

# **Analysis of the Radiation Tolerance of the LHC-B Silicon Vertex Detector**

H. Feick

ROSE/CERN - RD48 Collaboration

II. Institut für Experimentalphysik, Universität Hamburg,  
Luruper Chaussee 149, 22761 Hamburg, Germany

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This note analyses the radiation tolerance of the LHC-B silicon vertex detector in the framework of the latest damage models put forward by the ROSE / CERN RD 48 Collaboration. The calculations assume constant temperature and constant flux for a one year beam period of 240 d. It is found that the ultimate failure of the detectors is due to the damage-induced doping changes causing the loss of sensitive volume. Increases in the leakage current and carrier trapping stay at a tolerable level. Given a suitable operating temperature (5°C) and initial resistivity, detectors of 150  $\mu\text{m}$  (480  $\Omega\text{cm}$ ) and 200  $\mu\text{m}$  (850  $\Omega\text{cm}$ ) thickness are expected to remain fully depleted with 200 V up to equivalent 1-MeV neutron fluences of  $5 \times 10^{14} \text{ cm}^{-2}$  and  $9 \times 10^{14} \text{ cm}^{-2}$ , respectively. Admitting partially depleted operation, the lower benchmark figure of 7000 collected electrons is reached at radiation doses as high as  $8 \times 10^{14} \text{ cm}^{-2}$  and  $1 \times 10^{15} \text{ cm}^{-2}$ , respectively. A conservative 50% error in the quoted values is due to the uncertainty in the experimentally determined constants of the damage models.

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This note analyses the radiation tolerance of the LHC-B silicon vertex detector in the framework of the latest damage models put forward by the ROSE / CERN RD 48 Collaboration. The calculations assume constant temperature and constant flux for a one year beam period of 240 d. It is found that the ultimate failure of the detectors is due to the damage-induced doping changes causing the loss of sensitive volume. Increases in the leakage current and carrier trapping stay at a tolerable level. Given a suitable operating temperature (5°C) and initial resistivity, detectors of 150  $\mu\text{m}$  (480  $\Omega\text{cm}$ ) and 200  $\mu\text{m}$  (850  $\Omega\text{cm}$ ) thickness are expected to remain fully depleted with 200 V up to equivalent 1-MeV neutron fluences of  $5 \times 10^{14} \text{ cm}^{-2}$  and  $9 \times 10^{14} \text{ cm}^{-2}$ , respectively. Admitting partially depleted operation, the lower benchmark figure of 7000 collected electrons is reached at radiation doses as high as  $8 \times 10^{14} \text{ cm}^{-2}$  and  $1 \times 10^{15} \text{ cm}^{-2}$ , respectively. A conservative 50% error in the quoted values is due to the uncertainty in the experimentally determined constants of the damage models.

## 1. Introduction

The LHC-B experiment will be running at a luminosity of  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$  resulting in an annual equivalent 1-MeV neutron fluence of about  $1 \times 10^{14} \text{ cm}^{-2}$  at the innermost radius (1 cm) of the silicon vertex detector [1]. For safety reasons it is also worthwhile considering higher doses as additional radiation might be generated, e.g. by a lost beam. It is well known that at such radiation levels a serious deterioration of the silicon detectors must be envisaged, see e.g. [2]. The LHC-B Collaboration has well recognized this situation and gave a first estimate of the tracker performance degradation in ref. [3]. In this note we give a detailed description of the damage-induced changes in the doping concentration, leakage current, and charge collection based on the expertise of the ROSE Collaboration [4]. In particular we will highlight the implications of the material used for the manufacture of the detectors and the temperature maintained during their operation. At this point we also include our latest findings reported in ref. [5]. Still it was necessary to further refine the models as a) freezing of the beneficial annealing in the doping changes and b) charge collection at arbitrary fields had so far not been treated in enough detail, however, these issues turn out to be important for LHC-B. These and other more technical aspects are detailed in the Appendix. The bulk of the paper consists of the application of the damage models to the particular operating conditions met at LHC-B (Sect. 3.), the presentation of the results (Sect. 4.), and the discussion of the errors and weaknesses in the approach used (Sect. 5.).

