

# Progress on Cherenkov Reconstruction in MICE

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## Abstract

Two beamline Cherenkov detectors (Ckov-a,-b) support particle ID in the MICE beamline. Electrons and high-momentum muons and pions can be identified with good efficiency. We report on the Ckov-a,-b performance in detecting pions and muons with MICE Step I data.

## 1 Introduction

The international Muon Ionization Cooling Experiment (MICE) [1] is designed to measure muon ionization cooling [2]. Cooling is needed for neutrino factories based on muon decay ( $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$  and  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ ) in storage rings [3] and for muon colliders [4].

The 237 MeV/c data in this note come from runs 3506 to 3509 and 3512 to 3516 taken on 14 and 15 December 2011. The 294 MeV/c data come from runs 4082-4084 taken on 20 May 2012.

The two high density aerogel threshold Cherenkov counters [5], located just after the first time of flight counter, TOF0, in the MICE beamline, are used in support of muon and pion particle identification. The measured [6] refractive indices of the aerogels in the counters are  $n_a = 1.069 \pm 0.003$  in Ckov-a and  $n_b = 1.112 \pm 0.004$  in Ckov-b. The corresponding momentum thresholds for muons (pions) are at 280.5 (367.9) and 217.9 (285.8) MeV/c, respectively. Light is collected in each counter by four 9354KB eight-inch UV-enhanced phototubes and recorded by CAEN V1731 FADCs (500 MS/s).

A charge integration algorithm identifies charge clusters  $q_i, i = 1-8$  in the FADCs where the ADC value crosses a threshold, marking times  $t_1$  and  $t_2$  at the threshold crossings, approximating the pulse beginning and end times. The value of  $t_{max}$  at the cluster signal maximum is found. The algorithm integrates the charge within a  $t_1 - 8$  ns and  $t_2 + 16$  ns timing window in order to ensure full charge collection. The charges are converted to a photoelectron count  $pe_i$ , by subtracting a pedestal  $q_{0i}$  and then normalizing by the single photoelectron  $q_{1i}$  charge for each phototube:

$$pe_i = \frac{q_i - q_{0i}}{q_{1i}}, \quad i = 1 - 8. \quad (1)$$

In the event that no cluster is found, the algorithm repeats an exhaustive search for small  $\approx 1$ -pe signals. For all  $q_i > 0$ , the total charge, arrival time,  $t_1$ , and  $t_{max}$  are stored per event.

The asymptotic  $\beta=1$  light yield  $N_{\beta=1}$  in each counter is measured using the electron peak in MICE calibration-beam runs, giving 25 and 16 photoelectrons (pe's) in Ckov-b and Ckov-a, respectively, for a nominal run. The photoelectron yields versus momentum are displayed in Figure 1. The observed muon thresholds,  $213 \pm 4$  and  $272 \pm 3$  MeV/c, are in reasonable agreement with the expectations given above. The average number of photoelectrons for normal incidence in the counters can be predicted from the Cherenkov angle  $\cos \theta_c = 1/n\beta$ , and, near threshold  $\beta_{th} = 1/n$ ,

$$N_{pe} = N_{\beta=1} \times \sin^2 \theta_c = N_{\beta=1} \times (1 - (p_{th}/p)^2). \quad (2)$$

