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**A direct test of  $\mathcal{T}$  symmetry in the neutral K meson system with  
 $K_S \rightarrow \pi \ell \nu$  and  $K_L \rightarrow 3\pi^0$  at KLOE-2**

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**Abstract**

Quantum entanglement of K and B mesons allows for a direct experimental test of time-reversal symmetry independent of  $\mathcal{CP}$  violation. The  $\mathcal{T}$  symmetry can be probed by exchange of initial and final states in the reversible transitions between flavor and CP-definite states of the mesons which are only connected by the  $\mathcal{T}$  conjugation. While such a test was successfully performed by the BaBar experiment with neutral B mesons, the KLOE-2 detector can probe  $\mathcal{T}$ -violation in the neutral kaons system by investigating the process with  $K_S \rightarrow \pi^\pm l^\mp \nu_l$  and  $K_L \rightarrow 3\pi^0$  decays. Analysis of the latter is facilitated by a novel reconstruction method for the vertex of  $K_L \rightarrow 3\pi^0$  decay which only involves neutral particles. Details of this new vertex reconstruction technique are presented as well as prospects for conducting the direct  $\mathcal{T}$  symmetry test at the KLOE-2 experiment.

## 1 Introduction

A direct test of the time-reversal symmetry in a single experiment is of great interest among possible ways to probe the  $\mathcal{T}$  symmetry violation <sup>1)</sup>. For particles with spin 0 such as pseudo-scalar mesons, a direct test may be obtained by observation of an asymmetry between a reaction from state  $i$  to state  $f$  and a reversed reaction  $f \rightarrow i$ . While the CPLEAR experiment measured a nonzero value of the Kabir asymmetry in neutral kaon oscillations <sup>2)</sup>, a controversy was raised as to whether this result was independent of  $\mathcal{CP}$  violation as the  $K^0 \rightarrow \bar{K}^0$  and  $\bar{K}^0 \rightarrow K^0$  transitions are connected by both the  $\mathcal{T}$  and  $\mathcal{CP}$  symmetries. Therefore, an idea was proposed to exploit the quantum correlations of neutral B and K meson pairs to observe reversible transitions between flavour and  $\mathcal{CP}$ -definite states of the mesons <sup>3, 4)</sup>. Such a  $\mathcal{T}$  symmetry test was successfully performed by the BaBar experiment with the entangled neutral B meson system <sup>5)</sup>. In turn, the KLOE-2 detector at the DAΦNE  $\phi$ -factory is capable of performing a statistically significant direct observation of  $\mathcal{T}$  symmetry violation with neutral kaons independently of  $\mathcal{CP}$  violation <sup>4)</sup>.

## 2 Transitions between flavour and $\mathcal{CP}$ -definite neutral kaon states

Neutral kaon states may be described in a number of bases including flavour-definite states:

$$\mathcal{S} |K^0\rangle = +1 |K^0\rangle, \quad \mathcal{S} |\bar{K}^0\rangle = -1 |\bar{K}^0\rangle, \quad (1)$$

as well as the states with definite  $\mathcal{CP}$  parity:

$$|K_+\rangle = \frac{1}{\sqrt{2}} [|K^0\rangle + |\bar{K}^0\rangle] \quad \mathcal{CP} = +1, \quad (2)$$

$$|K_-\rangle = \frac{1}{\sqrt{2}} [|K^0\rangle - |\bar{K}^0\rangle] \quad \mathcal{CP} = -1. \quad (3)$$

State of the kaon can be identified at the moment of decay through observation of the decay final state. With the assumption of  $\Delta S = \Delta Q$  rule<sup>1</sup>, semileptonic kaon decays with positively and negatively charged leptons (later denoted as  $\ell^+$ ,  $\ell^-$ ) unambiguously identify the decaying state as  $K^0$  and  $\bar{K}^0$  respectively. Similarly, the  $\mathcal{CP}$ -definite states  $K_+$  and  $K_-$  are implied by decays to hadronic