## 2. Detector Parameters and Operational Conditions

A parameter of paramount importance for the operation of silicon detectors is the full depletion voltage  $V_{dep}$ . For our purposes it is sufficient to approximate  $V_{dep}$  by the expression

$$V_{dep} = |N_{eff}| d^2 q_0 / 2 e e_0. \quad (1)$$

It is evident that even for large absolute values of the effective doping concentration  $|N_{eff}|$  (e.g. brought about by radiation damage) a reasonably low  $V_{dep}$  can be obtained if the detector thickness  $d$  is made sufficiently small. In this report we consider either  $d = 200 \mu\text{m}$ , which is a quite optimistic figure for a wafer to be processed with standard equipment, or  $d = 150 \mu\text{m}$ , clearly being a challenge for the detector supplier due to the resulting mechanical instability. A small thickness also aids reducing the radiation length, however, it compromises the number of electron-hole pairs generated in the detector by a traversing particle. Detectors are assumed to be manufactured on comparatively low resistivity n-type silicon, suitable to counteract the damage-induced negative space charge [5]. As the operational voltage  $V_{op}$  is assumed in this note to be fixed to 200 V, we specified an initial depletion voltage  $V_{dep0}$  of 150 V for either thickness. The corresponding initial doping concentration  $N_{eff0}$ , compare eq. (1), and initial resistivity  $r \approx (q_0 m_i N_{eff0})^{-1}$  is listed in Table 1. Initial leakage currents are regarded as negligible compared with the damage-induced bulk generation current. For purpose of clarity all currents in this note are given normalized to area. In order to determine the current in a particular channel, the actual segmentation of the LHC-B vertex detectors has to be taken into account which is left to the interested reader.

$d$	$V_{dep0}$	$N_{eff0}$	$r(20^\circ\text{C})^a$
150 $\mu\text{m}$	150 V	$8.8 \times 10^{12} \text{ cm}^{-3}$	480 $\Omega\text{cm}$
200 $\mu\text{m}$	150 V	$4.9 \times 10^{12} \text{ cm}^{-3}$	850 $\Omega\text{cm}$

<sup>a)</sup> using  $m_i = 1480 \text{ cm}^2/\text{Vs}$

Table 1. The two alternative sets of detector parameters studied.

The analysis given in the following sections assumes a  $t_{exp} = 240 \text{ d}$  lasting operation at a constant average particle flux  $f_{eq} = F_{eq} / t_{exp}$ .  $F_{eq}$  denotes the equivalent 1-MeV neutron fluence absorbed in that time. Also the operating temperature  $T_{op}$  is assumed to be a constant. Results will be presented for values of  $F_{eq}$  and  $T_{op}$  ranging between  $2 \dots 8 \times 10^{14} \text{ cm}^{-2}$  and  $-10 \dots 25^\circ\text{C}$ , respectively.

## 3. Modeling Bulk Damage Effects at LHC-B

In this section the equations describing the macroscopic damage effects for constant flux and constant temperature operation are just written down without derivation from the basics. For a more detailed introduction into the physics behind the damage models see for example [6].

### Doping Changes

In general the damage-induced change in the doping concentration  $\Delta N_{eff} = N_{eff0} - N_{eff}$  can be split into three parts

$$DN_{eff} = N_a + N_c + N_Y. \quad (2)$$

They account for the fractions exhibiting short term (beneficial) annealing ( $N_a$ ), no annealing ( $N_c$ ), and long term (reverse and/or anti) annealing ( $N_Y$ ). Here we will presuppose that the first component can be visualized as to arise from a single acceptor introduced per volume at the rate  $g_a \mathbf{f}_{eq}$  and decaying at the rate  $k_a$ , for details see Appendix A. The solution of the appropriate differential equation under the given operational conditions writes

$$N_a(t) = g_a \mathbf{f}_{eq} [1 - \exp(-k_a t)] / k_a, \quad (3)$$

where  $t$  is the time elapsed since the beam was switched on. As the stable damage component  $N_c$  does not exhibit annealing it is only implicitly depending on time via the accumulated fluence  $\mathbf{f}_{eq} t$ :

$$N_c(t) = N_{c0}(1 - \exp(-c \mathbf{f}_{eq} t)) + g_c \mathbf{f}_{eq} t. \quad (4)$$

Again, an acceptor introduced with the damage rate  $g_c$  can be thought of to be the origin of the term on the right-hand side of eq. (4). Conversely, the term on the left-hand side is considered to be due to the removal of donors at the rate  $c \mathbf{f}_{eq}$ . In fact, for fluences greater than  $3 / c \approx 10^{13} \text{ cm}^{-2}$  these donors with initial concentration  $N_{c0}$  are almost completely exhausted. In this context the following relation was found by systemic studies on various detector materials with different resistivity [6]

$$N_{c0} = 0.3 \times N_{eff0} + 0.1 \times 10^{12} \text{ cm}^{-3}, \quad (5)$$

That is,  $N_{c0}$  is notably smaller than the phosphorus concentration of the original material<sup>†</sup>. Eq. (5) is of particular importance as it points to a reservoir of non-removable donors with concentration  $\approx 0.7 \times N_{eff0}$  causing the higher radiation tolerance of lower resistivity material.

