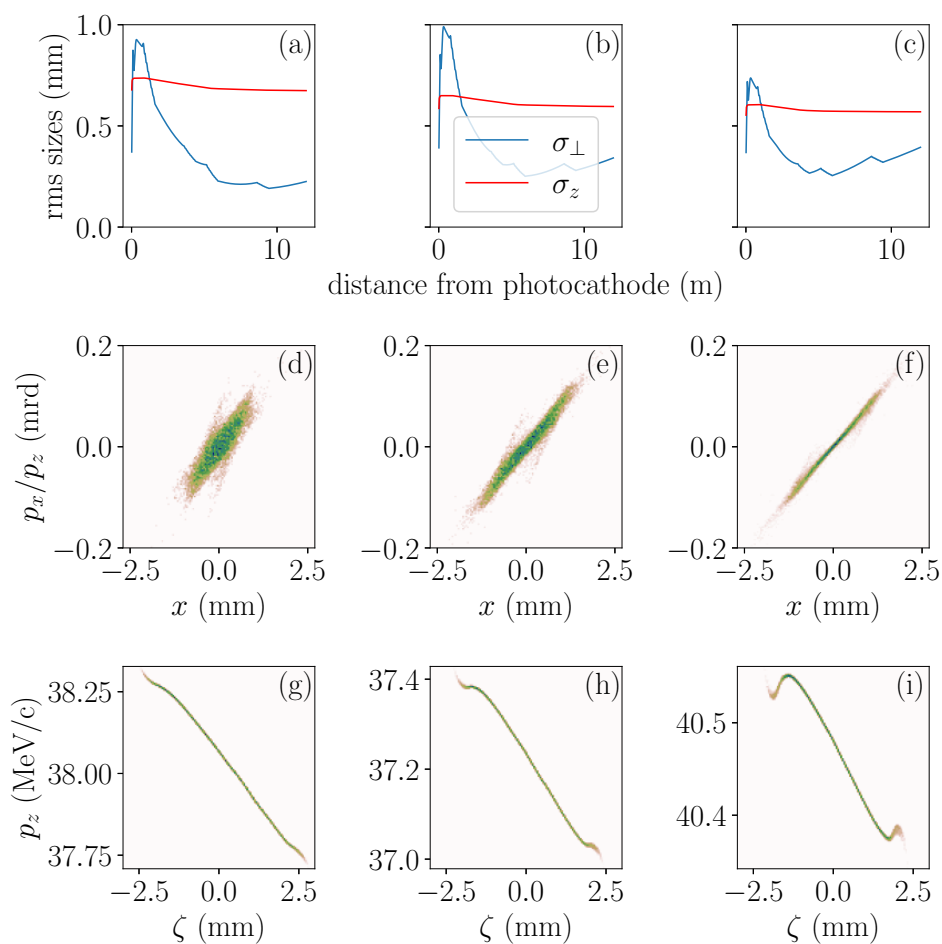


Figure 4. Example of bunch length (σ_z) and transverse size (σ_\perp) evolution (a–c) with the corresponding final transverse (d–f) and longitudinal (g–i) phase spaces simulated using a flat-top laser pulse for an MTE of 250 (a,d,g), 60 (b,e,h), and 5 meV (c,f,i). Only the horizontal phase space (x, p_x) is shown, given that the beam is cylindrical-symmetric. The colormap in the density plots (d–i) represents the particle density with blue (resp. orange) corresponding to a higher (resp. lower) charge density.

3.3. Impact of 3D Fields

In this section, we investigate the impact of realistic electromagnetic fields in the linac. AWA incorporates seven-cell accelerating cavities that are operated in the $TM_{010,\pi}$ mode. In the original design, the RF power is fed to the middle cell using a single-sided waveguide [1], and a subsequent modification to the linac introduces a dual feed in an attempt to symmetrize the middle cell and cancel the dipole kick [2]. In the proposed upgrade, the first two cavities are symmetrized, whereas the other follows the original design. Specifically, cavity C3 has its input coupler located in the $+\hat{x}$ direction, and all the following cavities have their input couplers oriented in the $-\hat{x}$ direction (here, we take $+\hat{z}$ to run along the beam direction and $+\hat{y}$ to point in the upward (vertical) direction). In order to quantify the impact of these realistic fields, we performed 3D electromagnetic simulations using an OMEGA3P frequency domain eigen solver [11]. The electromagnetic field maps were interpolated on a 3D Cartesian grid with $61 \times 61 \times 601$ cells and were imported into ASTRA for tracking. The OMEGA3P simulations were performed using a mesh with quadratic, tetrahedral elements and fourth-order basis functions.

