LIMIT ON $\bar{\nu}_e$ MASS FROM FREE MOLECULAR TRITIUM BETA DECAY

T. J. Bowles, J. C. Browne, J. A. Helffrich, D. A. Knapp[a], M. P. Maley,
R. G. H. Robertson, J. S. Cohen, R. L. Martin, J. F. Wilkerson
(Presented by Thomas J. Bowles)
Los Alamos National Laboratory,
Los Alamos, New Mexico 87545

The beta spectrum of free molecular tritium has been measured in order to
search for a finite electron antineutrino mass. The final-state effects in
molecular tritium are accurately known and the data thus yield an essentially
model-independent upper limit of 27 eV on the $\bar{\nu}_e$ mass at the 95% confidence
level. This limit is dominated by the statistics obtained in the data sets.
Optimization of the experimental apparatus is underway and an ultimate
sensitivity of 10 eV is expected.

The possibility that neutrino masses are nonzero has received considerable attention since Lyubimov et al.[1] in 1981 reported evidence for a finite electron antineutrino mass, currently fixed[2] between 17 and 40 eV, with a best-fit value of 30 eV. On the other hand, Fritschi et al.[3], also studying the beta decay of tritium, have reported an upper limit of 18 eV on the neutrino mass. Since the statistical evidence to support both claims is very strong, the difference between the two results must be due to systematic problems. These problems likely originate in the use of complex source materials in which the energy given up in molecular excitations following the beta decay of a tritium atom is comparable to the size of the neutrino mass in question. These final-state effects are difficult to calculate for a molecule as complex as valine[1] or for tritium implanted in carbon[3]. In addition, energy loss and backscattering of the betas in traversing the solid source are appreciable and must be very accurately accounted for. These considerations have led us to develop an experiment using free molecular tritium as the source material. The final-state effects have been accurately calculated[4,5] for the tritium molecule, and the uncertainties[5] in these calculations are at the level of approximately 1 eV. In addition, the energy loss in the source is small because the source consists of tritium only and there is no backscattering.

The experimental apparatus has been described in detail elsewhere[6] and will only be briefly described here. Molecular tritium enters a 3.7-m long, 3.8-cm inner diameter aluminum tube at the midpoint and is pumped away at the ends and recirculated. The tube is held at approximately 160 K to increase the source strength and is uniformly biased to typically -8 kV. The source tube is inside a superconducting solenoid so that betas from the decay of tritium spiral along the field lines without scattering from the tube walls. The equilibrium density of tritium in the source integrated along the axis is 6.9×10^{15} tritium molecules/cm^2. Electrons (that are not trapped in local field minima) pass through an average thickness 2.7 times that value as they spiral through the source gas. At one end, they are reflected by a magnetic pinch and at the other end are accelerated to ground potential. A hot filament located at the pinch emits thermal electrons that neutralize the space charge of positive ions trapped in the source. The betas are transported through a pumping restriction where the tritium is differentially pumped away and then are focused by nonadiabatic transport through a rapidly falling magnetic field to form an image on a 1-cm diameter collimator at the entrance to the spectrometer. The collimator defines an acceptance radius in the source tube such that decays originating more than 8.4 mm from the axis are not viewed by the spectrometer. A Si detector is located at a position in front of the

collimator where it intercepts a small fraction of the betas from decays in the source tube and serves to normalize the source strength. The spectrometer is a 5-m focal-length toroidal beta spectrometer similar in concept to the Tretyakov instrument[7], but with a number of modifications[6]. Betas from a 2.2-cm^2 area in the source tube are transmitted with about 1% net efficiency through the entrance collimator to a position sensitive proportional counter at the focus of the spectrometer. The detector is 2 cm in diameter with a 2-mm-wide entrance slit. The energy resolution for 26-keV electrons is 20% and the position resolution 6 mm FWHM (position information is used to reject backgrounds outside the slit acceptance). The earth's magnetic field is canceled to a level of <10 mG in the spectrometer volume by external coils. The effective integral event rate in the last 100 eV was typically 0.12 counts/sec.

