

ASTROMETRY AND OCCULTATION PREDICTIONS TO TRANSNEPTUNIAN AND CENTAUR OBJECTS
OBSERVED WITHIN THE DARK ENERGY SURVEY

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ABSTRACT

Transneptunian objects (TNOs) are a source of invaluable information to access the history and evolution of the outer solar system. However, observing these faint objects is a difficult task. As a consequence, important properties such as size and albedo are known for only a small fraction of them. Now, with the results from deep sky surveys and the Gaia space mission, a new exciting era is within reach as accurate predictions of stellar occultations by numerous distant small solar system bodies become available. From them, diameters with kilometer accuracies can be determined. Albedos, in turn, can be obtained from diameters and absolute magnitudes. We use observations from the Dark Energy Survey (DES) from November 2012 until February 2016, amounting to 4 292 847 CCD frames. We searched them for all known small solar system bodies and recovered a total of 202 TNOs and Centaurs, 63 of which have been discovered by the DES collaboration until the date of this writing. Their positions were determined using the Gaia Data Release 2 as reference and their orbits were refined. Stellar occultations were then predicted using these refined orbits plus stellar positions from Gaia. These predictions are maintained, and updated, in a dedicated web service. The techniques developed here are also part of an ambitious preparation to use the data from the Large Synoptic Survey Telescope (LSST), that expects to obtain accurate positions and multifilter photometry for tens of thousands of TNOs.

Keywords: astrometry – ephemerides – Kuiper belt: general – occultations – surveys

1. INTRODUCTION

The trans-neptunian region (30 AU distant from the Sun and beyond) is a world of small (diameters smaller than 2,400 km), faint (typically, $V > 21$), and cold (20 – 50 K) bodies. These are pristine objects, as well as collisional and dynamical remnants, of an evolved planetesimal disc of the outer solar system whose history and evolution can therefore be accessed from the trans-neptunian objects (TNOs).

Centaurs also play an important role in this study. They are located closer to the Sun in unstable orbits between Jupiter and Neptune, and it is generally accepted that they share a common origin with the TNOs. In this context, they serve as proxies to those more distant and fainter bodies (Fernández et al. 2002).

Because of their large distances from the Sun, TNOs are difficult to observe and study. It is interesting to note that the 30–50 AU region is expected to contain 70,000 or more TNOs with diameters larger than 100 km (Iorio 2007). However, the Minor Planet Center¹ (MPC) lists, to date, a total of $\sim 2,700$ TNOs/Centaurs and features like diameters, colors, taxonomy, presence of satellites are known for less than 15% of these objects². As a consequence, a number of questions about them, like their sizes, size distribution, and a relationship between size and magnitude, are poorly answered. The answers to these questions reveal the history of the trans-neptunian region and leads to the knowledge of its total mass (see Barucci et al. 2008, for a comprehensive review and discussion of the trans-neptunian region).

A dramatic change in this scenario, however, is expected from the deep sky surveys. LSST Science Collaboration et al. (2009), for instance, estimates that 40,000 TNOs will be observed by the Large Synoptic Survey Telescope (LSST) during its 10 years of operation.

As far as the study of these objects through the stellar occultation technique is concerned, it is clear that the combination of large sky surveys and the astrometry from the Gaia space mission (Gaia Collaboration et al. 2018) will provide accurate occultation prediction for numerous bodies.

Although stellar occultations are transient events and still poorly predicted for most TNOs and Centaurs, it is the only ground-based technique from which sizes and shapes can be obtained with kilometer accuracies. Atmospheres can also be studied as their presence, or upper limits for their existence to the level of few nanobars, can be inferred and modelled (see Widemann et al.

2009; Elliot et al. 2010; Sicardy et al. 2011; Ortiz et al. 2012; Braga-Ribas et al. 2013; Gomes-Júnior et al. 2015; Sicardy et al. 2016, for details on sizes, shapes, and atmospheres from stellar occultations). In addition, structures like rings (Braga-Ribas et al. 2014; Ortiz et al. 2017) or even topographic features (Dias-Oliveira et al. 2017) can be detected.

The Dark Energy Survey (DES, Flaugher 2005) observations offer a considerable contribution to the study of small bodies in the solar system (see Dark Energy Survey Collaboration et al. 2016, for an overview of the survey’s capabilities). During its first three years of operations, 2013–2016, more than 4 million CCD images were acquired, where tens of thousands of solar system objects can be found. This considerable amount of data provides accurate positions and multi-filter photometry to, so far, more than one hundred TNOs and tens of Centaurs as faint as $r \sim 24.0$.

Here we present, from the above mentioned observations, positions, orbit refinement, and stellar occultation predictions for all known TNOs and Centaurs, 63 of them discovered by the DES date-range for data as part of the tasks of its Transient and Moving Object (TMO) working group. One of these objects, 2014 UZ224, has already been studied in more detail from radiometric techniques by Gerdes et al. (2017).

In the next section, we briefly describe the DES. In Section 3, we describe the procedure to identify the known solar system objects in the images and the data reduction. In Section 4, we present results and data analysis. Conclusions and comments are presented in Section 5. Photometric data will be presented and explored in a separate paper.

2. THE DARK ENERGY SURVEY

The DES is a survey that covers 5,000 square degrees in the *grizY* bands of the southern celestial hemisphere. It aims primarily to study the nature of the dark energy, an unknown form of energy that leads to an accelerated expansion of the universe (e.g., Perlmutter et al. 1998; Riess et al. 1998; Peebles & Ratra 2003).

Observations within the survey are made with the Dark Energy Camera (DECam, Flaugher et al. 2015), a mosaic of 62 2k×4k red-sensitive CCDs installed on the prime focus of the 4m Blanco telescope at the Cerro Tololo Inter-American Observatory (CTIO). The DECam has a field of view (FOV) of 3 square degrees and the wide-area survey images have, at a 10σ detection level, a nominal limiting magnitude of $r = 23.34$, with the final co-added depth being roughly one magnitude deeper (Morganson et al. 2018). The limiting magnitude is a quantity explained later in the text.

¹ <https://minorplanetcenter.net/iau/mpc.html>

² <http://www.johnstonsarchive.net/astro/tnoslist.html>

Considering only those observations made during the first three years of operation of the DES, the DECam acquired science images from more than 69,000 pointings or, more precisely, 4,292,847 individual CCD exposures in the five bands. This is an invaluable dataset to studies in several fields of astronomy (see [Dark Energy Survey Collaboration et al. 2016](#)), in particular, those related to transient events and moving objects.

3. DATA AND TOOLS

Our basic observational resource are the individual CCD images available from the DES database. In this database, the images taken until FEB/2016 were already corrected for a number of effects (crosstalk, bias, bad pixels, nonlinear pixel response, and flat field), in addition to image-specific corrections like bleed trails from saturated stars, streaks, and cosmic rays (see [Morganson et al. 2018](#), for a detailed description of the DES image processing pipeline).

The set of tools used in this work are general, in the sense that they can be applied to any other survey or image database, and comprehensive, in the sense that they consider all necessary steps (in brief, identification of images with known Solar System bodies, astrometry, orbit refinement, and prediction of a stellar occultation).