In order to understand the impact of the field, we first performed simulations using a bunch composed of mono-energetic macroparticles (with a kinetic energy of $K = 5$ MeV) organized as a 2D transverse grid in (x, y) with vanishing transverse momentum $p_x = p_y = 0$. The bunch is tracked in the two 3D-field maps (associated with the single- and dual-coupler configuration cavities) and by using the 1D model described above, where the electromagnetic field components are received from the on-axis field $E_z(x = y = 0, z)$. The three cases are compared in Figure 5. As expected, the single-side RF input coupler introduces a significant dipole-like kick (see Figure 5d), which is strongly suppressed in the case of the dual-coupler configuration; see Figure 5e. In the latter case, we find that the relative deviation in transverse momentum compared to the paraxial approximation using the axial electric field is $\delta p_{\perp} \geq 0.4$ keV/c.

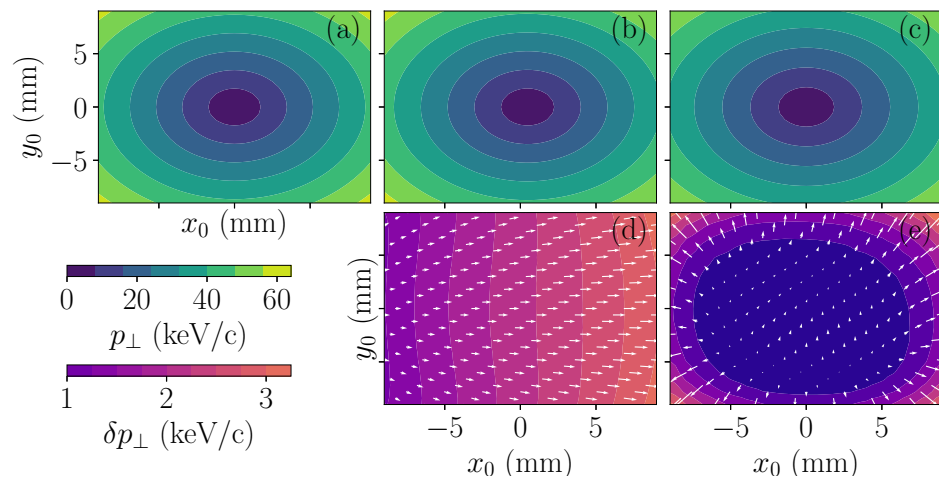


Figure 5. Change in transverse momentum, p_{\perp} , as a particle with the initial co-ordinates (x_0, y_0) passes through an accelerating cavity, as described using the 1D model (a) and the 3D field maps associated with a single (b), and dual RF-input coupler (c). Contours (d) and (e) represent the difference map between, respectively, (b) and (a) and between (c) and (a). The color map for contour (e) is scaled by $\times 10$ so that the maximum value is about $\delta p_{\perp} \simeq 0.3$ keV/c.

The 3D fields associated with the configuration planned for the AWA upgrade depicted in Figure 1 were used to examine the impact on the beam emittance for one of the optimized cases. For this study, we considered the case of an MTE of 250 meV optimized for the lowest emittance corresponding to the orange trace in Figure 3a. Figure 6a compares the evolution of the transverse emittance for the cases when the fields are considered to be cylindrical-symmetric (as assumed in Section 3.2 and when the OMEGA3P 3D field maps are employed). First, as already indicated in Figure 5, the dual-coupler configuration cavities

(centered at 1.8 and 4 m) do not degrade beam emittance (the 1D and 3D versions are in very good agreement up to the exit of C2 at a distance of $s \simeq 5$ m from the photocathode). As the beam passes through the middle cell of cavity C3 (with the RF input coupler in the $+\hat{x}$ direction), it receives a strong kick, which results in a ~ 2 -fold emittance increase in the horizontal plane. Finally, as the beam passes through the last power cavity C4 (with its RF input coupler in the $-\hat{x}$ direction), the reverse time-dependent kick cancels the emittance growth induced in C3, resulting in the final emittance within $\sim 10\%$ of the emittance computed for the case, assuming axisymmetric cavities. Further examination of the spatiotemporal distribution confirms that the correlations are not exactly compensated for, leading to a head-tail displacement in the horizontal plane; see Figure 6g. Further optimization using the realistic 3D map, including control of the beam trajectory (offset and angle of injection in the cavities), could provide further improvements.

