# Observation of tripleJ/ $\Psi$ meson production in proton-proton collisions 

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#### Abstract

Protons consist of three valence quarks, two up-quarks and one down-quark, held together by gluons and a sea of quark-antiquark pairs. Collectively, quarks and gluons are referred to as partons. In a proton-proton collision, typically only one parton of each proton undergoes a hard scattering referred to as single-parton scattering - leaving the remainder of each proton only slightly disturbed. Here, we report the study of double- and triple-parton scatterings through the simultaneous production of three J $/ \psi$ mesons, which consist of a charm quark-antiquark pair, in proton-proton collisions recorded with the CMS experiment at the Large Hadron Collider. We observed this process - reconstructed through the decays of J $/ \psi$ mesons into pairs of oppositely charged muons - with a statistical significance above five standard deviations. We measured the inclusive fiducial cross-section to be $272_{-104}^{+141}$ (stat) $\pm 17$ (syst) fb, and compared it to theoretical expectations for triple- $\mathrm{J} / \psi$ meson production in single-, double- and triple-parton scattering scenarios. Assuming factorization of multiple hard-scattering probabilities in terms of single-parton scattering cross-sections, doubleand triple-parton scattering are the dominant contributions for the measured process.


High-energy particle accelerators are unique tools to study the structure of matter at the shortest distances. The most powerful accelerator today is the CERN Large Hadron Collider (LHC) that has so far collided beams of protons with energies of up to 6.5 TeV , resulting in centre-of-mass energies of up to 13 TeV . Protons are used in energy-frontier colliders because they are relatively easy to accelerate and keep in a circular orbit to enable high collision rates. However, they are not fundamental particles and, in fact, have a complicated quantum mechanical structure. Protons consist of three quarks, two up-type and one down-type, and gluons, which hold together the three valence quarks, as well as of a 'sea' of virtual quark-antiquark pairs, which are fundamental elements of the quantum vacuum. All these components are referred to as 'partons'. In the standard picture of proton-proton (pp) collisions, typically only a few partons undergo a hard scattering with one another, with the remainders of each proton only slightly disturbed in the process. As the collision energy increases, the densities of gluons and sea quarks probed inside each proton grow
rapidly. Thus, at high enough energies, more than one pair of partons can undergo a hard scattering in a single pp collision, leading to the simultaneous and independent production of two or more particles with transverse momentum $\left(p_{T}\right)$ and/or mass $(m)$ above a few gigaelectronvolts. Double-parton scatterings (DPS) were first observed at the CERN Intersecting Storage Rings some 35 years ago ${ }^{1,2}$ and have been a subject of intense theoretical and experimental investigations ever since ${ }^{3}$. Numerous DPS processes have been studied in measurements with many combinations of pairs of heavy and/or high- $p_{\mathrm{T}}$ produced particles ${ }^{3}$. Triple-parton scatterings (TPSs), where three hard parton interactions take place simultaneously, have been proposed for study only recently ${ }^{4}$ and have not been experimentally explored yet. Studies of $n$-parton scattering (NPS) processes are important to elucidate the complicated inner structure of the proton and its evolution with energy ${ }^{5,6}$. Many of these features, for example, the parton density profile in the plane transverse to the colliding beams, as well as the various correlations (in position, momentum, flavour, colour, spin

[^0]and so on) between individual partons, are very difficult to calculate theoretically, and can only be mapped out through experimental studies of NPS in different systems and for different numbers $n$ of simultaneous scatterings ${ }^{3}$.

Measurements of such processes not only allow for a deeper understanding of the proton structure but also are of relevance at the LHC to predict backgrounds in rare standard-model processes, and in searches for new physics, in final states where multiple heavy particles are produced ${ }^{7,8}$. This Article presents the experimental study of the simultaneous production of three massive particles originating in NPS, and the observation of triple- $\mathrm{J} / \psi$ meson production. The study of TPS via triple- $J / \Psi$ production provides input for further theoretical and experimental progress in understanding the NPS dynamics.

In the simplest approach, ignoring any correlations between the individual partons, the probability to produce $n$ high- $p_{\mathrm{T}}$ particles in a given pp collision must be proportional to the $n$th product of probabilities to independently produce each of them. Thus, the probability to produce two or three high $-p_{\mathrm{T}}$ particles in DPS and TPS scales with the square and cube, respectively, of the corresponding single-parton scattering (SPS) probabilities ${ }^{9}$. The occurrence of DPS and TPS processes is therefore more likely for final states with large SPS cross-sections, such as quarkonia states (for example, $J / \psi$ and $r$ mesons), than for rarer heavier particles, such as electroweak bosons ${ }^{10}$. In the DPS case, the cross-section to produce, for example, two charmonium mesons $\psi_{1}$ and $\psi_{2}$ can be written as the product of the SPS cross-sections for the production of each individual meson divided by an effective cross-section to warrant the proper units of the final result

$$
\begin{equation*}
\sigma_{\mathrm{DPS}}^{\mathrm{pp} \rightarrow \psi_{1} \psi_{2}+X}=\left(\frac{\mathfrak{m}}{2}\right) \frac{\sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow \psi_{1}+X} \sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow \psi_{2}+X}}{\sigma_{\mathrm{eff,DPS}}} \tag{1}
\end{equation*}
$$

Here, $\mathfrak{m}$ is a combinatorial factor to avoid double counting, $\mathfrak{m}=1$ (2) if $\psi_{1}=\psi_{2}\left(\psi_{1} \neq \psi_{2}\right)$, and $\sigma_{\text {eff.,Ds }}$ is an effective cross-section that, in a purely geometric approach, can be determined from the pp transverse overlap ${ }^{9}$. A smaller value of $\sigma_{\text {eff,DPs }}$, which is proportional to the average (squared) transverse separation of the partons participating in the two hard scatterings, implies larger DPS yields.