An other result reported in ref. [5] concerns the reverse annealing component  $N_Y$ . It was found that the corresponding microscopic process is essentially of 1<sup>st</sup> order while 2<sup>nd</sup> order kinetics had been assumed so far. In order to account for this circumstance, the following expression has been used in this work (compare eq. (3))

$$N_Y(t) = g_Y \mathbf{f}_{eq} t - g_Y \mathbf{f}_{eq} [1 - \exp(-k_{YI} t)] / k_{YI}. \quad (6)$$

The reasoning for this approach and the relation between the 2<sup>nd</sup> order and 1<sup>st</sup> order annealing rates is left for Appendix C.

While the doping concentration is not considered to be temperature dependent by itself, both the beneficial annealing ( $k_a$ ) and the reverse annealing ( $k_{YI}$ ) rates obey the Arrhenius-relation

$$k = k_0 \exp(-E_a / k_B T). \quad (7)$$

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<sup>†</sup> Here the compensation of the original material with boron has been assumed to be very low. This was actually proven by photo luminescence spectroscopy [7]. Therefore  $N_{eff0}$  is almost entirely due to donors.

Frequency factors  $k_0$  and activation energies  $E_a$  are characteristic of the specific annealing process in question and need to be established experimentally, see Appendix A and C.

### Leakage Current

The damage-induced increase in the leakage current  $I$  per area  $A$  has been calculated with

$$\frac{I}{A}(t, T) = W \mathbf{a}_\infty R^{-1}(T) \sum_{i=0} \frac{a_i}{a_0} \mathbf{f}_{eq} \mathbf{t}_i(T) [1 - \exp(-t/\mathbf{t}_i(T))]. \quad (8)$$

$W$  denotes the width of the depleted region

$$W = d \times \min( (V_{op} / V_{dep})^{1/2}, 1 ). \quad (9)$$

Thus, the loss of active volume occurring in partial depletion operation is taken into account.  $\mathbf{a}_\infty$  is the current related damage constant as it is observed at room temperature ( $T_R = 20^\circ\text{C}$ ) after complete annealing<sup>‡</sup>.

Intrinsically the leakage current originating from damage-induced bulk generation centers varies strongly with temperature. This is accounted for by the dimensionless scaling factor

$$R(T) = (T_R / T)^2 \exp\left(-\frac{E_g}{2k_B} \left[\frac{1}{T_R} - \frac{1}{T}\right]\right). \quad (10)$$

Here  $E_g$  is an empirical parameter related to the effective energetic position of a single deep level representing the sum of all current generation centers introduced by bulk damage.  $E_g$  has a value of about the band gap of the semiconductor.

Steady-state introduction and annealing of the generation centers is treated similar to the beneficial annealing of the doping concentration, see eq. (3). However, as the leakage current annealing curve has originally been parameterized by a sum of exponential terms  $a_i \exp(-t/\mathbf{t}_i)$ , each has been identified here with an independent defect requiring the summation made in eq. (8). In this note the parameters listed in Table 2 have been used. They describe the normalized annealing function at room temperature for inverted detectors.

$i$	0	1	2	3	4
$\mathbf{t}_i(T_R)$ [d]	$\infty$	6.07	1.08	$5.9 \times 10^{-2}$	$9.4 \times 10^{-3}$
$a_i$	0.243	0.139	0.121	0.300	0.197

Table 2. Parameterization of the normalized leakage current annealing curve (room temperature) for inverted detectors, from [9].

<sup>‡</sup> Meanwhile it is known that on detectors operated with reasonable protection against edge leakage (e.g. grounded guard ring) the annealing process is not observed to come to rest at all [8]. More detailed studies on this subject are underway.

The decrease of the annealing rate at low temperature can be accounted for by scaling the time constants measured at room temperature [6]:  $t_i(T) = t_i(T_R) / q(T)$ . Only a single activation energy is thereby assumed to characterize the annealing at the microscopic level. Thus, the scaling factor is

$$q(T) = \exp\left(\frac{E_I}{k_B} \left[\frac{1}{T_R} - \frac{1}{T}\right]\right), \quad (11)$$

as can be inferred from the general Arrhenius-relation eq. (7).

### Charge Collection

$$\begin{aligned} t_{tr,n}^{-1}(F_{eq}) &= t_{tr,n0}^{-1} + \begin{cases} g_n F_{eq} & F_{eq} < F_{eq}^* \\ g_n^*(F_{eq} - F_{eq}^*) + g_n F_{eq} & F_{eq} > F_{eq}^* \end{cases} \\ t_{tr,p}^{-1}(F_{eq}) &= t_{tr,p0}^{-1} + g_p F_{eq} \end{aligned} \quad (12)$$

Inversion fluence  $F_{eq}^*$  see eq. (A.4) in Appendix B.