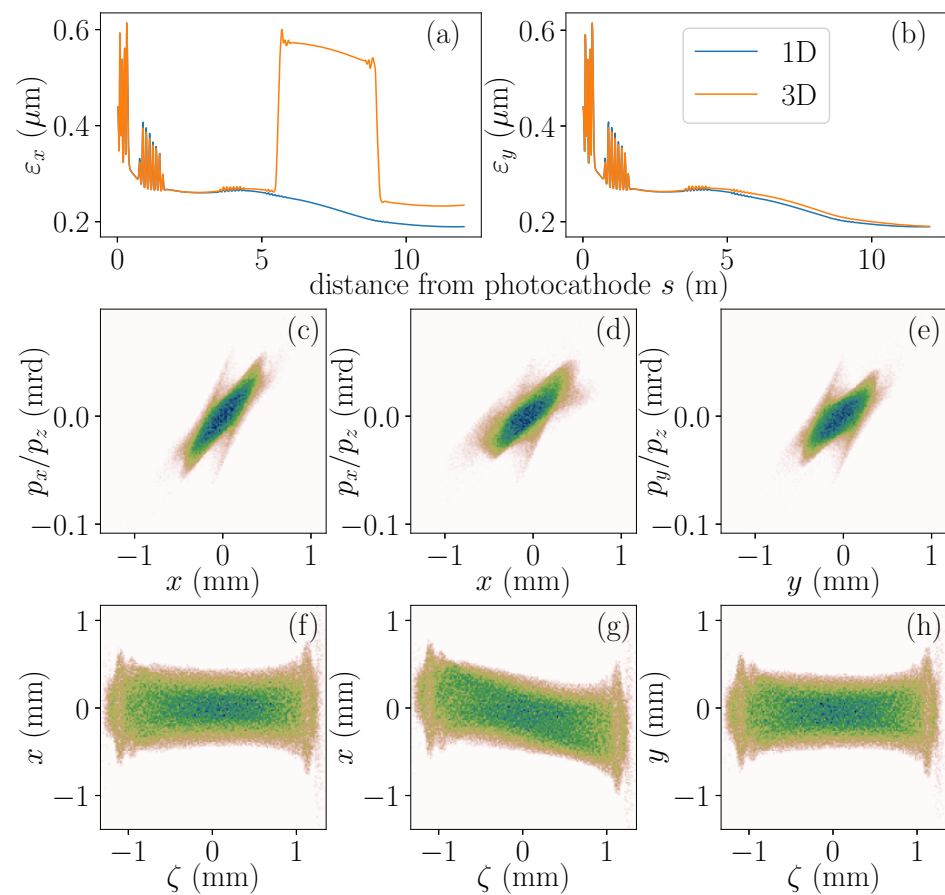


Figure 6. Horizontal (a) and vertical (b) emittance evolution along the beamline for the 1D (blue) and 3D (orange) field map model and the associated transverse phase-space (c–e) and spatiotemporal (f–h) distributions. The density plots (c,f) give the phase space associated with the 1D model (cylindrical symmetry), whereas the plots (d,g) and (e,h) give the distributions along the horizontal and vertical direction, respectively, for the 3D map model. The colormap used in the density plots (c–h) is the same as employed in Figure 4.

It should be noted that our simulations do not include a 3D field map for the RF gun at this point. However, the RF gun was modified to have a four-fold symmetry (suppression of dipolar- and quadrupolar-kick components), and we expect its effect on the beam dynamics to be minimal.

3.4. Opportunity for Peak Current Enhancement via Magnetic Bunch Compression

The use of a magnetic bunch compressor to increase the peak current, \hat{I} , and thus, the brightness (see Equation (1)), was explored. The chicane geometry is highly constrained as it reuses the first part of an already installed beamline associated with a transverse-to-longitudinal phase-space exchanger [12]; see Ref. [13]. The compressor reuses an available beamline and is arranged as an achromatic chicane composed of four dipole magnets with bending angles $(+20^\circ, -20^\circ, -20^\circ, +20^\circ)$. When a beam propagates through the bending dipoles of the chicane, it emits coherent synchrotron radiation (CSR), which interacts with the bunch and generally impacts the beam brightness. Simulations were performed to examine the possibility of enhancing the peak current and to quantify the emittance dilution during the bunch compression process. These simulations were performed using the self-consistent version of the LW3D code, which is a large-scale parallel program that computes the Liénard-Wiechert fields from first principles and applies them to the macroparticles at each time step [14].