For the proton form factors typically implemented in the Pythia $8^{11}$ and Herwig $+{ }^{12}$ event generators commonly used in collider physics, values of $\sigma_{\text {eff.DPs }} \approx 20-30 \mathrm{mb}$ are expected. Such estimates are, however, about a factor of two larger than those experimentally derived via the ratio $\sigma_{\text {eff,DPS }}=\left(\sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow x_{1}} \sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow x_{2}}\right) / \sigma_{\mathrm{DPS}}^{\mathrm{pp} \rightarrow \mathrm{x}_{1} \mathrm{x}_{2}}$ for processes involving pairs of high $-p_{\mathrm{T}}$ jets and/or electroweak bosons, which are found to lie in the range $\sigma_{\text {eff,DPs }} \approx 10-20 \mathrm{mb}$ (refs. ${ }^{13-19}$ ). This discrepancy has been mostly explained as evidence of parton correlations in the collision not accounted for in the purely geometrical approaches ${ }^{20}$. In addition, significantly lower $\sigma_{\text {eff,Dps }} \approx 3-10 \mathrm{mb}$ values have been extracted from measurements of quarkonium pair production $\left(J / \psi J / \psi\right.$ (refs. ${ }^{21-25}$ ), $J / \psi r\left(\right.$ ref. ${ }^{26}$ ) and $r r\left(\right.$ refs. $\left.{ }^{8,27}\right)$ ) that have been interpreted as due to the different dominant species (mostly gluons for quarkonia, and quarks for electroweak bosons) in the parton distribution functions (PDFs) probed in the different scatterings ${ }^{3}$, but can be also attributed in some cases to poorly controlled subtractions of SPS contributions ${ }^{10}$.

The study of TPS via triple-J/ $\psi$ production can help solve all the issues mentioned above. The equivalent of equation (1) for the production of three charmonium mesons in a TPS process reads

$$
\begin{equation*}
\sigma_{\mathrm{TPS}}^{\mathrm{pp} \rightarrow \psi_{1} \psi_{2} \psi_{3}+X}=\left(\frac{\mathfrak{m}}{3!}\right) \frac{\sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow \psi_{1}+X} \sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow \psi_{2}+X} \sigma_{\mathrm{SPS}}^{\mathrm{pp} \rightarrow \psi_{3}+X}}{\sigma_{\mathrm{eff}, \mathrm{TPS}}^{2}} \tag{2}
\end{equation*}
$$

where $\mathfrak{m}=1,3$ or 6 (depending on whether all three, two or none of the $\psi_{i}$ states are identical). In the absence of parton correlations, the effective cross-section $\sigma_{\text {eff,TPS }}$ is closely related to its DPS counterpart via
$\sigma_{\text {eff,TPS }}=\kappa \sigma_{\text {eff,DPS }}$, with $\kappa$ of order unity. A value of $\kappa=0.82 \pm 0.11$ has been derived in ref. ${ }^{4}$ for a variety of proton transverse parton profiles. A theoretical study of the production of three prompt- $J / \psi$ mesons ${ }^{28}$, based on the non-relativistic quantum chromodynamics approach at leading-order (LO) accuracy as implemented in the HELAC-Onia code ${ }^{29,30}$, has demonstrated that the pure SPS contributions are negligible compared with those from DPS and TPS. Namely, the top left diagram of Fig. 1 is irrelevant compared with the two other diagrams in the left column of the figure. The experimental measurement of $\mathrm{pp} \rightarrow \mathrm{J} / \psi \mathrm{J} / \psi \mathrm{J} / \psi X$ is thus a golden channel for the study of TPS and, in addition, provides an alternative extraction of $\sigma_{\text {eff.,DPs }}$, thereby shedding light on the underlying dynamics of hard NPS. The production of $J / \psi$ states can also proceed non-promptly through the decay of a beauty-quark $(b)$ hadron. Notwithstanding a small branching fraction, $\mathcal{B}_{b \rightarrow J / \psi X} \approx 1 \%\left(\right.$ ref. $\left.{ }^{31}\right)$, the cross-section to produce $b \bar{b}$ pairs is large at the LHC, $\sigma(\mathrm{pp} \rightarrow b \bar{b} X) \approx 0.5 \mathrm{mb}\left(\mathrm{ref} .^{4}\right)$. The contributions of such processes to inclusive triple- $/ / \psi$ production are schematically shown in Fig. 1 (diagrams to the right of the vertical dashed line).

This Article reports the observation of the simultaneous production of three $/ / \psi$ mesons in pp collisions. The analysis is based on a data sample collected at $\sqrt{s}=13 \mathrm{TeV}$ by the Compact Muon Solenoid (CMS) experiment, corresponding to an integrated luminosity of $133 \mathrm{fb}^{-1}$. The $J / \psi$ mesons are reconstructed in their dimuon decay mode over a fiducial phase space in transverse momenta ( $p_{T}^{\mu, / 4}$ ) and (pseudo) rapidities $\left(\left|\eta^{\mu}\right|\right.$ and $\left.\left|\left.\right|^{J / \psi}\right|\right)$ defined to maximize the signal purity and the detector acceptance and efficiency. The analysis of the $6 \mu$ final state offers a very clean experimental signature for inclusive triple- $J / \psi$ production, comprising prompt and non-prompt components. Methods provides more details on the experimental set-up and event reconstruction (the $J / \psi$ candidates passing the triple $-J / \psi$ selection criteria are shown in Extended Data Table 1).

The signal yield is extracted with a three-dimensional unbinned extended maximum likelihood fit of the $m_{\mu^{+} \mu^{-}}$distributions of all $J / \psi$ candidates in the event over the $2.9 \mathrm{GeV}<m_{\mu^{+} \mu^{-}}<3.3 \mathrm{GeV}$ range. The expected $J / \psi$ mass peaks are modelled with a Gaussian function with mean fixed to their nominal value $\left(m^{/ / \psi}=3.097 \mathrm{GeV}\right)^{31}$ and the root-mean-square (RMS) width fixed to the resolution derived from the Monte Carlo (MC) simulation ( $\sigma_{m} \approx 30 \mathrm{MeV}$ ). Given the very low number of events passing the selection, the mass mean and RMS width of the $J / \psi$ mesons cannot be left as free parameters in the fit. The dimuon background is described with an exponential function ${ }^{23,32-35}$. The fit has eight free parameters for the yields given by the combination of each of the three $J / \psi$ candidates as being either signal or background. The extracted signal yield (red shaded areas in the $m_{\mu^{+} \mu^{-}}$distributions of Fig. 2) corresponds to $N_{\text {sig }}^{3 / / \psi}=5.0_{-1.9}^{+2.6}$ triple $-J / \psi$ events, with $1.0_{-0.8}^{+1.4}$ background events. The statistical significance of the signal is evaluated using various methods. From the likelihood ratio of two fits (background-only imposing $N_{\text {sig }}^{3 / /}=0$, and the default signal-plus-background), with the standard asymptotic formula ${ }^{36}$ assuming that the conditions to apply Wilks' theorem ${ }^{37}$ are satisfied, a significance of 6.7 standard deviations (s.d.) is obtained. The significance derived assuming a Poisson counting experiment yields 5.8 s.d., and it is found to be above 5.5 s.d. by using MC pseudoexperiments.