These tools, described next, have been ingested in a high performance computational environment to form a pipeline in preparation to also use the data from the LSST. In fact, although LSST is expected to deliver astrometric accuracy ranging typically from 11 mas ($r=21$) to 74 mas ($r=24$) ([LSST Science Collaboration et al. 2009](#)), better astrometry (1-2 mas) is necessary to accurately predict stellar occultations by satellites of small bodies or grazing occultations by rings or by the main body itself, for example. Therefore, it is essential to have tools to independently determine accurate positions when needed.

3.1. Data retrieval and object search

The very first step consists of obtaining the necessary information – pointing, observing date, location in the DES database among others – on all CCD images acquired during the first three years of observations within the DES. This was done through *easyaccess*³, a friendly SQL-based tool to query the DES database. The result from such a query was a file containing the metadata from 4 292 847 CCD images. This file then feeds into the Sky Body Tracker (SkyBoT, [Berthier et al. 2006](#)).

SkyBoT is a project aimed at providing a virtual observatory tool useful to prepare and analyze observa-

tions of solar system objects. In addition to the web-interface service it offers, queries are also possible from the command line. The basic inputs to a cone search⁴, for instance, are: IAU identification of the observatory, J2000 pointing coordinates of a given CCD image, observation date, and a region centered on the pointing coordinates. All these data come from the meta-data previously mentioned. The output is a text or VOTable file format with pieces of information on all known small solar system bodies inside the given region, such as their J2000 astrometric right ascensions and declinations, V magnitudes, names and numbers (when they are numbered), and dynamical classes among others. Table 1 lists the total number of TNOs and Centaurs found in the DES images as well as the expected number of objects for which positions can be determined from them. As we will see later in the text, these expected numbers (column 4 in particular) were surpassed.

The result of the search with the SkyBoT was a file having 1,708,335 entries, most of them of around 140,000 main belt asteroid objects in more than 1.5 million CCD images. These objects, in addition to few thousand members of other dynamical classes also found in the images, are being treated separately.

Note that the detection of a TNO or Centaur is not expected for all selected CCD images. Objects that are faint ($V \gtrsim 24.0$) in the DES images, or images taken under non transparent sky, may not provide a detectable signal of the target. The most frequent exposure time of the DES frames presented here is 90 seconds (see [Morganson et al. \(2018\)](#)).

3.2. Astrometry

Our astrometric tool is the Platform for Reduction of Astronomical Images Automatically (PRAIA, [Assafin et al. 2011](#)) package. PRAIA was conceived to determine photometry and accurate positions from large numbers of CCD images as unsupervised as possible. Its use and performance have been reported by various works (see, for instance [Assafin et al. 2013](#); [Thuillot et al. 2015](#); [Gomes-Júnior et al. 2016](#)) from reference frame to solar system studies. The reference catalog used here for astrometry is the Gaia Data Release 2 ([Lindegren et al. 2018](#)). All differences in right ascension as well as all uncertainties related to measurements along right ascension are multiplied by the cosine of the declination.

A Intel(R) Xeon(R) CPU E5-2650 v4@2.20GHz configuration, using 40 cores, reduces 1,000 CCD images in

³ <https://github.com/mgckind/easyaccess>

⁴ A search based on a sky position and an angular distance from this position.

Table 1. Statistics of known TNOs and Centaurs in the DES images from the three first years of survey.

Dynamical class ^a	Total objects	Total observations	Expected objects	Expected observations
(1)	(2)	(3)	(4)	(5)
TNOs	270	16,537	84	3,010
Centaurs	67	2,519	13	333

NOTE—Columns (2) and (3): Total number of TNOs, Centaurs, and their respective observations, as alerted by the SkyBoT among the observations made by the DES until FEB/2016. Columns (4) and (5): Expected total number of TNOs, Centaurs, and their respective observations, under the following constraints: ($V \leq 24.0$) and ephemeris uncertainty $\leq 2''$ in both right ascension and declination. The visual magnitude as well as the positional uncertainties were also obtained from the SkyBoT.

^a As provided by the SkyBoT.

20 minutes from a parallelized run of PRAIA. A total of 12,561 CCD images were treated here.

The presence of distortion effects, also known as Field Distortion Pattern (FDP), are expected in detectors with large FOVs such as that of the DECam. Common solutions are, e.g., the use of a high-degree polynomial (not always recommended) to relate CCD and gnomonic coordinates of reference stars, the brute-force determination of a distortion mask (e.g., Assafin et al. 2010), and the construction of an empirical model that takes into consideration effects due to the atmosphere and the instrument. This last one was the solution adopted here to correct for the FDP.

Such a solution (hereafter C0) is based on the model developed by Bernstein et al. (2017) and was the first step toward the determination of positions. C0 provides corrections for the instrumental distortion effects including color terms from the optics. A first degree polynomial can be subsequently used to relate CCD and gnomonic coordinates of reference stars, providing reliable solutions from fields with low star densities. Observed positions will be sent to the MPC.

3.3. Orbits

The refinement of orbits is obtained with the code Numerical Integration of the Motion of an Asteroid (NIMA, Desmars et al. 2015). NIMA starts from existing orbital parameters and then iteratively corrects the state vector from the differences between observations and computed positions through least squares. NIMA adopts a specific weighing scheme that takes into account the estimated

precision of each position (σ_i), depending on the observatory and stellar catalog used as reference to determine the observed positions, the number of observations obtained during the same night in the same observatory (N_i) as well as a possible bias due to the observatory (b_i). The final variance of the observation i is given by $\omega_i^2 = N_i b_i^2 + \sigma_i^2$. As a consequence, the weight is given by $1/\omega_i^2$. This weighing scheme is particularly relevant when we consider old epoch positions that do not use the Gaia catalog as reference.

The values used in the NIMA weighing scheme are described in Desmars et al. (2015) and were consolidated before the release of the astrometric data from the Gaia mission. Therefore, the code was improved to profit from the DES observations and from the Gaia releases. In this way, we have adopted $\sigma_i = b_i = 0.125''$ for observations reduced with the Gaia DR1 and $\sigma_i = b_i = 0.1''$ for observations reduced with the Gaia DR2. We emphasize that this latter is the case of DES observations presented here.

It is possible to run NIMA, with the help of few scripts, in an unsupervised way so that it is suitable for a pipeline. One of its outputs is the object ephemeris in a format (*bsp* – binary Spacecraft and Planet Kernel) that can be readily used by the SPICE/NAIF tools (Acton 1996; Acton et al. 2018) to derive the state vector of a given body at any time.

3.4. Prediction of stellar occultations

The prediction of an occultation event is given by prediction maps that show where and when, on the Earth, such an event can be observed. This involves the knowledge of the Earth’s position in space, the geocentric ephemeris of the occulting body, and a set of stellar positions in the neighborhoods of the sky path of the occulting object as seen by a geocentric observer (see details in Assafin et al. 2010). Note that, with the astrometry from Gaia, the uncertainties in predictions rest completely upon the accuracy of the ephemerides.