The beta spectrum is scanned by changing the voltage applied to the source tube so that betas of constant energy are analyzed by the spectrometer. Accelerating the betas not only improves the emittance of the source but also raises the energy of betas of interest well above backgrounds from decay of tritium elsewhere in the pumping restriction or spectrometer. The beta monitor is biased at the same voltage as the source tube.

To determine the instrumental resolution, ^{83m}Kr is introduced into the source tube in the same manner as tritium. The krypton emanates from a mixed Na-Rb stearate[8] containing 5 mCi of ^{83}Rb, and produces a 17.835(20)-keV K-conversion line. The intrinsic lineshape is a 2.26-eV-wide Lorentzian[9]. The dominant shakeup satellite is located 20 eV below with an intensity of 8.2% of the total, as estimated by scaling the measurements of Spears et al.[10] according to the calculations of Carlson and Nestor[11]. The same calculations were used to assign intensities to shakeoff satellites. The spectral distribution of shakeoff was taken to have the 2p Levinger form[12]. The spectral contribution from scattering of the conversion electrons by nitrogen molecules in the source gas (which accumulate during recirculation of the krypton) has been calculated from experimental data[13] and has been removed from the resolution function by fitting the amount of nitrogen. The fitted contributions, 10 to 15%, were proportional to measured source pressures. The spectrometer response itself is well described by a skewed Gaussian convoluted with a rectangular slit-width contribution. The total resolution function is obtained by convoluting the instrumental contribution with the energy-loss spectrum of scattering in the tritium gas, calculated by Monte Carlo methods from the known doubly differential cross sections[14] for electron scattering from H$_2$. Some of the electrons, 11.7(10)%, are trapped in the source by local field minima and must multiply scatter in order to escape, and 6.5(14)% of the

untrapped electrons suffer a single interaction in the gas before being extracted.
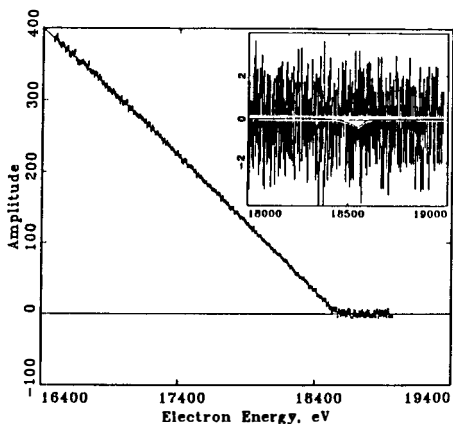

Fig. 1. Kurie plot for run 4A. Inset: Residuals (in standard deviations) for all data. The straight and curved lines are, respectively, the best fits for $m_\nu = 0$ and 30 eV.
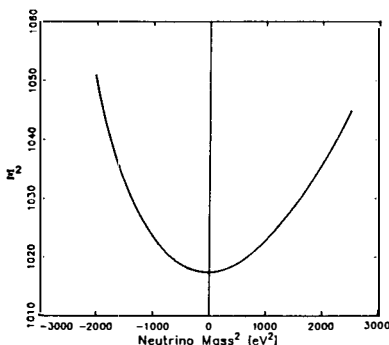
Fig. 2. Combined Ξ^2 plot for the data. At the minimum, Ξ^2 has the value for 1015 for 984 degrees of freedom.

Measurements of backgrounds from the source and tritium contamination of the spectrometer reveal no backgrounds originating from the source walls or extraction region, nor any increase in spectrometer background after operation of the source and spectrometer with tritium for more than one month. The background rate has remained steady at approximately 1 count/200 sec and is primarily from cosmic rays.

Four data sets were taken, each of 3-4 days duration, with operating conditions given in Table I. In total, 3.8×10^6 events were recorded. All but the third run were taken with the spectrometer set to analyze 26.0-keV betas. The beta spectrum was scanned from 16.44 to 18.94 keV in 10-eV steps. Two randomly selected data points were taken for 600 seconds each, followed by a 200-second run at 16.44 keV in order to monitor time-dependent effects. The third data set was taken in a similar manner, except that the spectrometer was set to analyze 26.5-keV betas in order to check for systematic effects in varying the extraction voltage (and therefore the extraction efficiency). Extra data points were taken in 5-eV steps near the endpoint in the third run. The fourth data set was recorded event by event, at randomly chosen energies for 55 seconds, and at the 16.44-keV calibration energy for 110 seconds every 10 minutes.