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<sup>1</sup>Although an assumption, the  $\Delta S = \Delta Q$  rule is well tested in semileptonic kaon decays <sup>6)</sup>

final states with respectively two and three pions (denoted  $\pi\pi$ ,  $3\pi$ ). In order to observe a transition between the  $\{K^0, \bar{K}^0\}$  and  $\{K_+, K_-\}$  states, both the *in* and *out* states must be identified in the respective basis. This is uniquely possible in the entangled system of neutral K mesons produced at a  $\phi$ -factory. Due to conservation of  $\phi(1^{--})$  quantum numbers, the  $\phi \rightarrow K^0 \bar{K}^0$  decay yields an anti-symmetric non-strange final state of the form:

$$|\phi\rangle \rightarrow \frac{1}{\sqrt{2}} (|K^0(+\vec{p})\rangle |\bar{K}^0(-\vec{p})\rangle - |\bar{K}^0(+\vec{p})\rangle |K^0(-\vec{p})\rangle), \quad (4)$$

which exhibits quantum entanglement between the two kaons in the EPR sense <sup>7</sup>). Thus, at the moment of decay of first of the K mesons (and, consequently, identification of its state) state of the partner kaon is immediately known to be orthogonal. This property allows for identification of state of the still-living kaon only by observing the decay of its partner. Its state can be then measured at the moment of decay after time  $\Delta t$ , possibly leading to observation of a transition between strangeness and CP-definite states. A list of all possible transitions is presented in Table 1. It is immediately visible that time-reversal conjugates of these transitions are not identical with neither their CP- nor CPT-conjugates which is crucial for independence of the test.

	Transition	$\mathcal{T}$ -conjugate
1	$K^0 \rightarrow K_+$ $(\ell^-, \pi\pi)$	$K_+ \rightarrow K^0$ $(3\pi^0, \ell^+)$
2	$K^0 \rightarrow K_-$ $(\ell^-, 3\pi^0)$	$K_- \rightarrow K^0$ $(\pi\pi, \ell^+)$
3	$\bar{K}^0 \rightarrow K_+$ $(\ell^+, \pi\pi)$	$K_+ \rightarrow \bar{K}^0$ $(3\pi^0, \ell^-)$
4	$\bar{K}^0 \rightarrow K_-$ $(\ell^+, 3\pi^0)$	$K_- \rightarrow \bar{K}^0$ $(\pi\pi, \ell^-)$

Table 1: Possible transitions between flavour and CP-definite states and their time-reversal conjugates. For each transition a time-ordered pair of decay products which identifies the respective states is given.

### 3 Observables of the test

For each of the transitions from Table 1 occurring in time  $\Delta t$  and its time-reversal conjugate a time-dependent ratio of probabilities can be defined as an observable of the  $\mathcal{T}$  symmetry test. In the region where high statistics is

expected at KLOE-2, however, two of them are important for the test:

$$R_2(\Delta t) = \frac{P[K^0(0) \rightarrow K_-(\Delta t)]}{P[K_-(0) \rightarrow K^0(\Delta t)]} \sim \frac{I(\ell^-, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^+; \Delta t)}, \quad (5)$$

$$R_4(\Delta t) = \frac{P[\bar{K}^0(0) \rightarrow K_-(\Delta t)]}{P[K_-(0) \rightarrow \bar{K}^0(\Delta t)]} \sim \frac{I(\ell^+, 3\pi^0; \Delta t)}{I(\pi\pi, \ell^-; \Delta t)}. \quad (6)$$

These quantities can be measured experimentally through numbers of events with certain pairs of decays occurring in time difference  $\Delta t$ . A deviation of these ratios from 1 would be an indication of  $\mathcal{T}$  symmetry violation. Bernabeu *et al.* have simulated the behaviour of these ratios expected at KLOE-2 for  $10\text{fb}^{-1}$  of data <sup>4)</sup> (Figure 1). At KLOE-2 the asymptotic region of  $R_2$  and  $R_4$  can be observed where their theoretical behaviour may be expressed as:

$$R_2(\Delta t) \xrightarrow{\Delta t \gg \tau_s} 1 - 4\Re\epsilon, \quad (7)$$

$$R_4(\Delta t) \xrightarrow{\Delta t \gg \tau_s} 1 + 4\Re\epsilon, \quad (8)$$

where  $\epsilon = (\epsilon_S + \epsilon_L)/2$  is a T-violating parameter <sup>4)</sup>.

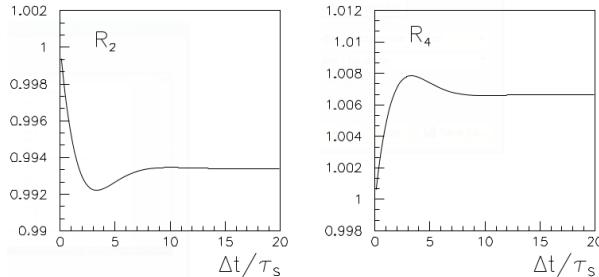


Figure 1: Simulated behavior of the probability ratios expected for  $10\text{fb}^{-1}$  of KLOE-2 data. The figure was adapted from <sup>4)</sup>.