To cross-check the size of the combinatorial background derived from the fit, two tests are carried out. First, the fit is repeated over the extended dimuon mass range [2.5-3.3] GeV for the two subleading $J / \psi$ mesons (dotted curves in Fig. 2). This mass range corresponds to an asymmetric window of about $\left[-20 \sigma_{m},+7 \sigma_{m}\right]$ around the $J / \psi$ nominal mass that, as aforementioned, covers lower dimuon masses where the background, if any, should be larger. The obtained signal yield is fully consistent with the default result. A second test is performed whereby the opposite-sign (OS) requirement is removed to allow also for same-sign dimuon combinations ( $\mu^{ \pm} \mu^{ \pm}$) for the two subleading pairs. After applying the rest of the selection criteria of the default analysis, no triplet events containing same-sign muon pairs are observed.


Fig. 1 Leading-order diagrams for inclusive triple- $J / \psi$ production in pp collisions. The SPS, DPS and TPS processes are depicted in the top, middle and bottom rows, respectively. The leftmost diagrams show triple prompt-J/ $\psi$ processes. The remaining diagrams show (left to right) final states with increasing contributions of non-prompt $-J / \psi$ mesons from beauty hadron decays.

Curly lines indicate gluons, arrows indicate (anti)charm quarks and ovals indicate the proton parton densities. The symbols $\sigma_{\text {NPS }}^{i \mathrm{p} j \mathrm{np}}$ identify the number ( $i$ and $j$ ) of prompt (p) and non-prompt (np) contributions to the cross-section of each diagram.


Fig. $2 \mid$ Invariant mass distributions for the three $\boldsymbol{\mu}^{+} \boldsymbol{\mu}^{-}$pairs in the selected events. The three distributions are ordered, left to right, by decreasing pair $p_{\mathrm{T}}$. The data are represented by the points with the vertical bars showing the (Poisson) statistical uncertainties. The solid (dotted) curve shows the overall fit to the data (in the extended mass range, discussed in the main text), and the red shaded area shows the fitted signal yield. The horizontal bin width is indicated on the vertical axis legend.

To estimate the average prompt and non-prompt contributions in the triple $J / \psi$ events, the proper decay length of each $J / \psi$ is calculated as $L^{J / \psi}=\left(m^{/ / \psi} / p_{\mathrm{T}}^{\prime / \psi}\right) L_{x y}^{/ / \psi}$, where $L_{x y}^{J / \psi}=\left(\mathbf{r} \cdot \mathbf{p}_{\mathrm{T}}^{J / \psi}\right) /\left|p_{\mathrm{T}}^{/ / \psi}\right|$ is the transverse distance between the $J / \psi$ decay vertex and the primary pp interaction vertex (PV) ( $\mathbf{r}$ is the vector from the PV to the $J / \psi$ vertex). The experimental resolution on $L^{J / \psi}$ is about $20 \mu \mathrm{~m}$. Prompt $-J / \psi$ mesons are defined as those having $L^{J / \psi}<60 \mu \mathrm{~m}$, a choice that reduces the non-prompt contribution by more than one order in magnitude ${ }^{33}$. A signal-only subset of events is defined based on all $/ / \psi$ candidates
found in a narrower invariant mass region, within $\pm 3$ s.d. around $m^{/ / \psi}$, than that used in the default signal extraction. In this range, five triple- $/ / \psi$ events are found that can be classified as two events being consistent with the ' 2 non-prompt +1 prompt $J / \psi$ ' hypothesis, and one event each in the ' 1 non-prompt +2 prompt $J / \psi^{\prime}, 3$ non-prompt $J / \psi$ ' and ' 3 prompt $J / \psi$ ' categories. Such a classification is confirmed with a second method where prompt and non-prompt weights are extracted with the sPlot technique ${ }^{38}$, exploiting an unbinned maximum likelihood fit of the $L^{J / \psi}$ distributions.

Table 1 | Fiducial phase space for the triple-J/ $\Psi$ cross-section measurement

| For all muons | $p_{\mathrm{T}}>3.5 \mathrm{GeV}$ for $\|\eta\|<1.2$ |
| :--- | :--- |
|  | $p_{\mathrm{T}}>2.5 \mathrm{GeV}$ for $1.2<\|\eta\|<2.4$ |
| For all J/ $\psi$ mesons | $p_{\mathrm{T}}>6 \mathrm{GeV}$ and $\|y\|<2.4$ |
|  | $2.9 \mathrm{GeV}<m_{\mu^{+} \mu^{-}}<3.3 \mathrm{GeV}$ |

The cross-section for inclusive triple- $/ / \psi$ production measured in the fiducial region defined in Table 1 is obtained via $\sigma(\mathrm{pp} \rightarrow \mathrm{J} / \psi J /$ $\psi J / \psi X)=N_{\text {sig }}^{3 / / \psi} /\left(\epsilon \mathcal{L}_{\text {int }} \mathcal{B}_{J / \psi \rightarrow \mu^{+} \mu^{-}}^{3}\right)$, where $N_{\text {sig }}^{3 / / \psi}$ is the number of signal events, $\mathcal{L}_{\text {int }}$ is the total integrated luminosity, $\mathcal{B}_{J / \psi \rightarrow \mu^{+} \mu^{-}}$is the dimuon branching fraction and $\epsilon=\epsilon_{\text {tri }} \epsilon_{\text {id }} \epsilon_{\text {reco }}$ is the total efficiency composed of trigger, identification and reconstruction components, respectively. The $J / \psi$ muon identification and reconstruction efficiencies are extracted with the tag-and-probe method using correction factors from the large inclusive $J / \psi \rightarrow \mu^{+} \mu^{-}$data samples used in ref. ${ }^{39}$. As they depend on the $p_{\mathrm{T}}$ and $\eta$ of the muons, they propagate into the final cross-section via two-dimensional maps, yielding $\epsilon_{\mathrm{id}} \epsilon_{\text {reco }}=0.78$. The trigger efficiency is found to be $\epsilon_{\text {trig }}=0.84$ from a study of the MC samples.