To analyze the data, a predicted beta spectrum was generated that includes the molecular final states[4], screening corrections, nuclear-recoil

effects, weak magnetism, and acceleration-gap effects (the last three are negligible). In the customary notation,

$$N(E) = C \, F(Z,R,E) \, p_e \, E \, \Sigma_i w_i (E_0 - E_i - E)[(E_0 - E_i - E)^2 - m_\nu^2 c^4]^{1/2}$$

$$\times \, [1 + \alpha_1(E_0 - E) + \alpha_2(E_0 - E)^2] \quad ; \quad E \le E_0 - E_i - m_\nu c^2$$

Weak magnetism and nuclear recoil give[15] a_1 a value of 2.312×10^{-9} eV^{-1}. The total resolution, including energy loss in the source, was folded with the calculated spectrum. A five-parameter fit to the amplitude, endpoint energy, neutrino mass, background level, and the quadratic extraction-efficiency term[16] α_2 in a maximum-likelihood procedure with Poisson statistics was then performed. The resulting fit (Fig. 1) is characterized by a Ξ^2 parameter[17], analogous to the usual χ^2 parameter:

$$\Xi^2 = 2\Sigma \, [s_i - y_i - y_i \ell n(s_i/y_i)] \quad ,$$

where s_i and y_i are the fit value and the measured value, respectively. (χ^2 minimization gives a biased estimate of areas, and results in an incorrectly fitted neutrino mass.) Because each point is renormalized for pressure variations in the source, this estimator was corrected by a factor y_i/σ_i^2, where σ_i^2 is the variance in y_i. This factor, unity when the number of counts is small, ranged from 0.2 to 0.8 at the low-energy end of the spectra. Dead-time corrections were necessary only in the beta-monitor data, as count rates in the spectrometer did not exceed 30 s^{-1}. Extensive Monte-Carlo calculations were carried out to verify the unbiased character of the fit estimator[6].

TABLE I. Summary of parameters and results from fitting procedure. Uncertainties are 1 standard deviation.

Run	Ξ^2	Data Points	E_0 (eV)	Resolution (FWHM, eV)	Skewness	α_2 (10^{-8}eV^{-2})	Last 100 eV Counts	Background	m_ν^2(eV^2)[a]
3	273	254	18585.1(34)	55.6(12)	-0.123(14)	-1.32(19)	170	36	-805(926,85)
4A	209	250	18585.5(43)	36.0(13)	0.150(16)	-1.88(21)	93	28	2049(1795,156)
4B	230	220	18577.4(39)	36.2(15)	0.164(15)	-0.77(40)	273	53	-84(724,84)
4C	303	280	18582.9(29)	36.1(9)	0.150(16)	-0.23(15)	113	24	120(811,22)
All	1015	1004	18582.8(18)				649	141	-57(453,118)

[a]Uncertainties are: (Statistical, Resolution). In this paper, the uncertainty in the last digit is placed in parenthesis; e.g. 18585.1(34) means 18585.1 + 3.4.

In Table I we summarize run parameters and fit results. The indicated uncertainty in the endpoint energy does not include the additional 20-eV

uncertainty in the energy[18] of the ^{83m}Kr calibration line. The change in resolution between the data sets resulted mainly from improved cancellation of residual magnetic fields from the source magnets in the region of the spectrometer. The quadratic correction term varies from run to run owing both to changes in focus-coil setting and, in runs 4B and 4C, to normalization of the source intensity by interpolation between calibration points rather than by the Si detector, which had become excessively contaminated. A linear term was tried in place of the quadratic term, and gave similar results, but with slightly lower neutrino mass limits. No nonstatistical variations were observed with either a (fixed) quadratic or linear term when the fitting interval below the endpoint was varied over the range 2200 to 300 eV. Statistical tests showed that inclusion of both linear and quadratic terms was not warranted.