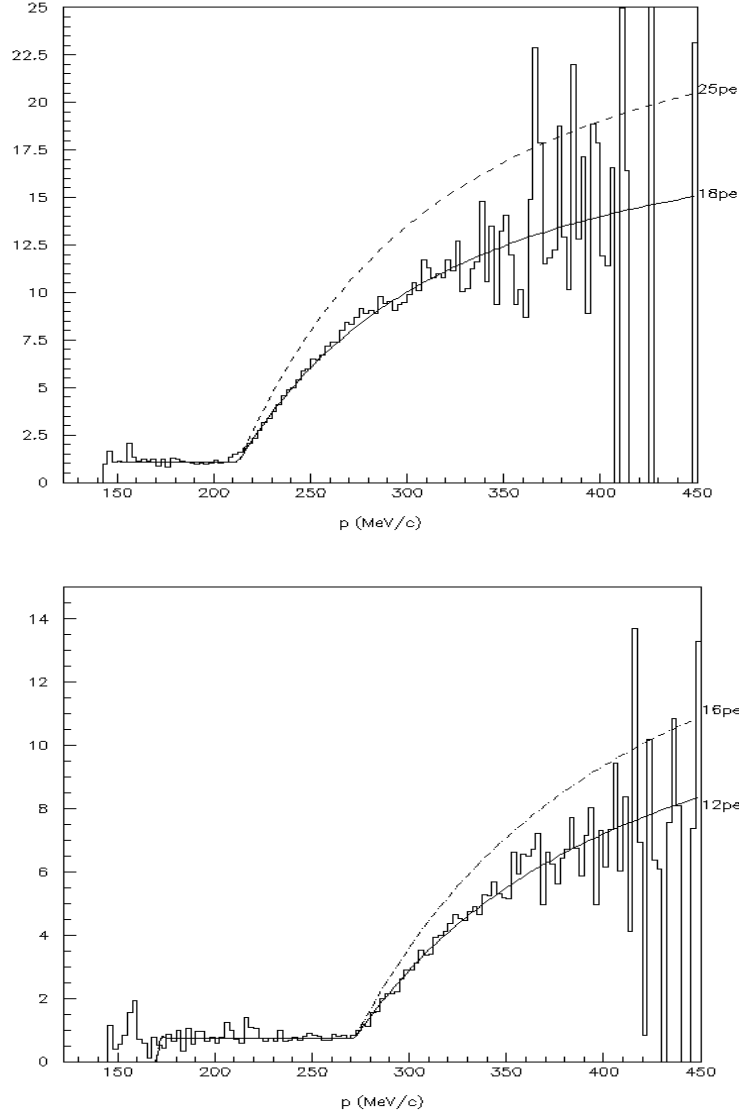


Figure 1: Photoelectron curves versus momentum for muons in Ckov-b (top panel) with the superimposed function  $f = 1.1 + 18 \times [1 - (213/p)^2]$ , and similarly for muons in Ckov-a (bottom), with  $f = 0.75 + 12 \times [1 - (272/p)^2]$ . The  $N_{\beta=1}$  values are about 75% of the values predicted from the asymptotic photoelectron spectrum of  $\beta = 1$  electrons (labeled on the right) — not unexpected since the electrons have a greater likelihood to produce accompanying electrons in TOF0, which acts effectively as a “preshower” radiator.

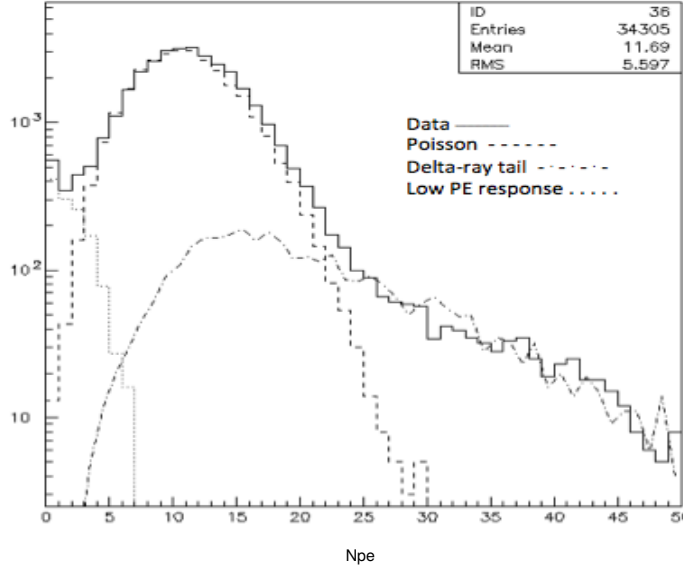


Figure 2: Typical photoelectron spectrum seen for muons or pions above threshold in Ckov-b (solid histogram), together with model fit components: Poisson (dashed), delta-ray tail (dot-dashed), and anomalous low- $N_{pe}$  component (dotted).

As seen in Figure 2, the photoelectron spectra for  $\mu$ ,  $\pi$  are observed to be Poisson-like with tails from electromagnetic showers and delta rays produced as the particle traverses TOF0 and the aerogel radiator. Secondary electrons from these processes above about 1 MeV/c produce Cherenkov light 5–6% of the time for each particle passage. For small- $N_{pe}$  signals, the measured spectra contain more zero-pe events than expected from pure Poisson-like behavior  $P_0(x) = e^{-x}$ ,  $x = \langle N_{pe} \rangle$ . Based on the data we have parameterized the behavior with the function