The impact on the extracted cross-section of the choice of functions used to reproduce the shapes of the signal and background dimuon invariant masses is studied. For the signal, the Gaussian distribution is changed to a Crystal-Ball function ${ }^{40}$ as well as to a Gaussian function with the RMS width left to vary in the fit. The background shape is changed from the default exponential to first-and zeroth-order polynomials. The relative differences in the cross-sections obtained from the alternative modelling for signal and background are $0.8 \%$ and $3.4 \%$, respectively, and are assigned as corresponding systematic uncertainties. Uncertainties arising from the muon reconstruction and identification efficiencies are derived by allowing the tag-and-probe correction factors for each ( $p_{\mathrm{T}}, \eta$ ) bin to vary within their precision, and checking the effect on the extracted cross-section. The maximal variation observed is $\pm 1.0 \%$. Varying the relative composition of double- and single- $J / \psi$ meson production in the MC event sample used for the determination of the trigger efficiency leads to a $3.4 \%$ propagated uncertainty. Uncertainties of $1.6 \%$ and $3.0 \%$ are added from the integrated luminosity measurement ${ }^{41-43}$, and from the simulated signal sample size, respectively. The uncertainty in the $\mathcal{B}_{J / \psi \rightarrow \mu^{+} \mu^{-}}=(5.961 \pm 0.033) \%$ value ${ }^{31-33}$ propagates into a $1.7 \%$ uncertainty in the cross-section. The total systematic uncertainty of the measured cross-section is $6.2 \%$, obtained by adding all individual sources in quadrature (Extended Data Table 2). The measured cross-section for triple- $/ / \psi$ production, within the fiducial region defined in Table 1 , is $\sigma(\mathrm{pp} \rightarrow J / \psi J / \psi J / \psi X)=272_{-104}^{+141}$ (stat) $\pm 17$ (syst) fb

The total inclusive triple $J / \psi$ cross-section is expected to correspond to the sum of the contributions from the SPS, DPS and TPS processes schematically shown in Fig. 1, each of which contains various combinations of prompt (p) and non-prompt (np) $J / \psi$ contributions

$$
\begin{align*}
\sigma_{\mathrm{tot}}^{3 / / \psi} & =\sigma_{\mathrm{SPS}}^{3 / / \psi}+\sigma_{\mathrm{DPS}}^{3 \mathrm{~J} / \psi}+\sigma_{\mathrm{TPS}}^{3 / \psi} \\
& =\left(\sigma_{\mathrm{SPS}}^{3 \mathrm{p}}+\sigma_{\mathrm{SPS}}^{2 \mathrm{p} 1 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{1 \mathrm{p} 2 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{3 \mathrm{np}}\right)  \tag{3}\\
& +\left(\sigma_{\mathrm{DPS}}^{3 \mathrm{p}}+\sigma_{\mathrm{DPS}}^{2 \mathrm{p} 1 \mathrm{np}}+\sigma_{\mathrm{DPS}}^{1 \mathrm{p} 2 \mathrm{np}}+\sigma_{\mathrm{DPS}}^{3 \mathrm{np}}\right) \\
& +\left(\sigma_{\mathrm{TPS}}^{3 \mathrm{p}}+\sigma_{\mathrm{TPS}}^{2 \mathrm{p} 1 \mathrm{np}}+\sigma_{\mathrm{TPS}}^{1 \mathrm{p} 2 \mathrm{np}}+\sigma_{\mathrm{TPS}}^{3 \mathrm{np}}\right)
\end{align*}
$$

Under the simplest assumption of factorization of multiple hard-scattering probabilities in terms of SPS cross-sections, the DPS and TPS contributions to triple-J/ $\psi$ production (last row of equation (3))
can be written through equations (1) and (2) as a combination of products of single- and double- $/ / \psi$ SPS cross-sections as

$$
\begin{align*}
\sigma_{\mathrm{DPS}}^{3 J / \psi} & =\frac{\mathfrak{m}_{1}}{\sigma_{\text {eff,DPS }}} \\
& \times\left[\sigma_{\mathrm{SPS}}^{2 \mathrm{p}} \sigma_{\mathrm{SPS}}^{1 \mathrm{p}}+\sigma_{\mathrm{SPS}}^{2 \mathrm{p}} \sigma_{\mathrm{SPS}}^{1 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{1 \mathrm{p}} \sigma_{\mathrm{SPS}}^{1 \mathrm{p} 1 \mathrm{np}}\right.  \tag{4}\\
& \left.+\sigma_{\mathrm{SPS}}^{1 \mathrm{p} 1 \mathrm{np}} \sigma_{\mathrm{SPS}}^{1 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{1 \mathrm{p}} \sigma_{\mathrm{SPS}}^{2 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{2 \mathrm{np}} \sigma_{\mathrm{SPS}}^{1 \mathrm{np}}\right]
\end{align*}
$$

and

$$
\begin{align*}
\sigma_{\mathrm{TPS}}^{3 / / \psi} & =\frac{\mathfrak{m}_{3}}{\sigma_{\mathrm{eff}, \mathrm{TPS}}^{2}}\left[\left(\sigma_{\mathrm{SPS}}^{1 \mathrm{p}}\right)^{3}+\left(\sigma_{\mathrm{SPS}}^{1 \mathrm{np}}\right)^{3}\right] \\
& +\frac{\mathfrak{m}_{2}}{\sigma_{\mathrm{eff}, \mathrm{TPS}}^{2}}\left[\left(\sigma_{\mathrm{SPS}}^{1 \mathrm{p}}\right)^{2} \sigma_{\mathrm{SPS}}^{1 \mathrm{np}}+\sigma_{\mathrm{SPS}}^{1 \mathrm{p}}\left(\sigma_{\mathrm{SPS}}^{1 \mathrm{np}}\right)^{2}\right], \tag{5}
\end{align*}
$$

with combinatorial prefactors $\mathfrak{m}_{1}=2 / 2=1, \mathfrak{m}_{2}=3 / 3$ ! $=1 / 2$ and $\mathfrak{m}_{3}=1 / 3!=1 / 6$ Therefore, from the eight individual SPS cross-sections for single-, double- and triple- $J / \psi$ production, one can determine the total triple- $J / \psi$ production cross-section via equations (3)-(5). The values of the relevant SPS cross-sections, each within the fiducial phase space defined in Table 1, are computed as described next and listed in Table 2.