A dedicated website, as presented in the next section, provides these occultations maps where many events occurring during daylight are also shown. This is done so that we are aware of even those ones that can be observed near the Earth terminator.

4. RESULTS AND ANALYSIS

The high quality of the DES images provided us an accurate set of positions within the range of the observed magnitudes. As a consequence, the objects studied here were grouped according to the number of observations and the uncertainty of their existing ephemeris, rather than on the accuracy of the observed positions.

Note that we use the ephemeris positions as a primary parameter to identify the observed position of a given TNO/Centaurs in the images.

4.1. Filtering

The determination of positions of TNOs and Centaurs from the DES images was subject to at least three constraints. The first one is that the ephemeris position of the target falls inside a box size of $4'' \times 4''$ centered on its observational counterpart. The second is an iterative 3σ filtering on the offsets, as obtained from the differences between observations and a reference ephemeris, to eliminate outliers. The third constraint is based on a brief inspection of the magnitudes as obtained from the DES database for each filter. Differences larger than $\Delta = 0.9$ magnitude between the brightest and faintest values in each filter, when multiple measurements were available, were investigated and eventually eliminated. This value of Δ takes into account a maximum variation of $\sigma_S = 0.15$ (absolute value) in the magnitude due to the object's rotation, a maximum uncertainty of $\sigma_M = 0.1$ in the observed magnitude, and a maximum variation of $\sigma_P = 0.25$ (absolute value) in the observed magnitude due to the phase angle. In other words, $\Delta \sim 3 \times \sqrt{\sigma_S^2 + \sigma_M^2 + \sigma_P^2}$.

These constraints were expected to provide a reliable identification of the solar system objects in the images with minimum elimination of good data. However, a preliminary orbit fitting of some objects still showed the presence of real outliers (misidentifications). To solve this, a fourth filter was applied to our data and affected mostly those sources whose ephemerides presented large uncertainties (extension and doubtful sources, see Section 4.2). Basically, this filter looks for positional offsets (observed minus ephemeris positions) that are clustered and, from them, a mean (x_0) and standard deviation (σ_0) are determined. Then, any offset that differs from x_0 by more than $N \times \sigma_0$ is eliminated. Most frequently, $N = 5$ was used. This filter is more resistant to the presence of outliers than the 3σ filtering mentioned above.

As a result from this process, misidentifications of TNOs and Centaurs from the images were reduced to a minimum, although real outliers may still be found mostly among the doubtful sources with large ephemeris uncertainties.

4.2. Organization

Our results in astrometry are organized in Tables 5 to 7 (Appendix A), and the respective source distribution in the sky can be seen in Fig. 1.

Table 5 (main) consider those sources for which the 1σ ephemeris uncertainty (σ_E) in RA/DEC is smaller than

or equal to $2''$ for TNOs and Centaurs and the number of observations (N) is greater than or equal 3. Table 6 (extension) consider those sources for which the ephemeris uncertainty is $2'' < \sigma_E \leq 12''$ and $N \geq 5$. Table 7 (doubtful) consider the remaining sources. All the ephemeris uncertainties used in these tables were obtained from the JPL on 27 April 2018 and are referred to 2014-Jan-01 at 0h UTC. Note that these uncertainties are given as they appear in their respective ephemerides, that is, 3σ values.

4.2.1. The extension table: rationale

Most (90%) of the CCD images treated here have less than 1,100 sources. Knowing that the size of one CCD in the DECam is $\sim 9' \times 18'$, we can consider that there is 1 field object⁵, on average, inside a box of $24'' \times 24''$. In this way, it is expected that a box of this size centered on the ephemeris (calculated) position of an object in Table 6 contains the respective observed position and a field star. If any of them falls inside a box of $4'' \times 4''$ around the ephemeris position, then this observed position is flagged as an eligible target. If not eliminated by the other steps of the filtering process, then this observed position is selected to refine the respective orbit.

We adopted the number 5 as the minimum number of filtered (see Section 4.1) selected positions that an object with ephemeris uncertainty $2'' < \sigma_E \leq 12''$ must have to appear in the extension table. Orbits for the objects in this table do not have the same quality as those for objects in Table 5. However, as illustrated by Fig. 2 (compare it to Fig. 6, panel (a), shown later in the text), the 5 or more positions of each object in that table are a relevant contribution to the refinement of their respective orbits.

4.3. Accuracies

In the astrometric analysis of these images, it is interesting to introduce here the concept of *limiting magnitude*, as presented by Neilsen et al. (2015), and also discussed by Morganson et al. (2018).

The limiting magnitude is that at which the magnitude of a star is measured with an uncertainty of 0.1 mag. It can be shown to be related to a quantity τ by

$$m_{lim} = m_0 + 1.25 \log \tau, \quad (1)$$

where τ is a scaling factor to the actual exposure time (given by the image header). As a consequence, an *effective exposure time* can be defined as $\tau \times$ nominal exposure time. The τ quantity and the limiting magnitude,

⁵ Any signal on the CCD that is recognized as an object (star, solar system object, etc).

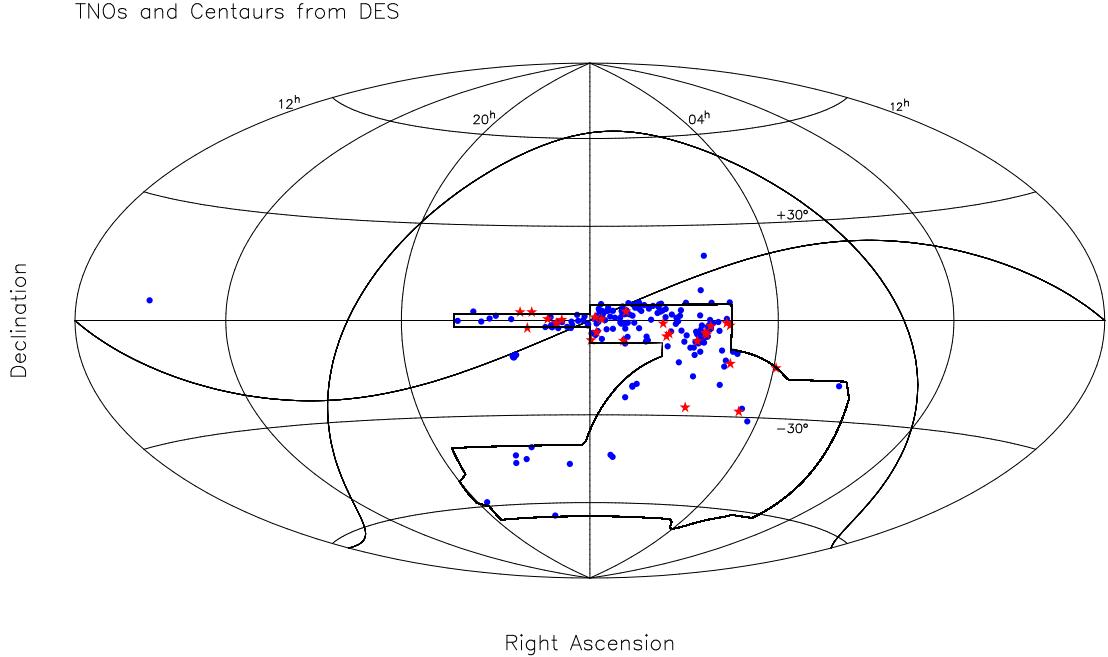


Figure 1. Hammer-Aitoff equal-area projection of the sphere for the TNOs (blue dots) and Centaurs (red stars) for which a position was determined. The ecliptic and Galactic planes, as well as the DES footprint, are also represented by black lines. Some fields are clearly outside the DES footprint. They refer to observations associated to the Vimos VLT deep survey (leftmost blue dot - Le Fèvre et al. 2005), to the LIGO event G211117 (the two northermost blue dots - Cowperthwaite et al. 2016), and to DES engineering time (blue dots close to the ecliptic, at right ascension ~ 22.4 h).