$$P_0(x) = \max(e^{-x}, 0.2298e^{-0.34344x}). \quad (3)$$

## 2 Beam Particle Spectra

The D1 and D2 dipoles predominantly control the beam momentum and particle types transmitted through the MICE spectrometer. In the  $p_{tgt} \approx p_{D1} \approx p_{D2}$  setting (calibration mode), the beamline transports a mixture of decay/conversion electrons, decay muons, and primary pions. For  $p_{tgt} \approx p_{D1} \approx 2p_{D2}$ , backward muon decays from the decay solenoid (DS) are selected. G4beamline[7] Monte Carlo runs indicate that a small leakage of primary pions through the D2 selection magnet can occur at the  $\sim 1\%$  level. (Note that these pions produce high-momentum decay muons in the MICE beam—a different production mechanism than that of the nominal MICE beam, which comes from pion decays *upstream* of D2.) Both these high-momentum pions and their decay muons should be observable in both Ckov-a and Ckov-b. Ckov-a can be used effectively to select the high-momentum  $\pi$ ,  $\mu$  events that are just over threshold. In Figure 3 we show the MC spectrum of high-momentum pions emerging from the decay solenoid (DS) and then those  $\pi$  (green) and  $\mu$  (red) that will trigger Ckov-a. The ratio of high-momentum muons to pions is about 5:1 at TOF0. Pions emerging from D2 are badly aimed and most miss the TOF1 trigger hodoscope 7.733

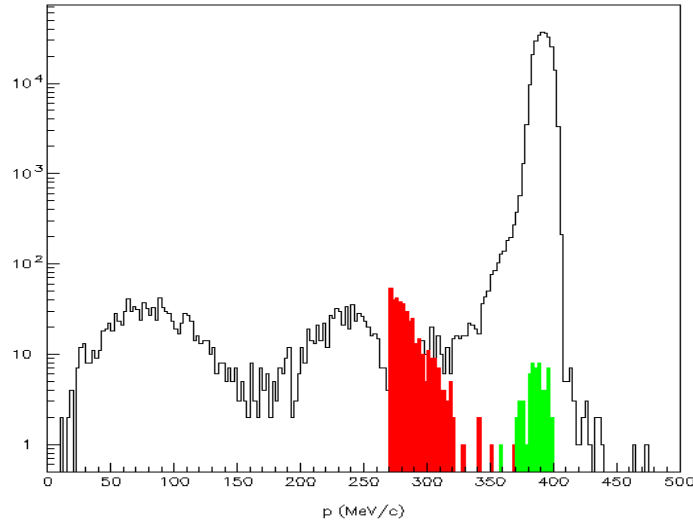


Figure 3: (Solid) MC momentum spectra of pions emerging from the DS: (green) pions surviving at TOF0 with  $p \geq 354$  MeV/c; (red) muons surviving at TOF0 with  $p \geq 270$  MeV/c.

meters downstream. At TOF1 the high-momentum-muon to pion ratio given by G4beamline is approximately 20:1.

### 3 Analysis

For unambiguous identification of particle species the Cherenkov detectors (measuring velocity) would need a momentum measurement from the MICE tracker, which was not available in Step I data. Muons and pions are thus indistinguishable here by the Cherenkov effect. In the following analysis we look for high-momentum  $\pi$  or  $\mu$  that trigger Ckov-a. An additional cut on the number of photoelectrons in Ckov-b serves to suppress the  $\approx 6\%$  of slow “background” events that pass the Ckov-a cut due to delta-ray emission.

We analyzed 120k Step I muon events with  $p_{tgt} = 400$  MeV/c and  $p_{D2} = 237$  MeV/c (the “standard” muon beam settings). We also analyzed 35k muon events with  $p_{tgt} = 500$  MeV/c and  $p_{D2} = 294$  MeV/c. The momentum spectra for these two muon data sets are displayed in Figure 4. In Figure 5 we show the time-of-flight spectrum in the standard  $p_{D2} = 237$  MeV/c muon running condition. The electron time-of-flight peak is centered at 25.84 ns with a width  $\sigma = 0.164$  ns. In the high-momentum time-of-flight window  $27 \text{ ns} < \text{tof} < 28 \text{ ns}$  a small fraction of particles may be pions.

In Figure 6 we cut away the electron signal (by requiring  $\text{tof} > 26.4$  ns) and also make a Ckov-a  $N_{pe} > 2$  cut. The shoulder centered at 27.6 ns is made up of fast muons and pions triggering in Ckov-a and at TOF1. The background events centered approximately at  $\text{tof} = 28$  ns are from particles with momenta below threshold in Ckov-a, but giving  $N_{pe} > 2$  Ckov-a light by delta-ray emission. This background is consistent with the expected 6% contamination level. The  $\text{tof} = 27.6$  ns peak corresponds to  $p_{\mu} = 277$  MeV/c or  $p_{\pi} = 363$  MeV/c, both above threshold in Ckov-a.