Tmax = 25 ns

### Damage Parameters

Doping Concentration		Leakage Current	
$g_a$	$1.54 \times 10^{-2} \text{ cm}^{-1}$	$a_V$	$2.86 \times 10^{-17} \text{ A/cm}$
$k_{0a}$	$2.3 \times 10^{13} \text{ s}^{-1}$	$E_I$	1.09 eV
$E_{aa}$	1.08 eV	$E_g$	1.24 eV
$c$	$2.29 \times 10^{-13} \text{ cm}^2$	Charge Collection	
$g_c$	$1.77 \times 10^{-2} \text{ cm}^{-1}$		
$g_V$	$4.60 \times 10^{-2} \text{ cm}^{-1}$		
$k_{0YI}$	$8.74 \times 10^{14} \text{ s}^{-1}$		
$E_{aY}$	1.31 eV		
		$t_{tr,n0} = t_{tr,p0}$	1.96 $\mu\text{s}$
		$g_n = g_p$	0.24 $\text{cm}^2/\mu\text{s}$
		$g_n^*$	1.01 $\text{cm}^2/\mu\text{s}$

Table 3. Numerical values of the damage parameters used for the calculations. If not revised in this note, the values are the global data compiled for neutron damage in ref. [2].

## 4. Results

$$F_{eq}(R) = F_{eq}(1 \text{ cm}) / R^2$$

$$T_{op}(R) = 3^\circ\text{C}/\text{cm} (R - 1 \text{ cm}) + 5^\circ\text{C}$$