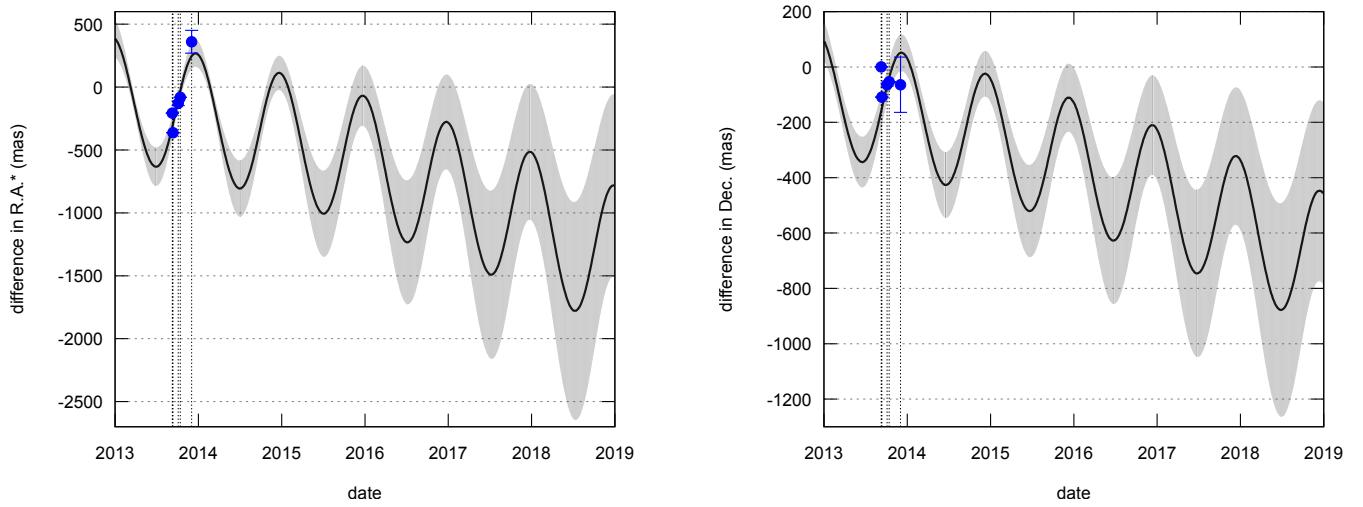


Figure 2. Difference (black lines) in right ascension (left panel) and declination (right panel) between the orbit determined with NIMA and that from the JPL (version: JPL#4) for the TNO 2002 PD149. In the same way, blue dots are the differences between the observed positions and those from the JPL ephemeris. This object belongs to the TNO extension group, Table 6. The sense of the differences is NIMA minus JPL.

therefore, can be used as a quality parameter for a given image. In order to determine the limiting magnitude in the r -band shown in Figs. 3 and 4, the value $m_0 = 23.1$ was taken from Neilsen et al. (2015) and the values of τ were obtained directly from the DES database for each CCD (Morganson et al. 2018).

The accuracy of the observations for the objects presented in Tables 5 to 6 (columns 5 and 6) is illustrated by Fig. 3, where the average limiting magnitude (22.9) in the r -band (dashed line) sets a rough limit in the upper panels from which the uncertainties become larger, mainly when the number of observations is low. It also shows that the sources with a large number (hundreds) of observations have magnitudes that are close to or fainter than this limiting magnitude.

Two relevant features are shown by Fig. 3. Firstly, the lower panels show that, even in frames with the shortest exposure time (90 s), we detect sources with r as faint as ~ 24.0 with a quality that is comparable to those from frames with an exposure time of 400 s thanks to the excellent quality of the images. It is worth mentioning that the faintest objects are more than 1 magnitude fainter than the average limiting magnitude in the r -band. Secondly, it is also possible to note that the range of uncertainties in right ascension is wider than that in declination. This feature most probably results from the fact that the ephemeris uncertainties (columns 3 and 4, Tables 5 to 7) are, on average, larger in right ascension than in declination, since we do not verify such a large difference between our measurements in RA and DEC as discussed below.

The standard deviations in Tables 5 to 7 (columns 5 and 6), obtained from the differences between the observed positions and those from the respective JPL ephemeris, is a common way to express the positional accuracy of solar system targets. These differences vary as a function of time so that, in the present study, the standard deviations provided by these columns numerically overestimate the internal accuracy (or repeatability) of the astrometric measurements.

A second astrometric empirical model (hereafter C1), also developed by the DES collaboration and based on Bernstein et al. (2017), provides improved astrometric solutions for all of the good-quality wide-survey DES exposures for years 1 through 4 of the survey. From C1, instrumental solutions are believed accurate to smaller than 3 mas RMS per coordinate. As a consequence, every DES astrometric measurement will be limited by the stochastic atmospheric distortions, typically ~ 10 mas RMS in a single exposure within this solution. Note that, as compared to C0, C1 is available to a smaller set of DES exposures.

Table 2. Differences between the astrometric results presented here and the DES empirical model

Type	$\Delta\alpha\cos\delta$	$\Delta\delta$	$\sigma_\alpha\cos\delta$	σ_δ	Measurements
	(mas)	(mas)	(mas)	(mas)	
(1)	(2)	(3)	(4)	(5)	(6)
TNO	3	-4	11	9	142
Centaur	2	-5	12	5	22

NOTE—Columns (2) and (3): average of the differences between this work and the empirical model in right ascension and declination, respectively. Columns (4) and (5): standard deviation from the measurements used to determine the values in Columns (2) and (3), respectively. Sense of the differences: this work minus empirical model.

We compared the positions we determined for TNOs and Centaurs to all those ones resulting from C1. This comparison is summarized in Table 2, where all differences we found between our results and those from C1 were kept. It is important to note, however, that C1 does not provide a solution for all CCDs. We stress that C1 is only used to provide a more realistic estimate of the internal accuracy of our measurements as well as a comparison between our positions and those from the most recent astrometric empirical model developed by the DES collaboration. C1 does not participate in any of the astrometric determinations provided here.