The values of the SPS single, double and triple prompt $-J / \psi$ cross-sections ( $\sigma_{\text {SPS }}^{1 \mathrm{p}} \sigma_{\mathrm{SPS}}^{2 \mathrm{p}}$ and $\sigma_{\mathrm{SPS}}^{3 \mathrm{p}}$ ) are obtained with HELAC-Onia at LO or at approximately next-to-leading-order ( $\mathrm{NLO}^{*}$ ) accuracy ${ }^{44,45}$. For the single prompt $-J / \psi$ prediction $\left(\sigma_{\text {sPS }}^{1 \mathrm{p}}\right)$, the theoretical calculations HO (data) in Table 2 are normalized with a parameterization ${ }^{46}$ that reproduces the data measured in pp collisions at 7 TeV (refs. ${ }^{34,47}$ ), including all feed-down contributions from decays of heavier charmonium resonances. For the double and triple prompt $-J / \psi$ processes, the HELAC-Onia calculations include only the $\psi(2 S)$ feed-down because the $\chi_{c}$ decay contribution is only a few percent. All predictions for cross-sections of non-prompt- $J / \psi$ meson production in beauty hadron decays ( $\sigma_{\mathrm{SPS}}^{1 \mathrm{np}}, \sigma_{\mathrm{SPS}}^{2 \mathrm{np}}$ and $\sigma_{\mathrm{SPS}}^{3 \mathrm{np}}$ ) have been obtained with MadGraph 5 aMC@NLO (v.2.6.6) ${ }^{48}$ matrix elements, scaled by a factor of 1.15 to account for next-to-next-to-leading-order $b \bar{b}$ cross-section corrections ${ }^{4}$, combined with the Pythia 8.244 generator for parton shower and decays (including all feed-down quarkonium contributions) ${ }^{45}$. Mixed prompt plus non-prompt cross-sections $\left(\sigma_{\mathrm{SPS}}^{X \mathrm{PY} \eta}\right)$ are obtained from $J / \psi+b \bar{b}$ events generated with HELAC-Onia at LO in the colour-singlet model interfaced with Pythia 8.244 for the $b$ quarks fragmentation into non-prompt $-/ / \psi$ mesons. The uncertainties include the (dominant) theoretical scale dependence and the (subdominant) PDF uncertainties of the CT14NLO set ${ }^{49}$, except for the single prompt $-J / \psi$ predictions that have a better precision because they are determined with an explicit fit of the non-relativistic quantum chromodynamics predictions to the LHC data ${ }^{46}$ and have an associated $10 \%$ uncertainty of experimental origin. All these sources are treated as uncorrelated and the corresponding uncertainties are added in quadrature.

Using equations (4) and (5) with the SPS cross-sections listed in Table 2, and assuming that the effective DPS and TPS crosssections are related by $\sigma_{\text {eff,TPS }}=(0.82 \pm 0.11) \sigma_{\text {eff,DPS }}\left(\right.$ ref. $\left.{ }^{4}\right)$ in a baseline approach that ignores parton correlations, one can extract the value of the effective DPS cross-section that yields the experimentally measured $\sigma_{\text {tot }}^{3 / 4}$ value. Following such a procedure, the value $\sigma_{\text {eff, DPS }}=2.7_{-1.0}^{+1.4}(\exp )_{-1.0}^{+1.5}($ theo $) \mathrm{mb}$ is derived, where the first uncertainty is due to the experimental $\sigma_{\text {tot }}^{3 / / 4}$ precision and the second is due to the propagation of all sources of theoretical uncertainties in the ingredients of equations (3)-(5).

The inclusive triple-J/ $\psi$ theoretical cross-sections and yields for each individual process contributing to the total production are listed in Table 3. The expected contributions from SPS, DPS and TPS processes to the total triple- $J / \psi$ cross-section amount to about $6 \%, 74 \%$ and $20 \%$, respectively. This confirms the conclusion of ref. ${ }^{28}$ that triple- $/ / \psi$

## Table 2 | Theoretical $J / \Psi, J / \psi+J / \psi$, and $J / \psi+J / \psi+J / \psi$ cross-sections

| SPS single-J/ $\Psi$ production |  | SPS double-J/ $\boldsymbol{\psi}$ production |  |  | SPS triple-J/ $\boldsymbol{\psi}$ production |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HO(data) | MG5NLO + Py8 | HO (NLO*) | HO(LO) + Py8 | MG5NLO + Py8 | HO(LO) | HO(LO) + Py8 | HO(LO) + Py8 | MG5NLO + Py8 |
| $\sigma_{\mathrm{SPS}}^{1 \mathrm{p}}$ | $\sigma_{\mathrm{SPS}}^{1 \mathrm{npp}}$ | $\sigma_{\mathrm{SPS}}^{2 \mathrm{p}}$ | $\sigma_{\mathrm{SPS}}^{1 \mathrm{p} 1 \mathrm{np}}$ | $\sigma_{\mathrm{SPS}}^{2 \mathrm{np}}$ | $\sigma_{\mathrm{SPS}}^{3 \mathrm{p}}$ | $\sigma_{\mathrm{SPS}}^{2 \mathrm{p} 1 \mathrm{np}}$ | $\sigma_{\mathrm{SPS}}^{1 \mathrm{p} 2 \mathrm{np}}$ | $\sigma_{\mathrm{SPS}}^{3 \mathrm{np}}$ |
| $570 \pm 57 \mathrm{nb}$ | $600_{-220}^{+130} \mathrm{nb}$ | $40_{-26}^{+80} \mathrm{pb}$ | $24_{-16}^{+35} \mathrm{fb}$ | $430_{-130}^{+95} \mathrm{pb}$ | <5ab | $5.2_{-3.3}^{+9.6} \mathrm{fb}$ | $14_{-8}^{+17} \mathrm{ab}$ | $12 \pm 4 \mathrm{fb}$ |

Predictions for single-, double- and triple- J/ $\psi$ production cross-sections in SPS processes, which pass the fiducial criteria listed in Table 1 , derived from the HELAC-Onia (HO) and MadGraph 5_aMC@NLO (MG5NLO) matrix element calculators, complemented with the Pythia 8 (Py8) parton shower, as described in the text.