#### 4 Reconstruction of events for the test

The  $\mathcal{T}$  symmetry test requires reconstruction of the processes with  $K_S \rightarrow \pi\pi$ ,  $K_L \rightarrow \pi^\pm \ell^\mp \nu$  and  $K_S \rightarrow \pi^\pm \ell^\mp \nu$ ,  $K_L \rightarrow 3\pi^0$  pairs of decays. While for  $K_S \rightarrow \pi\pi$  the  $\pi^+\pi^-$  final state can be chosen to take advantage of good vertex and momentum reconstruction from charged pion tracks in the KLOE drift chamber, the  $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$  decay reconstruction is a challenging task.

This process only involves neutral particles resulting in the calorimeter clusters from six  $\gamma$  hits being the only recorded information. Moreover, this decay has to be reconstructed in cases where the partner  $K_S$  decays semileptonically and the missing neutrino prevents the use of kinematic constraints to aid  $K_L \rightarrow 3\pi^0$  reconstruction. Therefore, this process requires independent reconstruction.

## 5 The $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$ decay vertex reconstruction

The aim of the new reconstruction method is to obtain the spatial coordinates and time of the  $K_L$  decay point by only using information on electromagnetic calorimeter clusters created by  $\gamma$  hits from  $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$ . Information available for  $i$ -th cluster includes its spatial location and recording time  $(X_i, Y_i, Z_i, T_i)$ . The problem of localizing the vertex is then in its principle similar to GPS positioning and can be solved in a similar manner.

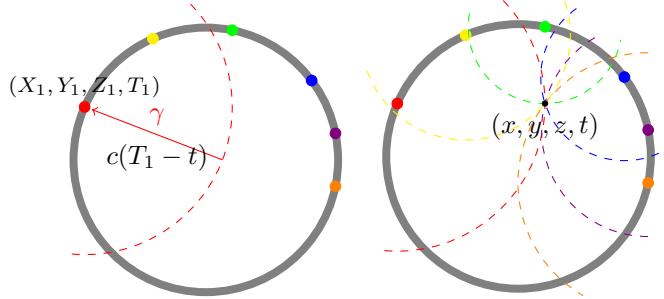


Figure 2: A scheme of  $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$  vertex reconstruction in the section view of KLOE-2 calorimeter barrel (grey circle). Colored dots denote clusters from  $\gamma$  hits. Left: a set of possible origin points of a  $\gamma$  which created a cluster is a sphere centered at the cluster (red dashed line) with radius parametrized by kaon flight time  $t$ . Right: intersection point of such spheres for all  $\gamma$  hits is the  $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$  decay point.

For each cluster a set of possible origin points of the incident  $\gamma$  is a sphere centered at the cluster with radius parametrized by an unknown  $\gamma$  origin time  $t$  (Figure 2, left). Then, definition of such sets for all available clusters yields a system of up to six equations:

$$(T_i - t)^2 c^2 = (X_i - x)^2 + (Y_i - y)^2 + (Z_i - z)^2 \quad i = 1, \dots, 6, \quad (9)$$

with the unknowns  $x, y, z$  and  $t$ . It is then easily noticed that the  $K_L \rightarrow 3\pi^0 \rightarrow 6\gamma$  vertex is a common origin point of all photons which lies on an intersection of the spheres found as a solution of the above system (Figure 2, right). At least 4 clusters are required to obtain an analytic solution although additional two may be exploited to obtain a more accurate vertex numerically.

It is worth noting that this vertex reconstruction method directly yields kaon decay time in addition to spatial location which is useful for time-dependent interferometric studies such as the  $\mathcal{T}$  symmetry test.

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### References

1. L. Wolfenstein, Int. J. Mod. Phys. E **8** (1999) 501.
2. A. Angelopoulos *et al.* [CPLEAR Collab.], Phys. Lett. B **444** (1998) 43.
3. J. Bernabeu, F. Martinez-Vidal and P. Villanueva-Perez, JHEP **1208** (2012) 064 [arXiv:1203.0171 [hep-ph]].
4. J. Bernabeu, A. Di Domenico and P. Villanueva-Perez, Nucl. Phys. B **868** (2013) 102 [arXiv:1208.0773 [hep-ph]].
5. J. P. Lees *et al.* [BaBar Collab.], Phys. Rev. Lett. **109** (2012) 211801
6. J. Beringer *et al.* [Particle Data Group Collab.], Phys. Rev. D **86**, 010001 (2012).
7. A. Einstein, B. Podolsky and N. Rosen, Phys. Rev. **47** (1935) 777.