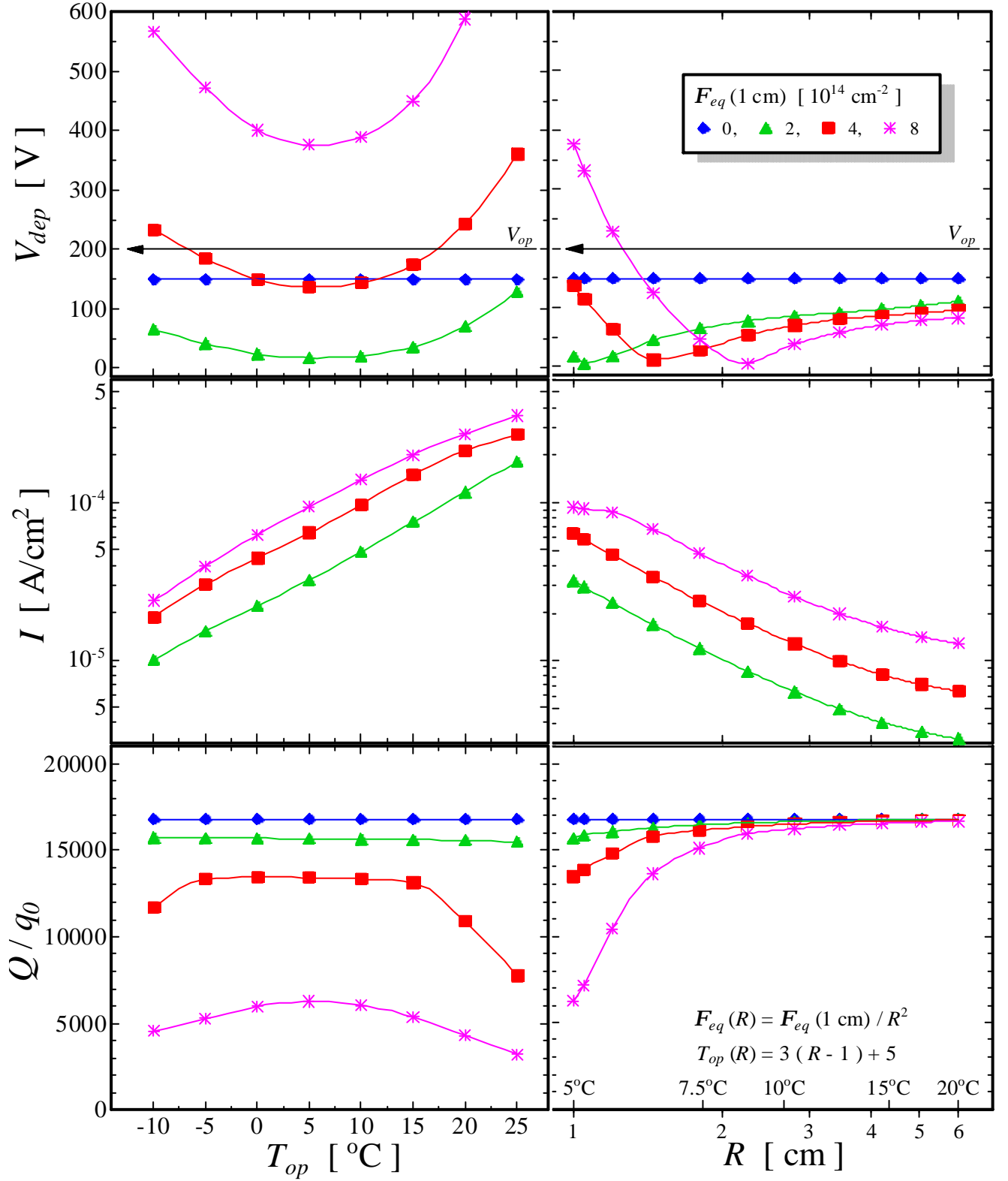


Fig. 1. Results for  $d = 200 \mu\text{m}$



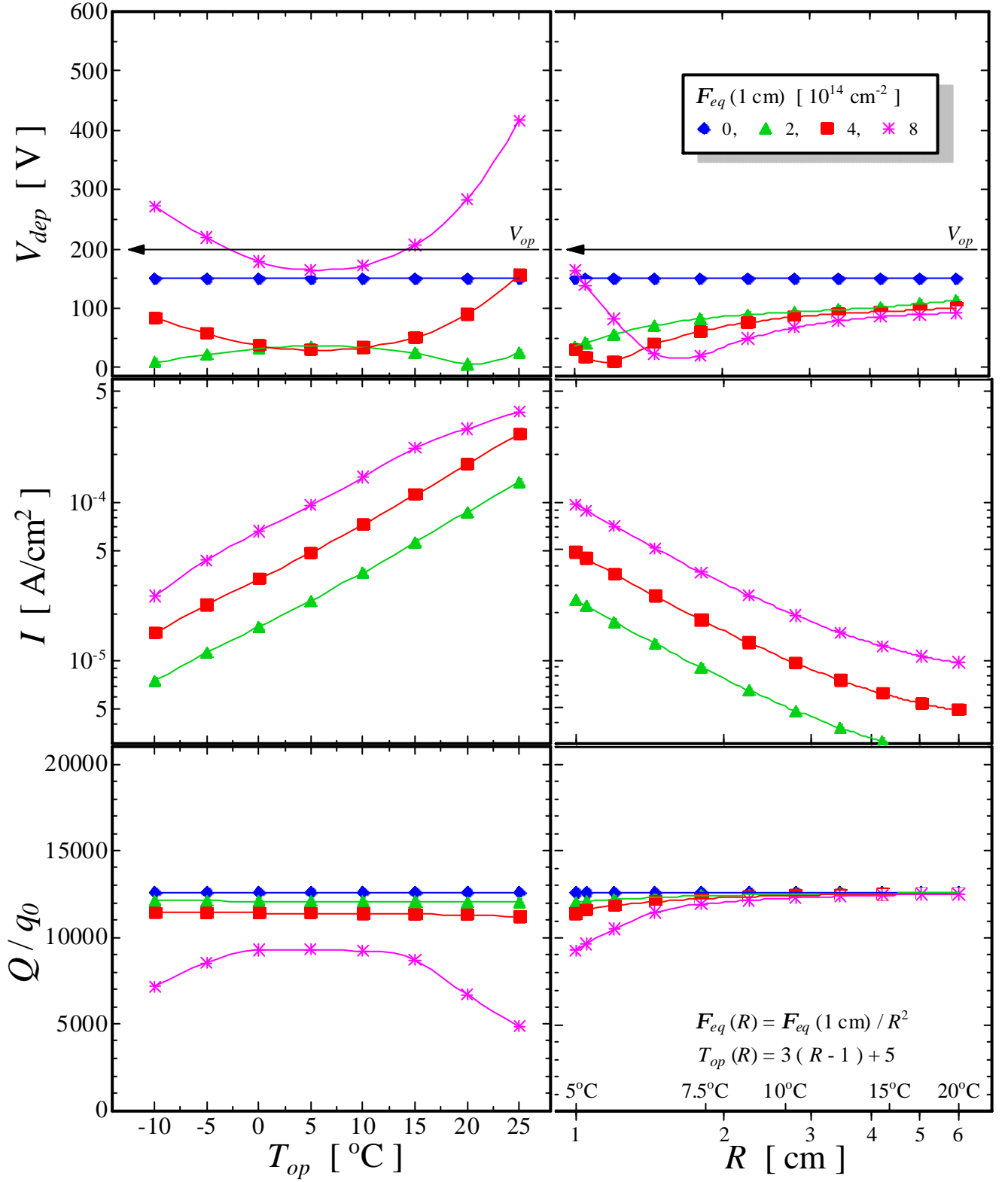


Fig. 2. Results for  $d = 150 \mu\text{m}$

## 5. Discussion

### Operating Temperature

$T$	-10	-5	0	5	10	15	20	25
$t_a$ [d]	$2.43 \times 10^2$	$1.00 \times 10^2$	$4.25 \times 10^1$	$1.86 \times 10^1$	$8.40 \times 10^0$	$3.90 \times 10^0$	$1.86 \times 10^0$	$9.07 \times 10^{-1}$
$t_{yl}$ [d]	$1.62 \times 10^5$	$5.53 \times 10^4$	$1.96 \times 10^4$	$7.20 \times 10^3$	$2.74 \times 10^3$	$1.08 \times 10^3$	$4.40 \times 10^2$	$1.84 \times 10^2$
$R$	20.3	11.8	6.95	4.17	2.55	1.59	1.00	0.641
$q$	$7.31 \times 10^{-3}$	$1.79 \times 10^{-2}$	$4.25 \times 10^{-2}$	$9.76 \times 10^{-2}$	$2.18 \times 10^{-1}$	$4.73 \times 10^{-1}$	$1.00 \times 10^0$	$2.06 \times 10^0$

Table 4. Parameters deciding on the choice of the optimum operating temperature.