Fast muons and pions will leave considerable light in Ckov-b. According to Equation 2 about 10 pe will be produced in Ckov-b at  $p_{\mu} = 270$  MeV/c. The probability for simultaneous delta-ray

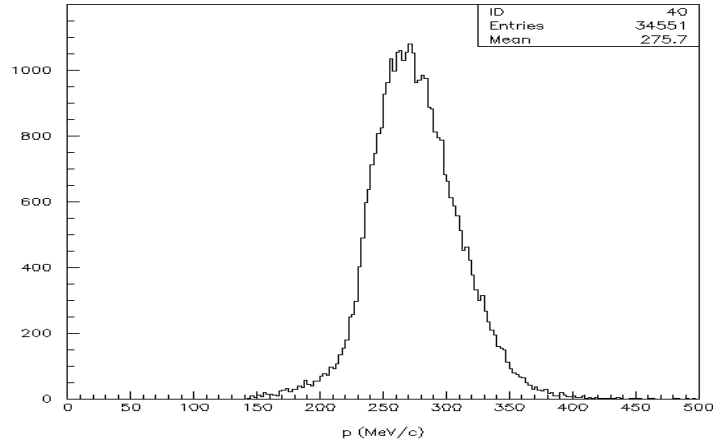
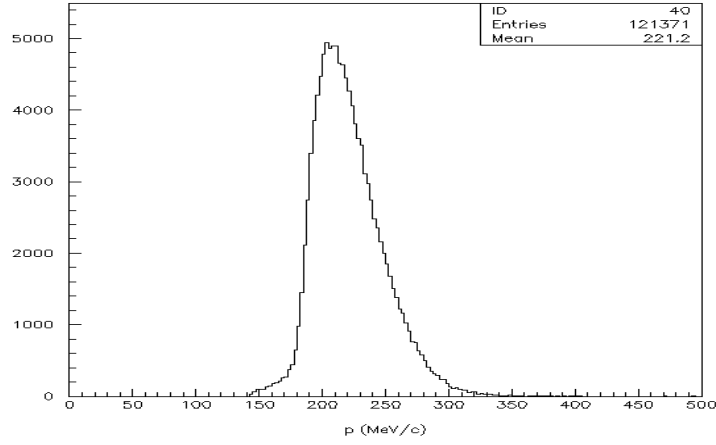


Figure 4: Momentum spectra determined for  $p_{D2} = 237$  MeV/ $c$  data (top) and  $p_{D2} = 294$  MeV/ $c$  data (bottom). Momenta were determined from time-of-flight,  $\Delta t = L/c\sqrt{1 + (m/p)^2}$ , assuming particles are muons.

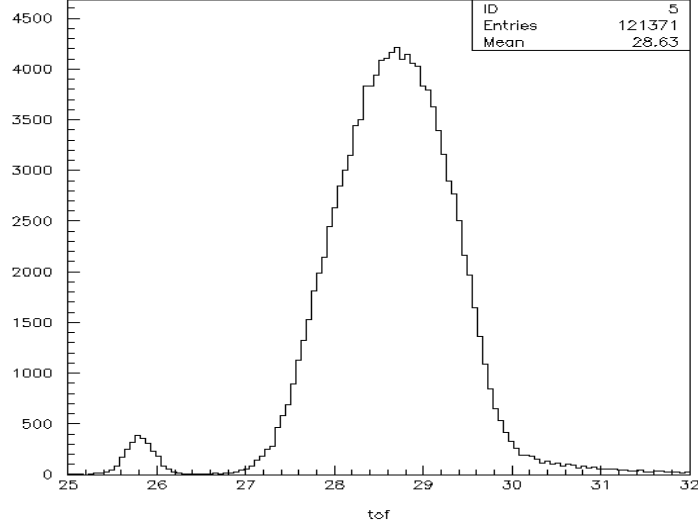


Figure 5: Time-of-flight spectrum from standard ( $p_{D2} = 237 \text{ MeV}/c$ ) muon runs. The electron time-of-flight peaks just below 26 ns.