The standard deviations shown in Table 2 (columns 4 and 5) are a more reliable estimate of the internal accuracy of our measurements, as compared to those obtained in Tables 5 to 6. This internal accuracy is given by the standard deviation of the measurements, not of the mean. Therefore, the small systematics between both solutions (columns 2 and 3) can not be considered negligible. Part of them, at least, may be explained by the fact that the empirical model is based on the Gaia Data Release 1 (Gaia DR1, Lindegren et al. 2016). It is also worth mentioning that, when our positions are referred to the Gaia DR1 (that is, the Gaia DR1 is used as reference for astrometry), the values of these standard deviations in right ascension and declination are more similar to each other.

On the other hand, a realistic estimate of the final positional accuracy of the targets (or how accurate their equatorial coordinates are given in the International Celestial Reference Frame (ICRF, Ma et al. 1998)) can be obtained from the root mean square (RMS) of the ref-

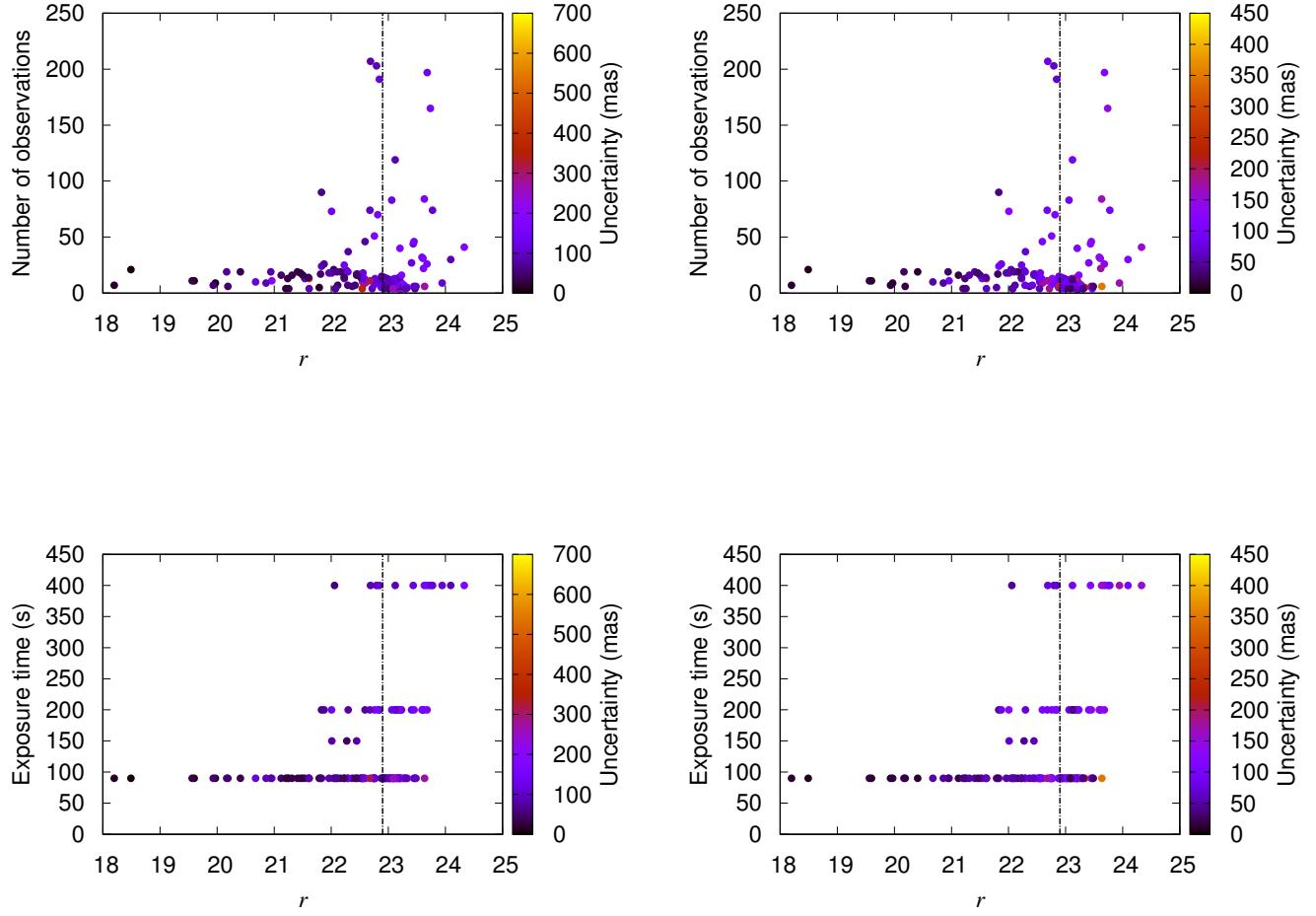


Figure 3. Positional uncertainty as a function of the magnitude and the number of observations in right ascension (left panels) and declination (right panels) for the TNOs and Centaurs in Tables from 5 to 6. In the upper panels, the number of observations is given as a function of the magnitude. In the lower panels, the exposure times are given as a function of the magnitude. In case of different exposure times for the same object, the longest one was considered. In all panels, the positional uncertainty is given in mas and are color coded. The dashed line gives the median value (22.9) of the limiting magnitude in the r -band for these observations. In the upper panels, the TNO (437360) 2013 TV158 (see Table 5) is not shown due to its large number of observations (438).

ference stars, as given by the differences between their observed and catalog positions, and the precision in the determination of the object’s centroid. This latter as well as the RMS of the reference stars for different filters and magnitude ranges are provided by Table 3. In this context, this final accuracy to both equatorial coordinates is obtained, at the 1σ level, from the quantity

$$\sigma_F = \sqrt{\sigma_C^2 + \sigma_R^2}, \quad (2)$$

where σ_C is the uncertainty in the determination of the objects’ centroid and σ_R is the RMS of the reference

stars. For the r filter, for instance, $12 \text{ mas} < \sigma_F < 20 \text{ mas}$.

4.4. Timing

When dealing with solar system objects, the mid exposure time (time of the shutter opening plus half of the exposure time) is of particular importance. DECam has a shutter that takes a while (about 1s) to cross the focal plane, so the actual mean of the exposed time depends on the position in the focal plane. To compensate for this feature, the mid exposure time was obtained by

Table 3. Overall uncertainty values

Mag. interval (1)	g r i z centroid (mas)				g r i z reference stars (mas)			
	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
18 \leq mag $<$ 19	7	5	5	5	14	11	11	10
19 \leq mag $<$ 20	11	6	5	6	14	12	11	10
20 \leq mag $<$ 21	17	9	7	8	15	12	11	11
22 \leq mag	26	13	10	12	15	15	12	12

NOTE—Column 1 (1): magnitude interval. Columns (2) to (5): precision in the determination of the centroid of TNOs and Centaurs as a function of the magnitude in a given filter. Columns (6) to (9): RMS of the reference stars as a function of the magnitude in a given filter. Note: these magnitudes do not correlate directly to those from Gaia.

adding

$$0.5 \times (\text{exposure time} + 1.05s) \quad (3)$$

to the value of the MJD as read from the image headers (see [Flaugh et al. 2015](#)). This becomes particularly relevant when dealing with objects in the inner solar system.