### Starting Material

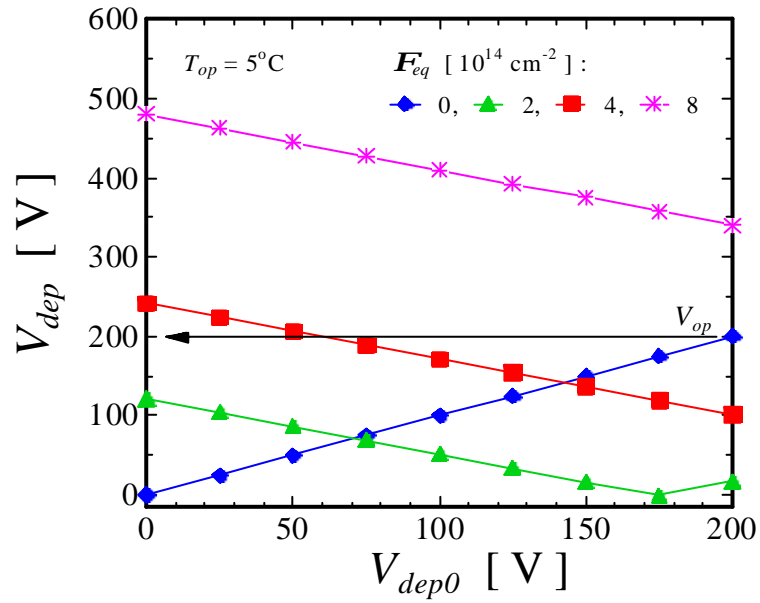


Fig. 3. Variation of the final depletion voltage with the initial depletion voltage for  $d = 200 \mu\text{m}$ .

### Accuracy

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## Appendix A: Beneficial Annealing of the Doping Concentration

The variation of the full depletion voltage observed directly after a short term exposure to heavy-particle irradiation is attributed to the annealing of a small number of acceptors. This approach corresponds to a mathematical representation of the annealing curve by a sum of exponential terms  $a_i \exp(-t/t_i)$ . As annealing time constants of the order of minutes or hours are not relevant to the operation of silicon detectors in high-energy physics experiments, only the longest decay time constant  $t_a$  will be considered here. For a specific irradiation with 1 MeV-neutron-equivalent fluence  $F_{eq}$  the contribution from this portion to the overall doping change varies with time as

$$N_a(t) = g_a F_{eq} \exp(-t/t_a). \quad (\text{A.1})$$

In this note  $t_a$ -data have been compiled from literature along with the corresponding introduction rates  $g_a$ , see Table A.1.

$T$ [°C]	$t_a$ [d]	$g_a$ [ $10^{-2} \text{ cm}^{-1}$ ]	$k$	Reference
-10	$440 \pm 32^a)$			[10]
0	$44 \pm 2.0$	$1.26 \pm 0.02$	$0.582^b)$	[11] M40
0	$66.7 \pm 4.8^a)$			[10]
10	$8.3 \pm 0.7$	$1.68 \pm 0.05$	$0.582^b)$	[11] M44
10	$12.1 \pm 0.87^a)$			[10]
10	$5.8 \pm 1.0$	$1.45 \pm 0.28$	$2.89^c)$	[12] Mean pC
10	$4.6 \pm 1.1$	$1.05 \pm 0.03$	$0.94^d)$	[12] Mean $\pi$ C
20	$2.0 \pm 0.32$	$2.23 \pm 0.17$	$0.582^b)$	[11] M18
21	$1.8 \pm 0.13^a)$	1.78	$\approx 1.10^e)$	[10]
25	$1.5 \pm 0.5$	$0.69 \pm 0.37$	$0.94^d)$	[12] Mean $\pi$ W
60	$(1.45 \pm 0.09) \times 10^{-2}$	$2.2 \pm 0.2$	$1.44^f)$	[13]

<sup>a)</sup> Error taken as the difference between the data points and the fit in [10]

<sup>b)</sup> Experimental value (ref. [6]) for the 24 GeV/c p at CERN PS

<sup>c)</sup> 21 MeV p at MPI Heidelberg

<sup>d)</sup> 190 MeV  $\pi^+$  at PSI

<sup>e)</sup> 647 MeV and/or 800 MeV p at LAMPF

<sup>f)</sup>  $<5.3>$  MeV n at PTB Be(d,n)

Table A.1. Annealing time constant and introduction rate as function of temperature compiled from literature.