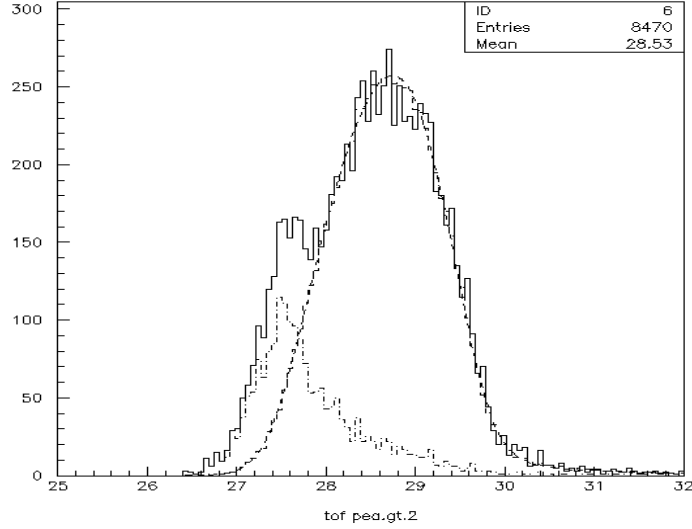


Figure 6: Time-of-flight spectrum with  $p_{D2} > 2$  cut (solid) with shape of muon spectrum superimposed (dashed). Fast  $\pi$ - $\mu$  are identified as the satellite peak centered at 27.6 ns. A cut on  $p_{D2} > 8$  (dot-dash) further reduces the delta-ray background.

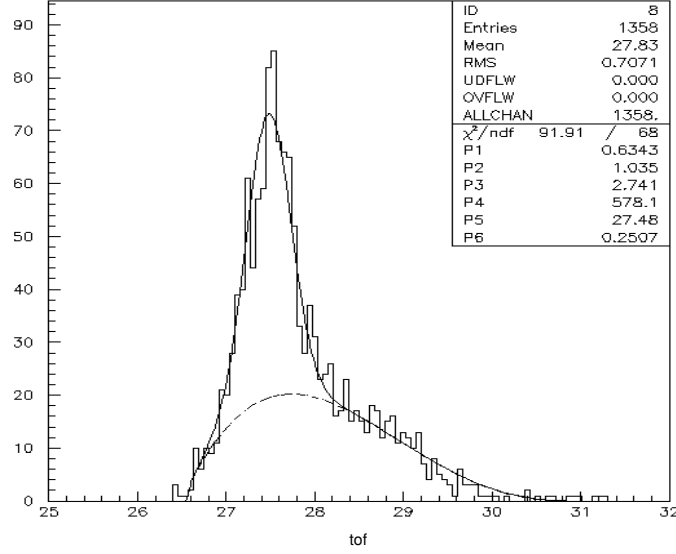


Figure 7: Time-of-flight spectrum with  $\text{pea} > 2$  and  $\text{peb} > 10$  cuts, greatly reducing the delta-ray contribution.

detection in *both* Ckov-a and Ckov-b will be about  $0.06^2 = 3.6 \times 10^{-3}$ . In Figure 7 we add a Ckov-b  $N_{pe} > 10$  cut. The delta-ray background is substantially reduced to about 500 events. A fit to Gaussian signal and phase-space background of the form ( $x \equiv \text{time of flight}$ )

$$f = \frac{N}{\sqrt{2\pi}\sigma} e^{-(x-\bar{x})^2/2\sigma^2} + B (x - x_{lo})^\alpha (x_{hi} - x)^\beta \quad (4)$$

gives  $539 \pm 34$  signal events. When corrected for efficiency (see Section 4) we obtain  $N = 1002 \pm 56$  events. By varying the fitting parameters we find a  $\pm 101$ -event systematic (syst) uncertainty (discussed in Section 5). The fast  $\pi$ - $\mu$  fraction is thus

$$R_{\mu\pi} = \frac{1002 \pm 56 \pm 101}{118,793} = [0.84 \pm 0.05 (\text{stat}) \pm 0.09 (\text{syst})] \%. \quad (5)$$

If we assume all fast  $\pi$ - $\mu$  are pions, we can obtain upper limits on the pion fraction:  $R_{\mu\pi} < 0.97\%$  (90% CL) and  $R_{\mu\pi} < 1.00\%$  (95% CL). Any Bayesian model [8] would require some prior knowledge of the pion-to-muon ratio in the beam. Estimating this (based on the G4beamline simulation) to be about 1/20 (or about 50 pions) allows us to estimate the fraction of pions in the beam to be  $\pi/\mu \simeq 50/119,000 = 0.04\%$ .