Table 3 | Expected contributions to triple- $J / \boldsymbol{\psi}$ production

| Process: | $\mathbf{3 p}$ | $\mathbf{2 p + 1} \mathbf{n p}$ | $\mathbf{1 p + 2 n p}$ | $\mathbf{3 n p}$ | Total |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\sigma_{\text {SPS }}^{3 / / \psi} \mathrm{fb}$ | $<0.005$ | 5.7 | 0.014 | 12 | 18 |
| $N_{\text {SPS }}^{3 / / \psi}$ | 0.0 | 0.10 | 0.0 | 0.22 | 0.32 |
| $\sigma_{\text {DPS }}^{3 / / \psi} \mathrm{fb}$ | 8.4 | 8.9 | 90 | 95 | 202 |
| $N_{\text {DPS }}^{3 / \psi}$ | 0.15 | 0.16 | 1.65 | 1.75 | 3.7 |
| $\sigma_{\text {TPS }}^{3 / / \psi} \mathrm{fb}$ | 6.1 | 19.4 | 20.4 | 7.2 | 53 |
| $N_{\text {TPS }}^{3 / \psi}$ | 0.11 | 0.36 | 0.38 | 0.13 | 1.0 |
| $\sigma_{\text {tot }}^{3 / / \psi} \mathrm{fb}$ | 15 | 34 | 110 | 114 | 272 |
| $N_{\text {tot }}^{3 / / \psi}$ | 0.3 | 0.6 | 2.0 | 2.1 | 5.0 |

Central values of the predictions for triple- $J / \psi$ production cross-sections (in fb) and yields from SPS, DPS (for $\sigma_{\text {eff,DPS }}=2.7 \mathrm{mb}$ ) and TPS (for $\sigma_{\text {eff,TPS }}=0.82 \times \sigma_{\text {eff,DPS }}=2.2 \mathrm{mb}$ ) processes, and their total sum. The values are given in columns for combinations of $n$ prompt and (3-n) non-prompt-J/ $\psi$ mesons, the last column giving their corresponding sums. The DPS and TPS results are derived via equations (3)-(5) from the SPS cross-sections listed in Table 2 with $\sigma_{\text {eff,DPs }}$ chosen so that the sum of contributions yields a total cross-section equal to the experimental value of $\sigma_{\text {tot }}^{3 / \psi}$. The expected yield, $N_{\mathrm{NPS}}^{3 / \psi}$, is given for an effective integrated luminosity of $\epsilon \mathcal{L}_{\mathrm{int}}=87 \mathrm{fb}^{-1}$ for each contributing process. The last column lists the total cross-sections and yields for SPS, DPS, TPS and their sums.
production is a golden channel to study DPS and TPS, with minimal SPS contamination. The largest contributors to the triple- $/ / \psi$ cross-section are $\sigma_{\text {DPS }}^{3 \mathrm{np}}$ and $\sigma_{\text {DPS }}^{1 \mathrm{p} 2 \mathrm{np}}$, accounting for about $33 \%$ each, $\sigma_{\text {TPS }}^{2 \mathrm{p} 1 \mathrm{np}}$ and $\sigma_{\text {TPS }}^{1 \mathrm{p} 2 \mathrm{np}}$ amounting to about $7 \%$ each, and $\sigma_{\text {SPS }}^{3 \mathrm{np}}$ representing about $4 \%$ of the total production. In terms of prompt and non-prompt contributions, the theoretical expectation for the production of three promptly produced $J / \psi$ mesons is about $5 \%$ of the total yield, whereas the percentage expected for three non-prompt $-J / \psi$ mesons is about $45 \%$. The remaining half of the triple $-J / \psi$ events are expected to be due to the combination of $J / \psi$ mesons produced promptly and from beauty hadron decays. This result is consistent, within the large statistical uncertainties of the present dataset, with the combination of prompt and non-prompt- $J / \psi$ mesons derived from the decay length of each dimuon candidate.

In Fig. 3, the $\sigma_{\text {eff,Dps }}$ value extracted here (red circle) is compared with the world data on effective DPS cross-sections derived from midrapidity measurements with quarkonium final states ${ }^{22,22,24,24-26,50}$ (blue symbols), as well as from processes with jets, photons and/or $W$ bosons ${ }^{13-19,51-56}$ (black symbols). A few of the $\sigma_{\text {eff.,DPs }}$ values plotted have been derived by more advanced phenomenological studies ${ }^{57-60}$ of the experimental quarkonium data. The effective cross-sections obtained from quarkonium measurements favour a smaller value of $\sigma_{\text {eff,DPs }} \approx 3-10 \mathrm{mb}$ compared with the $\sigma_{\text {eff.,Ds }} \approx 10-20 \mathrm{mb}$ derived from harder or heavier final states. Such an apparent process-dependent $\sigma_{\text {eff.DPs }}$ value is suggestive of different parton transverse profiles, and/or correlations present, probed inside the proton at varying fractional momenta, given by $x=\sqrt{p_{\mathrm{T}, V}^{2}+m_{V}^{2}} \mathrm{e}^{\eta} / \sqrt{s}$, for $V=J / \psi, r, W, Z$. At midrapidity $(|\eta|<2.5)$, quarkonia are produced mostly in gluon-gluon scatterings carrying a fraction $x \approx 5 \times 10^{-4}$ of the proton momentum, whereas mostly quarks