4.5. Detection efficiency

In Fig. 4 we show the detection efficiency as measured by the number of observed positions divided by the number of images for a given object. This figure has contributions from all images matched to objects in Tables 5 and 6, including those taken under non photometric sky. This efficiency justifies the more favorable detection statistics shown in Table 4 (column 3) as compared to the initial estimates given by Table 1. It is true that this latter, as opposed to Table 4, considers only those objects for which the uncertainty in the ephemeris is $\leq 2''$. However, Table 5 alone, with 114 entries, corroborates this better performance.

4.6. Orbits

Orbit refinement is a straight forward process with NIMA, once positions are obtained. One ephemeris (*bsp* format) file is provided for each of the 177 TNOs and each of the 25 Centaurs (see Table 4), from which the J2000 equatorial heliocentric state vector of each

Table 4. General numbers from images containing known TNOs and Centaurs

Type	Total	Ast	Pos	g	r	i	z	griz
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
TNO	270	177	3454	54	93	75	48	34
Centaur	67	25	545	9	6	9	6	3

NOTE—Columns (2): total number of objects at start. Column (3): total number of objects with at least one position determined. Column (4): total number of positions determined. Columns (5) to (8): number of objects with at least 3 magnitude measurements in each indicated filter. Columns (9): number of objects with at least 3 magnitude measurements in each the four filters. Note: there were 4 positions measured in the *Y* band and none measured in the *u* band.

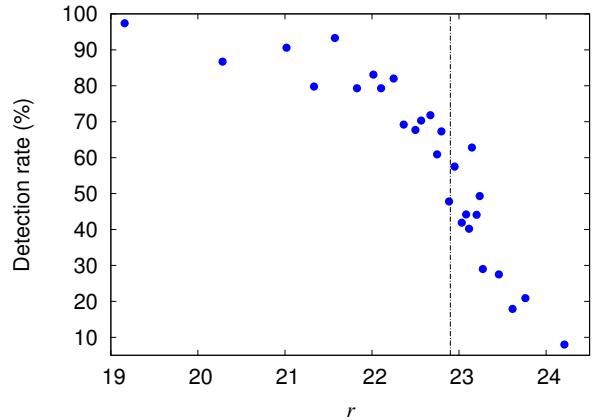


Figure 4. Detection efficiency as a function of the magnitude. No constraints on image quality are applied. The median limiting magnitude in the *r*-band (22.9), when accounting for τ is indicated by the vertical dashed line. Only TNOs and Centaurs in Tables 5 to 6 with at least one measured magnitude in the *r* band were considered.

body at any time⁶ can be obtained with the help of the SPICE/NAIF tools.

As far as stellar occultations are concerned, it is enough to be aware of an occultation event one or two years in advance so that the object's ephemeris can be more intensively refined, if necessary, and the respective observation missions for the occultation can be organized. In this way, these ephemerides should be suffi-

⁶ Limited to an interval of few decades (for instance, 2015 to 2025) to avoid large files.

ciently accurate for 1-2 years after the most recent observations and constant updates must be provided. Ideally, we consider an ephemeris to be sufficiently accurate when its 1σ uncertainty is smaller than the angular size of the respective occulting body and very few objects – (10199) Chariklo and Pluto among them – profit from such ephemerides. Observations like those from the DECam are invaluable to change this scenario.

One disadvantage of the *bsp* files is that they do not carry information on uncertainties. Our dedicated website provides an orbit quality table in which uncertainties are given in steps of 6 months to each target. These uncertainties vary from few to hundreds of mas, depending mainly on the astrometric quality of the current epoch of observations.

The result of an ephemeris refinement is illustrated by Figs. 2 (object from the Table 6) and 6, panel (a) (object from Table 5). They compare the refined orbit with its counterpart from the JPL and show the uncertainty of the refined orbit along with the recently observed positions of the respective solar system body. Among others, it helps to have a first idea of the work still needed to reach suitable uncertainties for successful predictions.

The waving pattern seen in Fig. 6, panel (a), is a common feature. It is a consequence of the different heliocentric distances of the solar system bodies as determined from NIMA and the JPL combined with the Earth’s motion around the Sun. Deep sky surveys like the DES also play a relevant role to improve the determination of these distances by providing observations at different phase angles.

Orbits determined in this work can be found from the address <http://lesia.obspm.fr/lucky-star/des/nima>. To each object, a text file lists the positions here determined as well as the respective observational history from AstDys⁷ (MPC, if the object is not found in the AstDys) that were used to determine the orbit. The 1σ orbit uncertainty ($\sigma_\alpha \cos \delta$ and σ_δ) is given for a period of two years in steps of six months from the last observation. Orbits themselves are available in *bsp* format. Details on the pages content are provided in a README file.

4.7. The $a \times e$ plane

One important feature of surveys like DES is the possibility to provide a better insight on dynamical theories as the number of objects on which such theories may be employable increase through new discoveries. This is illustrated with the help of Fig. 5.

⁷ <http://hamilton.dm.unipi.it/astdys/>

Considering explicitly the osculating elements, it is interesting to note that the MPC lists, to date, 48 objects with $q > 40$ AU and $a > 50$ AU. They constitute a conspicuous population of detached objects, for which mechanisms capable of increasing their perihelia is a subject of interest. Three of these – 2013 VD24, 2014 QR441, and 2005 TB190 – were observed by the DES, the first two being discovered by the survey. All of them are shown in Fig. 5.

Gomes (2011) showed that there is a path between a scattering particle, induced by the migration of the giant planets, and the stable orbit similar to that of 2004 XR190 (black square in Fig. 5, object not observed by the DES). This path results from a combination of Neptune’s migration and mean motion resonance (MMR) plus Kozai resonance. One of the features of this dynamical path is that the new stable orbits escape the Neptune’s MMR. The discovery of more objects by deep sky surveys with $q > 40$ AU and $a > 50$ AU may help to confirm this dynamical path.

2013 VD24 (close to the 5:2 resonance) and 2014 QR441 (close to the 7:2 resonance) are potentially among these objects. Numerical integrations of the equations of motion are necessary to check if they are not trapped in the resonances indicated in Fig. 5. A more detailed study is ongoing.

4.8. Occultation maps

A dedicated website also provides access to occultation prediction maps for the TNOs and Centaurs in this work.

These maps can be found from the address <http://lesia.obspm.fr/lucky-star/des/predictions> along with a link to specific ongoing campaigns where intense astrometric efforts are done to orbit improvement. These specific campaigns are those for which worldwide alerts are sent. The basic pieces of information given by the maps are as illustrated by Fig. 6 (b).

Prediction maps, plots with ephemeris uncertainties, as well as the respective ephemerides (*bsp* files) are available and are constantly updated at the websites mentioned earlier in the text.

5. COMMENTS AND CONCLUSIONS

We used 4,292,847 individual CCD frames from the DES collaboration to search for all known small bodies in the solar system. They represent a huge amount of high quality data, obtained by a single instrument and treated in a homogeneous and reproducible way.