## 4 Efficiency Correction

For the efficiency correction we use the  $p_{D2} = 294 \text{ MeV}/c$  data set. The muons in this data set span the Ckov-b and Ckov-a muon thresholds well at 212 MeV/c and 272 MeV/c respectively (see Figure 4(bottom)). We assume the corresponding pion efficiency behaves in a similar manner. This assumption will be checked with  $\pi$ - $\mu$ - $e$  calibration data (Section 5). The efficiency curves for Ckov-a(b),  $\epsilon_{a(b)}(\Delta t)_i$  in each tof bin are determined by taking the ratio of the number of events  $n_i$

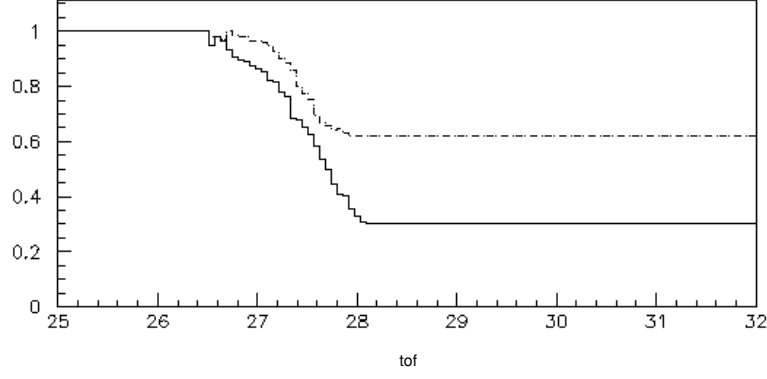


Figure 8: Efficiency curves  $\epsilon_{a(b)}$  vs tof (in ns), in Ckov-b with  $\text{pea} > 10$  (solid) and Ckov-a,  $\text{peb} > 2$  (dashed).

satisfying the  $\text{pea}(b) > x$  cut in the  $i^{\text{th}}$  tof bin to the total number of events  $N_i$  in that tof bin with no Ckov cut applied:

$$\epsilon_{a(b)}(\Delta t)_i = n_i(\text{pea} > x)/N_i, \quad x = 2(10) \text{ pe}. \quad (6)$$

The efficiency curves are displayed in Figure 8. Below 26.5 ns and above 28.0 ns, where data are sparse, asymptotic averages were used.

## 5 Systematic Errors

The systematic errors on the measurement are dominated by the signal fit, and also the efficiency correction  $1/\epsilon_a\epsilon_b$  for Ckov-a and Ckov-b. The efficiency corrections were compared with efficiency corrections from  $\pi\text{-}\mu\text{-}e$  calibration data where muons and pions can be identified via time-of-flight. The average efficiency shift between the  $\pi\text{-}\mu\text{-}e$  calibration data and the  $p_{D2} = 294 \text{ MeV}/c$  muon data sets gave systematic error shifts of  $\pm 0.7\%$  and  $\pm 3.4\%$  (a,b) on the  $n = 1002$  fitted  $\pi\text{-}\mu$  events, or  $\pm 7$  and  $\pm 34$  events respectively. Taken in quadrature we obtain a  $\pm 35$  event systematic error on the efficiency correction. For the fit correction we varied the signal and background fits and determined  $\pm 95$  event count error in Equation 5 corresponding to  $0.08\%$  absolute error. When taken in quadrature, we obtain a  $\pm 101$  event systematic error on the  $\pi\text{-}\mu$  signal.

Table 1: Systematic error estimates on the number of fitted  $\pi\text{-}\mu$  events.

Systematic error	% error	# events	Source
Efficiency correction Ckov-a	0.7%	7	comparison to muon calibration runs
Efficiency correction Ckov-b	3.4%	34	comparison to muon calibration runs
Fitting model	9.4%	95	variation of fit parameters



## 6 Conclusion

We have used the Ckov-a,-b counters to measure the fast- $\pi$ -or- $\mu$  fraction in Step I data. Under the assumption that fast  $\pi$ - $\mu$ 's dominate the pion background (Figure 3), we measure the fast  $\pi$ - $\mu$  ratio to be  $R_{\mu\pi} < 0.97\%$  (90% CL) and  $R_{\mu\pi} < 1.00\%$  (95% CL). Under the further assumption from MC studies that only 5% of the pions in the fast  $\pi$ - $\mu$  beam reach the TOF1 trigger, then the pion contamination level is  $\approx 0.04\%$ , indeed very small.

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