The annealing time constant is the inverse of the corresponding annealing rate. Thus, according to the Arrhenius-relation eq. (8), it is

$$t_a^{-1} = k_a = k_{0a} \exp(-E_{aa}/k_B T). \quad (\text{A.2})$$

Fig. A.1. demonstrates the reasonable agreement between the experimental values and eq. (A.2). It will be noted that the individual errors in the  $t_a$  data quoted in Table A.1 were not used as weights because the resulting  $\chi^2$  was much larger than the number of degrees-of-freedom of the problem. These errors must therefore be considered unreliable and cannot be used as they might lead to a wrong fit. Consequently, a common unknown error has been estimated from the straight-line fit. The numerical results are

$$E_{aa} = (1.08 \pm 0.05) \text{ eV}$$

$$k_{0a} = 2.3_{0.29}^{18} \times 10^{13} \text{ s}^{-1}.$$

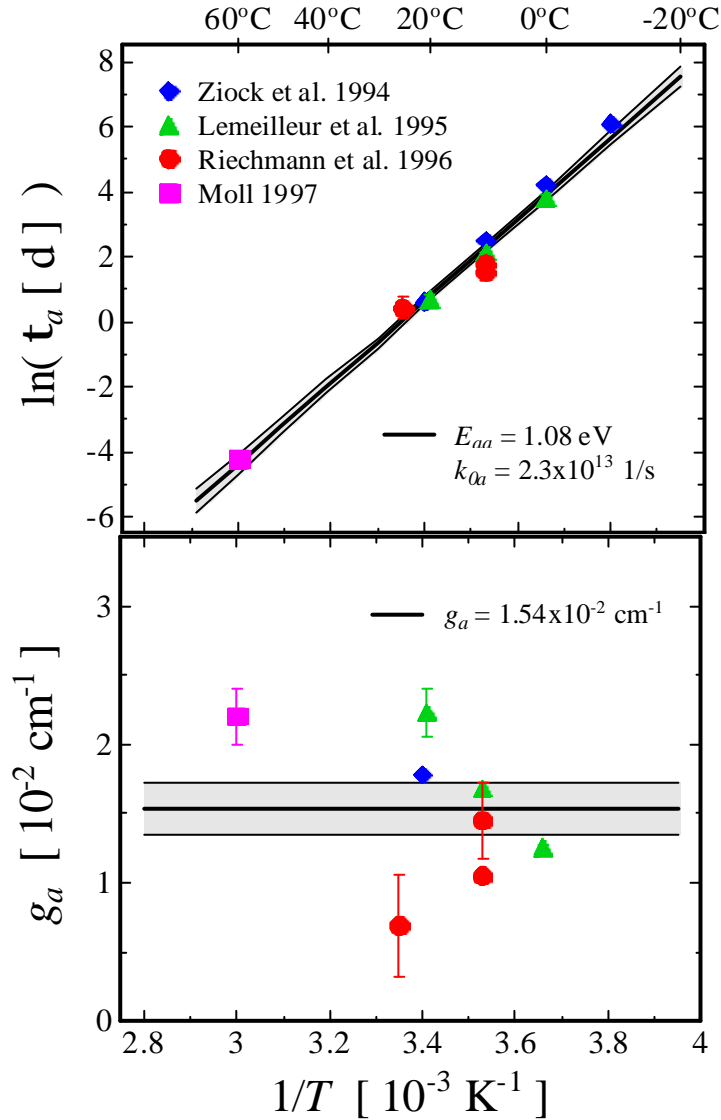


Fig. A.1 Top: Arrhenius plot for the longest annealing time constant. Bottom: corresponding introduction rates. The shaded area represents the prognosis error in the fitted quantity.

It is worth noting the approximately equal values of the activation energies characteristic of the short term annealing of the doping concentration  $E_{aa}$  and the leakage current  $E_I$ , see Table 2. This provides evidence for a

similar origin of the two phenomena, as was already concluded earlier by means of a correlation of the overall annealing curves [14]. Here we have in addition gained the frequency factor  $k_{0a}$  which in the temperature range studied is of the order of the most abundant phonon frequency  $k_B T / h \approx 10^{13} \text{ s}^{-1}$ . At the microscopic level the annealing processes do therefore require only a single jump (dissociation or reorientation) rather than long range migration.