In Section 3.2, we considered the distribution to be optimized for the 5-meV MTE and flat-top laser distribution. The initial and final beam currents appear in Figure 7a, along with the final (b) longitudinal phase-space distribution. The peak current increases by a factor of \sim seven during compression and the longitudinal phase space is highly disrupted.

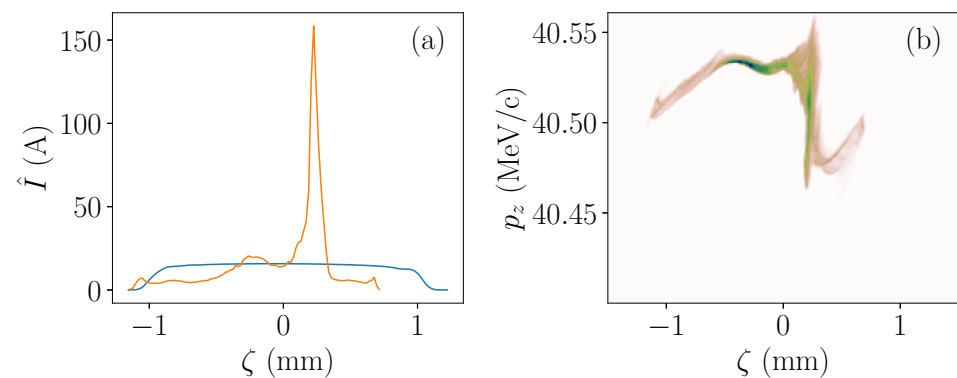


Figure 7. Initial (blue curve) and final (orange curve) peak current (a), along with the final longitudinal phase-space distribution (b), after magnetic bunch compression. The colormap used in the density plot (b) is the same as employed in Figure 4.

The final horizontal (bending-plane) emittance is found to increase by more than one order of magnitude, i.e., from 126 nm to $\varepsilon_{x,f} = 2.7 \mu\text{m}$. Considering the eigen emittances, we find the final horizontal emittance to be $\varepsilon_{1,f} = 1.7 \mu\text{m}$, which is $\sim 40\%$ smaller than $\varepsilon_{x,f}$. Such a discrepancy between the projected and eigen emittances indicates that linear cross-plane correlations are present in the final beam distribution, and the proper correction of this coupling could further improve the projected emittance.

4. Discussion

The simulations presented in this paper indicate that obtaining low-emittance 100 pC bunches using the AWA drive beam accelerator is possible. Specifically, low emittance can be obtained using a flat-top laser pulse. In the near term, this model will be validated against experiments at the AWA. These experiments could present some challenges, as a stable beam and high-resolution diagnostics will also be required.

These simulations also confirm that the photocathode MTE does have an impact on the final transverse emittance of the electron beam in the considered photo-injector. Therefore, reducing the MTE of the photocathode would be beneficial to produce brighter bunches from the AWA photo-injector. A transverse emittance close to 100 nm was obtained for the 5 meV MTE. Consequently, we are planning an experimental campaign to explore the generation of bright bunches at AWA. In the first phase, and once the photo-injector is upgraded with a symmetrized RF gun for the first two accelerating cavities, the current

photocathode (Cs₂Te with 250-meV MTE) will be employed to validate the working point devised in this paper. Specifically, a digital-twin model of the AWA linac will be developed to precisely calibrate the operating parameters with physical quantities (e.g., RF input power set in the control room with a peak field in the RF gun or RF cavity). Such a model will ease the practical implementation of the optimum working point devised in this paper. The beam parameters (emittance and bunch length) will be measured and further optimized experimentally. These initial results will provide further guidance on the benefit of using lower MTE photocathodes as they become available from the Center for Bright Beam Collaborations. A second experimental phase will be dedicated to directly investigating the performances of lower MTE photocathodes within the AWA photo-injector. However, these photocathodes will first need to go through extensive characterization in a standalone L-band gun, which is available at the AWA facility.

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Data Availability Statement: The data presented in this study are available upon request from the corresponding author.

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