Statistical errors in m_ν^2 were extracted from the Ξ^2 plots [which were closely parabolic in positive m_ν^2 (Fig.2)]. Resolution-function uncertainties in each run were then added in quadrature to the statistical error. To guard against the possibility of a correlated error, the average resolution error (87 eV^2) was also combined with the error in the final result, as were uncertainties from the measurement of the density of the source gas and the Monte-Carlo simulation of multiple scattering (80 eV^2). Changes of 10% in the Kr shakeup and shakeoff intensities produced effects less than 1% of the final statistical error. These were the only uncertainties considered to be non-negligible.

The uncertainty in the final result is predominantly statistical. An upper limit on the mass of the electron antineutrino is found to be 26.8 eV at the 95% confidence level (C.L.) or 23.3 eV at the 90% C.L. It does not support the central value reported by Lyubimov[2], 30(2) eV, but neither does it exclude the lower part of the range 17 to 40 eV. It is compatible with the upper limits from solid-source experiments by Fritschi et al.[3] and Kawakami et al.[19]. The present result is, for all practical purposes, model independent, and thus establishes the maximum mass the electron antineutrino can have.

The ultimate sensitivity of the experiment will be determined primarily by the statistics and background which can be achieved, as the systematic effects are small. In fact, the uncertainty in our current result due to statistics is four times larger than the systematic uncertainty. Given infinite statistics, systematic uncertainties would limit our present sensitivity to about 11 eV. We have recently substantially reduced the effects which produced the major systematic uncertainties. This was done by installing a monotonic gradient field along the source, thus eliminating any trapping of

betas in the source. As a result, the single scattering probability is reduced since the betas now have a shorter path length as they spiral out of the source, and the multiple scattering is essentially eliminated. Secondly, we have installed a getter pump in the vacuum system which operates while we are making krypton resolution measurements. This eliminates the buildup of (and subsequent energy loss in) residual gases in the krypton measurements. With these effects eliminated, the major remaining systematic uncertainty in the experiment is due to the width of the total spectrometer resolution function (including tails due to energy loss). Although our spectrometer resolution was modest (36 eV) during our present runs, we expect to improve it to better than 30 eV in future runs. In our experiment, the uncertainty in determining the total spectrometer resolution is less than in the experiments using solid sources, because although our FWHM is somewhat worse, the tail on the resolution function is substantially smaller with our gaseous source than with solid sources. Thus, the sensitivity limit due to systematic effects in our experiment is expected to be at the level of a few eV.

We are presently working to improve our statistical accuracy and to reduce the backgrounds. This will be accomplished primarily by replacing the single wire proportional counter which has a 2 mm wide entrance slit with a 96 channel annular silicon strip detector. This detector has eight pads mounted on a 2 cm diameter cylinder. Each pad has twelve silicon strip detectors which are 0.83 mm wide, with a total width of 1.0 cm. This allows us to increase the acceptance of the focal plane detector by a factor of five, while simultaneously reducing the contribution of the slit width to the spectrometer resolution. The detector is expected to have better energy resolution than the present proportional counter (10% vs 20%), which will not only reduce the background, but will also allow us to operate the source at a lower accelerating potential while still eliminating backgrounds from any tritium contamination in the spectrometer and pumping restriction. This will result in improved spectrometer resolution, since the resolution scales as the total energy of the particles being analyzed. In addition, we will be able to reject any through going particles (such as muons, and electrons from converted gamma rays), which will further reduce our backgrounds. We have also realigned the spectrometer, which we expect will result in increased acceptance. Finally, we have now completed Monte Carlo calculations optimizing the counting time spent at each point in the spectrum, with the result that we can achieve the same statistical accuracy on the neutrino mass in one fourth the time compared to our present method of spending equal time at each point. Combining these factors, we expect to reduce the background by at least a factor of two and to increase our effective counting rate by at least a factor of twenty. This will

allow to search for a neutrino mass with 10 eV sensitivity in a model independent manner.

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[a] Present address: Lawrence Livermore National Laboratory, Livermore, CA 94550.

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