Fig. $3 \mid$ Comparison of $\sigma_{\text {eff,DPs }}$ parameters extracted in various processes.
The result obtained here (top red circle) is compared with those derived in midrapidity measurements of double-quarkonium and electroweak-boson-plus-quarkonium production ${ }^{22,24,25,57-60}$ (blue symbols), as well as in final states with jets ${ }^{19,51,52,62}, \gamma+$ jets $^{53-56}, W+$ jets ${ }^{13,14}$ and same-sign $W$ bosons ${ }^{18}$ (black symbols). The arrows indicate lower (or upper) limits at $95 \%$ (68\%) confidence level. For the experimental results marked with a star, more recent theoretical reinterpretations based on more accurate calculations of the corresponding SPS cross-section are plotted. The original experimental results can be found in ref. ${ }^{23}$ (CMS), ref. ${ }^{26}$ (D0) and refs. ${ }^{50,63}$ (ATLAS).
with $x \approx 10^{-2}$ participate in the production of electroweak bosons. The fact that LHCb measurements of double-quarkonia and quarkonia-plus-charm ${ }^{25,61}$ at forward rapidities ( $\eta \approx 2-4.5$ ), processes that originate in parton scatterings with asymmetric fractional momenta $x_{1} \approx 10^{-4}$ and $x_{2} \approx 10^{-2}$, lead to values of $\sigma_{\text {eff.,DPs }} \approx 15 \mathrm{mb}$, larger than those measured at midrapidity for similar final states, seems to confirm the dependence of the effective DPS cross-section on the relevant parton species and $x$ fractions probed.

## Online content

Any methods, additional references, Nature Portfolio reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at https://doi.org/10.1038/s41567-022-01838-y.

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CERN 2023, for the benefit of the CMS Collaboration 2023

## The CMS Collaboration

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## Methods

## Experimental set-up

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter, and a brass and scintillator hadron calorimeter, each composed of a barrel and two endcap sections. Forward calorimeters extend the $\eta$ coverage provided by the barrel and endcap detectors. Muons are measured over the range $|\eta|<2.4$ in gas-ionization detectors, embedded in the steel flux-return yoke outside the solenoid, made using three technologies: drift tubes, cathode strip chambers and resistive plate chambers. A more detailed description of the CMS detector can be found in ref. ${ }^{64}$.

Events of interest are selected using a two-tiered trigger system. The first trigger level, composed of custom hardware processors, uses information from the calorimeters and muon detectors to select events at a rate of around 100 kHz with a fixed latency of about $4 \mu \mathrm{~s}\left(\mathrm{ref} .{ }^{65}\right)$. The second level (or high-level trigger, HLT) consists of a farm of processors running a version of the full event reconstruction software optimized for fast processing, and reduces the event rate to around 1 kHz before data storage ${ }^{66}$. The present analysis employs an HLT that requires three muons, each having $p_{\mathrm{T}}>3.5 \mathrm{GeV}$ for $|\eta|<1.2$ (barrel) or $p_{\mathrm{T}}>2.5 \mathrm{GeV}$ for $1.2<|\eta|<2.4$ (endcap). In addition, the event must have at least one pair of oppositely charged muons with invariant mass between 2.80 GeV and 3.35 GeV that originate from a common vertex with a probability greater than $0.5 \%$, as determined by a Kalman vertex fit ${ }^{67}$, thus suppressing random combinations of muons from unrelated sources. MC simulations are used to determine the trigger efficiency. Simulated events are generated using HELAC-Onia (v.2.6.6) with the NNPDF3.0 PDF set ${ }^{68}$, and Pythia 8.205 for the hadronization and decay with the CUETP8M1 underlying event tune ${ }^{62}$. Triple- $/ / \psi$ events are simulated by combining events from two different MC samples with varying relative fractions. The first MC sample contains three singly produced $J / \psi$ mesons, whereas the second sample combines single- and double- $/ / \psi$ meson production, following ref. ${ }^{28}$. As the $J / \psi$ mesons originating in both processes have slightly different $p_{\mathrm{T}}$ spectra, the variation of their relative fractions in the simulation allows to effectively scan the triple-muon trigger efficiency in the more uncertain region close to the trigger $p_{\mathrm{T}}$ thresholds. The generated events are then processed through a detailed Geant 4 simulation ${ }^{69}$ of the CMS detector response.

## Event reconstruction and selection

Muons are reconstructed by combining information from the silicon tracker and the muon system ${ }^{39}$. The matching between tracks reconstructed in each of the subsystems proceeds either outside-in, starting from a track in the muon system, or inside-out, starting from a track provided by the silicon tracker. Matching muons to tracks measured in the silicon tracker leads to a relative $p_{\mathrm{T}}$ resolution of $1 \%$ in the barrel and $3 \%$ in the endcaps for muons with $p_{\mathrm{T}}$ up to 100 GeV (ref. ${ }^{39}$ ). The candidate vertex with the largest value of summed physics-object $p_{\mathrm{T}}{ }^{2}$ in the event is taken to be the $\mathrm{PV}^{70}$. Only charged particles that are either directly participating in the PV determination, or are closest to the PV along the $z$ direction and not used in any other PV identification (namely, they are consistent with secondary decays from the closest PV), are used in the analysis. Simulation studies show that this procedure efficiently suppresses any potential contamination from charged particles produced in any other pp collision taking place in the same bunch crossing (pile-up).

The offline data analysis starts by selecting events with six or more reconstructed muons, each passing the $p_{\mathrm{T}}$ and $\eta$ criteria implemented at the HLT. The muons are combined into OS pairs, and are considered for further study if their invariant mass is $2.9 \mathrm{GeV}<m_{\mu^{+} \mu^{-}}<3.3 \mathrm{GeV}$ (corresponding to about $\pm 7$ times the $J / \psi$ mass resolution discussed below) and originate from a common vertex with a probability greater than $0.5 \%$, thereby reducing the random pairing of muons originating
from other background sources in the same event, as discussed below. All selected muon pairs are further required to share the same PV (including the possibility that they originate from secondary vertices associated to a common PV) to eliminate accidental combinations of muons from different pp collisions in the same or neighbouring bunch crossings. The analysis thereby includes prompt- $J / \psi$ mesons coming directly from the pp interaction (or from feed-down decays of promptly produced and decayed resonances), and non-prompt ones coming from the decays of beauty hadrons. To ensure high purity and reconstruction efficiency, the $J / \psi$ candidates are required to have $p_{\mathrm{T}}>6 \mathrm{GeV}$ and $|y|<2.4$.