Introduction rates  $g_a$  have been normalized to equivalent 1 MeV-neutron values using the hardness factor  $k$  quoted in Table A.1. For mono-energetic sources with particle energy  $E_p$  it is

$$k = D(E_p) / 95 \text{ MeVmb.} \quad (\text{A.3})$$

$D(E_p)$  denotes the displacement damage cross section and/or damage function. With this definition the 1 MeV-neutron-fluence equivalent to the fluence  $F$  is given by  $F_{eq} = kF$ . If not stated otherwise, the numerical evaluations of  $D(E_p)$  as recommended by the ROSE Collaboration have been used here [5]. Further details on the calculation of  $k$ , also for wide spectrum sources, can for example be found in ref. [15]. Due to the reasons already mentioned above the individual errors in  $g_a$  listed in Table A.1 have not been taken into account. The non-weighted average of the normalized introduction rates and the corresponding error is then found to be (compare Fig. A.1 bottom)

$$g_a = (1.54 \pm 0.19) \times 10^{-2} \text{ cm}^{-1}$$

There is clearly a significant spread around the average value originating from systematic errors. Their sources are various, as for example i) the method used for the evaluation of CV curves, ii) the procedure used for the fitting of the annealing function, iii) the source calibration, and so on. Also the influence of the starting material, a potential hidden parameter in the evaluation, has not yet been thoroughly investigated.

## Appendix B: The Inversion Fluence

As an application of eq. (5) we can very grossly determine the inversion fluence  $F_{eq}^*$  at which the sign of the space charge changes from positive to negative, that is, where  $N_{eff}$  equals zero. It will be assumed that the corresponding change in the doping concentration  $\Delta N_{eff} = N_{eff0} - N_{eff} = N_{eff0}$  is due only to the stable damage component  $N_c$ . This ensures inversion even if the annealing and the reverse annealing fraction are at a certain time much smaller than  $N_c$ . Moreover, it will be anticipated that for conventional materials  $F_{eq}^*$  is so large that all donors with concentration  $N_{c0}$  are removed. Then eq. (4) reduces to  $N_c \approx N_{c0} + g_c F_{eq}^*$  and substitution of eq. (5) yields

$$F_{eq}^* \approx (N_{eff0} - N_{c0}) / g_c \approx 40 \text{ cm} \times N_{eff0}. \quad (\text{A.4})$$

In view of the above presuppositions it is obvious that eq. (6) gives an upper limit of the inversion fluence. For the instance of a short term exposure not allowing for beneficial annealing,  $g_c$  must be replaced with  $g_c + g_a$ . This gives  $F_{eq}^* \approx 21 \text{ cm} \times N_{eff0}$ , which is in good agreement with the result obtained in ref. [16].

## Appendix C: Reverse Annealing — a Process of Effectively 1<sup>st</sup> Order

Reverse annealing data as measured on a silicon detector in the long term after a short term exposure to bulk damaging radiation is best parameterized by the function

$$N_Y(t) = g_Y F_{eq} [ 1 - ( 1 + g_Y F_{eq} k_Y t )^{-1} ]. \quad (\text{A.5})$$

Originally it was believed that two neutral defects of equal concentrations combine to form an acceptor by a 2<sup>nd</sup> order reaction. Recently it was found that the 2<sup>nd</sup> order rate constant  $k_Y$  in eq. (A.4) varies with fluence as  $1 / F_{eq}$  [6]. This does then however point to 1<sup>st</sup> order kinetics at the microscopic level. While therefore the use of eq. (A.4) in conjunction with a fluence dependent rate constant  $k_Y(F_{eq})$  is still valuable for the description of laboratory annealing data, it is not straight-forward to derive a model valid during steady-state irradiation as required for high-energy physics applications. In order to circumvent these difficulties it will be noted that eq. (A.4) is equal to

$$N_Y(t) = g_Y F_{eq} [ 1 - \exp( - g_Y F_{eq} k_Y t ) ] \quad (\text{A.6})$$

as long as  $g_Y F_{eq} k_Y t$  is much smaller than unity. Indeed, the reverse annealing time constant is about one year at room temperature and much larger at lower temperature. Thus, under the operational conditions anticipated at LHC experiments the used approach is well justified. Evidently the equivalent 1<sup>st</sup> order annealing time constant is given by

$$k_{YI} = g_Y F_{eq} k_Y(F_{eq}) = 1.9 \times 10^{16} \text{ cm/s} \times g_Y \exp( - E_{aY} / k_B T ), \quad (\text{A.6})$$

where  $k_Y(F_{eq})$  has been substituted with the empirical expression found in [6]. Moreover, identifying eq. (A.6) with the Arrhenius-relation eq. (8) gives the corresponding frequency factor  $k_{0YI} = 1.9 \times 10^{16} \text{ cm/s} \times g_Y$ . As eq. (A.5) is the solution of a usual differential equation of 1<sup>st</sup> order it is now easy to include an inhomogeneity accounting for the steady-state generation of neutral defects transforming into acceptors during reverse annealing. The solution is given by eq. (7).

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