Our procedure provided accurate positions from the DECam images and can be extended to other detectors. The correction for the chromatic refraction is a step to

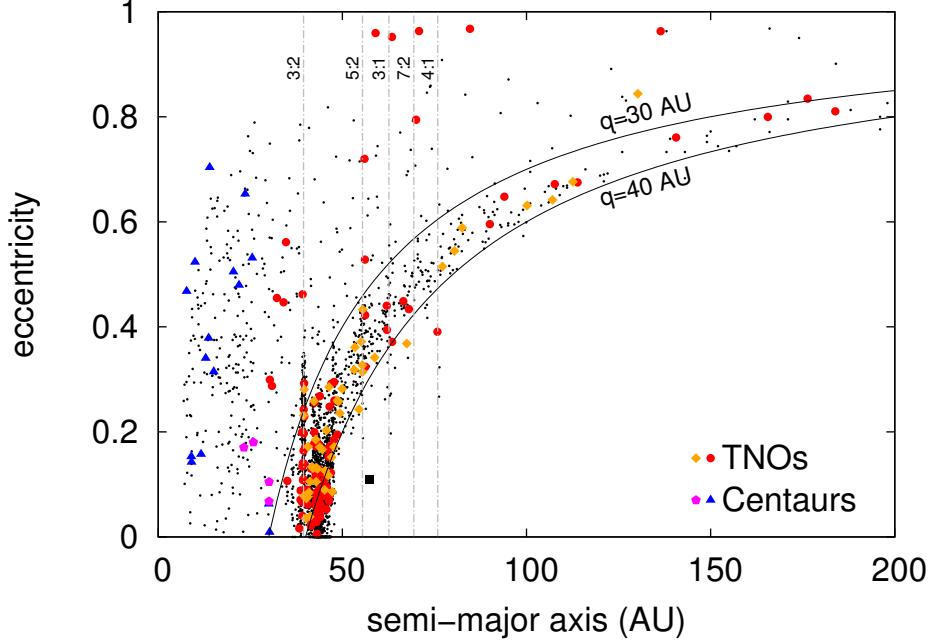


Figure 5. Distribution of the TNOs and Centaurs whose orbits were refined (red circles, orange diamonds, blue triangles and magenta pentagons), along with others taken from the MPC (small back dots), in the $a \times e$ plane. Some mean motion resonances (MMR) with Neptune are also indicated. Objects discovered by the DES are given by orange diamonds (Centaurs) and magenta pentagons (TNOs). The black square shows the scattered disk object 2004 XR190, not observed by the DES.

profit from the full excellence in space metrology of the instrument. Such a correction is in progress.

The whole procedure, from image retrieval from the DES database to the prediction of stellar occultations, is part of a pipeline that is being implemented in a high performance computational environment. Nevertheless, we interfered a number of times to check the data quality. As a result, the pipeline itself is refined.

The accuracy of the positions has a stronger dependence on the objects' magnitude than on its number of observations. This means that the low detection threshold adopted by PRAIA software to extract the faintest sources did not compromise the quality of the results.

Our detection efficiency is around 90% to $r < 22$ and we detect objects as faint as $r \sim 24$, more than 1 magnitude fainter than the average limiting magnitude in the same band. Again, this indicates that the faintest sources were found.

The basic results provided here (astrometry, orbits, and predictions to TNOs and Centaurs) are constantly updated as more observations from the DES or from other telescopes become available, the LSST being a natural continuation of this work. These results are available in dedicated websites.

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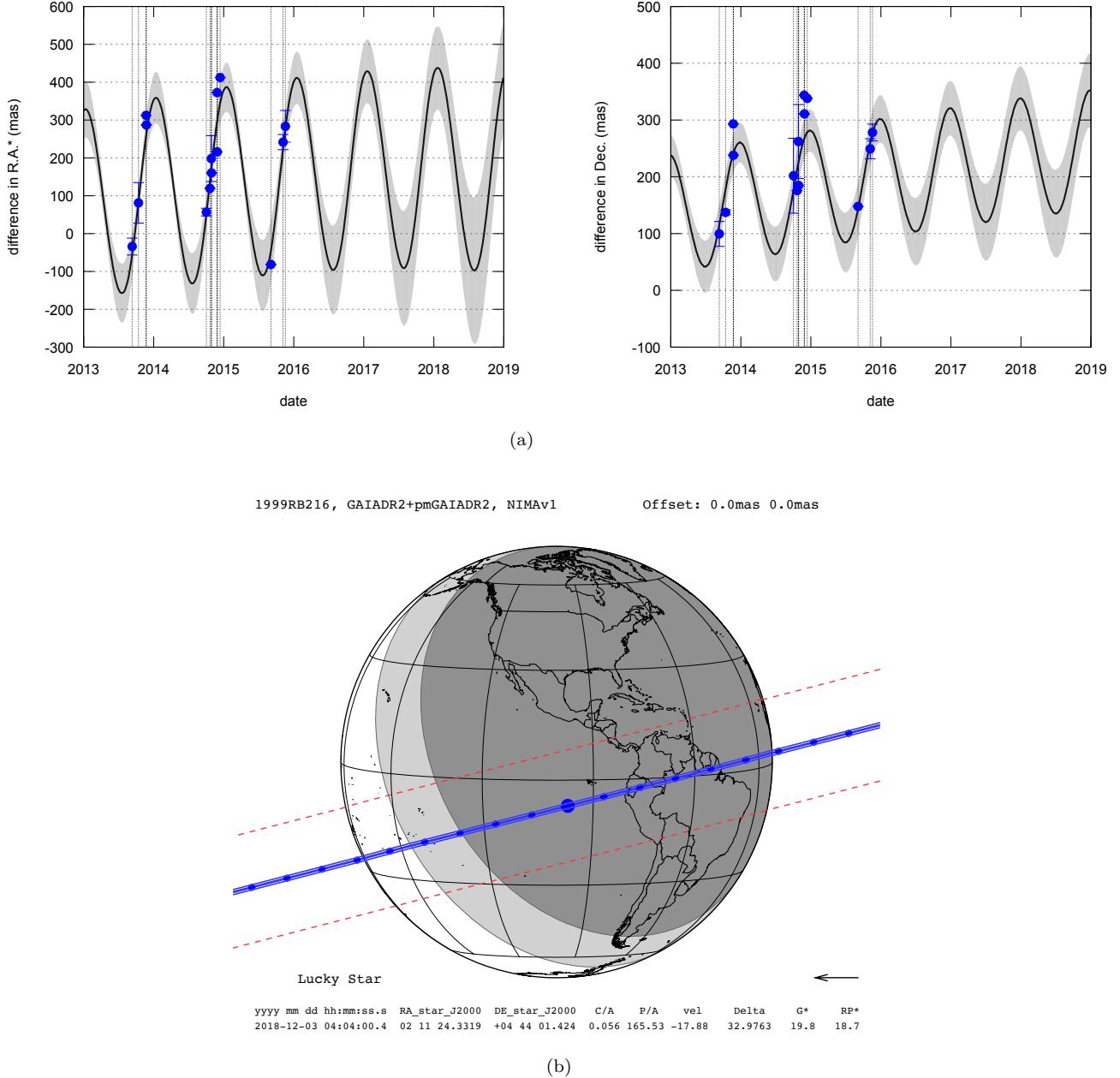