After applying the selection criteria discussed above, six triple-J/ $\psi$ events are observed. No alternative pairings among the OS muons in these six events are found to satisfy the analysis requirements. In all events, the $J / \psi$ meson with highest $p_{\mathrm{T}}$ ('leading' $J / \psi$ ) is found to correspond to the muon pair that passed the online trigger selection. In inclusive $J / \psi$ measurements ${ }^{23,32-35}$, a continuum background is present in the $m_{\mu+\mu^{-}}$distribution due to random combinations of OS muons originating from semileptonic beauty- and charm-quark hadron decays, $b \rightarrow \mu+X$ and $c \rightarrow \mu+X$, and Drell-Yan events, which pass the trigger and data analysis criteria. To monitor the sideband background population, the mass windows corresponding to the two subleading $/ / \psi$ mesons are extended well below the $/ / \psi$ mass region. The corresponding dimuon invariant mass distributions are shown in Fig. 2 ordered (left to right) by decreasing $p_{\mathrm{T}}$ of the $\mu^{+} \mu^{-}$system. Only one additional background event is found in the extended mass region indicated by the dotted curves, confirming that the combinatorial continuum is suppressed by the requirement of having three reconstructed $J / \psi$ candidates in the same event.

## Event kinematic properties

Detailed information of the kinematic properties of the $J / \psi$ candidates passing the triple $-J / \psi$ selection criteria are shown in Extended Data Table 1. The kinematic distributions of all six $J / \psi$ triplets do not show any local peak, which could be indicative of, for example, a resonance decaying into three $J / \psi$ mesons, but are distributed featureless (with large point-to-point statistical uncertainties) over triple- $J / \psi$ mass, $p_{\mathrm{T}}$ and $\eta$.

All sources of systematic uncertainty in the triple- $/ / \psi$ cross-section measurement are listed in Extended Data Table 2.

## Data availability

Tabulated results are provided in the HEPData record for this analysis ${ }^{71}$. Release and preservation of data used by the CMS Collaboration as the basis for publications is guided by the CMS policy as stated in CMS data preservation, re-use and open access policy.

## Code availability

The CMS core software is publically available at https://github.com/ cms-sw/cmssw.

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## Author contributions

All authors have contributed to the publication, being variously involved in the design and the construction of the detectors, in writing software, calibrating subsystems, operating the detectors and acquiring data, and finally analysing the processed data. The CMS Collaboration members discussed and approved the scientific results. The manuscript was prepared by a subgroup of authors appointed by the collaboration and subject to an internal collaboration-wide review process. All authors reviewed and approved the final version of the manuscript.

## Competing interests

The author declare no competing interests.

## Additional information

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Extended Data Table 1 | Properties of $J / \Psi$ candidates measured in thetriple- $J / \Psi$ events. Dimuon invariant mass, proper decay length, transverse momentum, rapidity, and azimuthal angle of each of the three $J / \Psi$ candidates measured in the six triple- $J / \psi$ events passing our selection criteria. (The last $J / \psi$ candidate in the last row, with invariant mass $m^{J / \psi, 3}=2.94 \mathrm{GeV}$, is likely a background event)

| Event | $m^{\mathrm{J} / 4,1}(\mathrm{GeV})$ | $m^{J / 4,2}(\mathrm{GeV})$ | $m^{J / 4,3}(\mathrm{GeV})$ | $L^{\mathrm{J} / 4,1}(\mathrm{~mm})$ | $L^{\mathrm{J} / 4,2}(\mathrm{~mm})$ | $L^{\mathrm{J} / 4,3}(\mathrm{~mm})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 3.08 | 3.10 | 3.07 | 1.77 | 0.24 | -0.01 |
| 2 | 3.15 | 3.06 | 3.09 | 0.05 | 0.36 | 0.02 |
| 3 | 3.10 | 3.14 | 3.11 | -0.04 | 0.03 | 0.05 |
| 4 | 3.07 | 3.03 | 3.09 | 0.48 | 0.81 | 0.82 |
| 5 | 3.12 | 3.14 | 3.14 | -0.25 | 0.13 | -0.02 |
| 6 | 3.06 | 3.17 | 2.94 | 0.11 | 0.38 | 0.61 |
| Event | $p_{\mathrm{T}}^{\mathrm{J} / 4,1}(\mathrm{GeV})$ | $p_{\mathrm{T}}^{\mathrm{J} / 4,2}(\mathrm{GeV})$ | $p_{T}^{\mathrm{J} / 4,3}(\mathrm{GeV})$ | $y^{\text {J/4.1 }}$ | $y^{J / 4.2}$ | $y^{J / 4,3}$ |
| 1 | 17.64 | 17.50 | 8.68 | -2.25 | -0.39 | 1.53 |
| 2 | 91.50 | 54.04 | 11.81 | 1.99 | 0.81 | -0.71 |
| 3 | 11.29 | 10.29 | 6.98 | -0.50 | -0.37 | -1.64 |
| 4 | 15.46 | 10.61 | 7.84 | -0.83 | -2.24 | -1.78 |
| 5 | 8.67 | 7.71 | 6.75 | 2.03 | -1.14 | -1.87 |
| 6 | 60.70 | 19.09 | 17.03 | 1.59 | 2.29 | 1.58 |
| Event | $\phi^{J / 4,1}$ | $\phi^{J / 4,2}$ | $\phi^{\mathrm{J} / 4,3}$ |  |  |  |
| 1 | -1.98 | 2.06 | -1.56 |  |  |  |
| 2 | 2.60 | -2.14 | -0.38 |  |  |  |
| 3 | -0.87 | -1.50 | 0.66 |  |  |  |
| 4 | 1.00 | -2.07 | -1.77 |  |  |  |
| 5 | -1.77 | 1.99 | 2.91 |  |  |  |
| 6 | -1.98 | -1.74 | -2.17 |  |  |  |

Extended Data Table 2 | Systematic uncertainty contribution. Relative contributions to the systematic uncertainty of the $\mathrm{pp} \rightarrow \mathrm{J} / \Psi \mathrm{J} / \Psi \mathrm{J} / \Psi \mathrm{X})$ measurement. The last row gives the sum in quadrature of all components

| Source | Relative uncertainty |
| :--- | :--- |
| J/ meson signal shape | $0.8 \%$ |
| Dimuon continuum background shape | $3.4 \%$ |
| Muon reconstruction and identification | $1.0 \%$ |
| Trigger efficiency | $3.4 \%$ |
| MC sample size | $3.0 \%$ |
| Integrated luminosity | $1.6 \%$ |
| Dimuon branching fraction | $1.7 \%$ |
| Total | $6.2 \%$ |


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