Figure 6. Example of prediction result and orbit refinement for TNO (137295) 1999 RB216 Panel (a): Same as Fig. 2 for the TNO (137295) 1999 RB216. The ephemeris JPL#18 is used to determine the differences NIMA minus JPL. This object belongs to the TNO main group, Table 5. Panel (b): occultation map, telling date and time (UTC) of the closest approach (largest blue point) between the shadow path and the geocenter, equatorial coordinates of the candidate star to be occulted, the closest approach (angular distance as seen from the occulting body, in arcsec, between the geocenter and the largest blue dot), the position angle (angle measured, in degrees, from the north pole to segment linking the geocenter and the largest blue point, counted clockwise), an estimate of the shadow speed on the Earth (km s^{-1}), the geocentric distance of the occulting body (AU), the Gaia DR2 G magnitude of the occulted star normalized to a reference shadow speed of 20 km s^{-1} , and the magnitude of the occulted star from the Gaia DR2 red photometer also normalized to the same reference shadow speed. Dark and white areas indicate nighttime and daylight, respectively. The gray zone shows the limits of the terminator (see also Assafin et al. 2010, for a detailed description). The distance between the blue lines indicates the diameter of the occulting body. The prediction uncertainty is given by the red dashed lines. The arrow in the bottom right corner of the map indicates the sense of the shadow's movement.

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APPENDIX

A. ASTROMETRIC RESULTS

Table 5. Statistics from the reduction of TNOs and Centaurs - main sources.

Object Id.	App. Mag. ^a	RA-3 σ (mas) ^b	DE-3 σ	$\sigma_{\alpha} \cos \delta$ (mas)	σ_{δ} min. (s) max.	Exposure (5)	Positions (6)	Detections (7)	Images (8)	Filters (9)	Filters (10)	Filters (11)
TNO												
1999 OZ3	23.1 (0.1)	2015	928	69	68	200 200	6	6	6	6	6	6r
2001 QP297	23.2 (0.3)	2605	1889	152	152	90 90	4	4	4	15	15	2rli
2001 QQ297	23.19 (0.06)	2761	2168	285	134	90 90	6	6	6	20	20	2r
2001 QQ322	22.8 (0.2)	3154	1736	180	165	90 90	13	13	18	18	18	4r4i2z
2001 QS322	23.1 (0.1)	1774	1399	91	103	90 90	12	13	13	21	21	6r2i2z
2003 QQ91	23.4 (0.1)	1802	1662	83	174	90 90	6	6	6	16	16	1rli
2003 QT91	23.5 (0.1)	3074	2141	60	89	90 90	4	4	4	15	15	1rli
2003 QV90	22.9 (0.1)	4122	2598	196	124	90 90	3	3	3	17	17	1i
2003 QY111	23.3 (0.4)	3386	2144	191	219	90 90	5	5	5	17	17	2r
2003 QZ111	23.2 (0.1)	4725	2510	172	63	90 90	11	11	11	19	19	3r3i
2003 SQ317	23.0 (0.1)	4030	1745	98	94	90 90	10	10	14	19	19	3g4r1i1z
2003 SR317	23.2 (0.1)	438	311	174	115	90 90	4	4	4	15	15	1rli
2003 UJ292	22.6 (0.4)	474	294	135	90	90 90	5	5	5	9	9	2i2z
2004 SC60	22.886 (0.008)	177	151	39	53	90 90	7	7	7	7	7	2g3r1i1z
2006 QF181	23.31 (0.09)	258	196	73	118	90 90	4	4	4	22	22	2rli
2006 QQ180	23.3 (0.1)	1373	973	116	98	90 90	15	15	15	19	19	1g4r2i5z
2006 UO321	23.5 (0.1)	333	279	274	204	90 90	10	10	10	22	22	1g2r2i
2007 TD418	24.27 (0.06)	2190	738	154	123	90 200	26	29	29	133	133	4g6r4i2z
2007 TZ417	23.7 (0.2)	1356	1598	56	276	90 90	14	14	14	31	31	4g5rli
2010 RD188	22.17 (0.02)	1718	1630	429	209	90 90	13	13	13	13	13	3g4r3i3z
2010 RF188	23.4 (0.1)	437	285	262	58	90 90	10	10	10	12	12	1g3r4i2z
2010 RF64	21.5 (0.1)	2213	1188	175	94	90 90	11	11	11	16	16	3g3r3i1z

Table 5 continued

Table 5 (continued)

Object Id.	App. Mag. a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha}\cos\delta$ (mas)	σ_{δ} (mas)	Exposure min. (s) max.	Positions (8)	Detections (9)	Images (10)	Filters (11)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
2010 RO64	22.12 (0.05)	141	128	37	43	90 90	4	4	10	2g1r1i
2010 TJ	22.00 (0.04)	1854	1785	102	95	90 90	13	14	15	2g3r2i4z
2010 TY53	20.90 (0.07)	138	176	37	13	90 90	19	20	20	6g7r1i5z
2012 TC324	22.81 (0.06)	122	103	97	119	90 90	24	24	26	5g3r5i6z
2012 TD324	23.1 (0.1)	708	444	260	181	90 90	9	9	14	4g1r1i2z
2012 YO9	23.6 (0.2)	1711	1759	169	174	90 200	22	25	174	5r2i
2013 QP95	23.4 (0.1)	144	261	93	67	90 400	203	218	321	20g21r40i84z
2013 RB98	23.5 (0.1)	870	1004	190	117	90 200	51	53	92	4g11r12i13z
2013 RD98	24.13 (0.06)	314	399	163	137	90 400	165	188	655	4g25r32i19z
2013 RR98	23.85 (0.02)	3450	3244	98	129	90 90	14	16	30	2g2r4i5z
2013 SE99	24.0 (0.1)	982	1195	226	232	150 400	30	46	479	3i
2013 SZ99	23.6 (0.2)	458	357	273	349	90 90	6	6	19	1r1i
2013 TH159	24.2 (0.2)	5163	3873	171	158	200 400	41	60	670	1g7r1i
2013 TM159	23.3 (0.2)	727	486	129	122	90 90	17	17	24	2g3r4i3z
2013 UK15	23.2 (0.1)	4669	2236	248	58	90 90	3	3	6	1r1i
2013 UO15	22.9 (0.1)	320	254	56	96	90 90	4	4	10	1r1i
2013 UQ15	23.440 (0.004)	473	387	120	86	90 90	5	5	11	2g3r
2013 UR15	23.7 (0.2)	492	336	168	77	90 90	6	6	16	1g1r2i
2014 GE54	22.81 (0.07)	151	128	41	43	150 150	20	21	35	6g6r4i3z
2014 LO28	21.69 (0.08)	213	107	30	37	90 90	13	13	14	5g3r3i1z
2014 OD394	22.93 (0.08)	3146	663	56	40	90 90	6	6	14	1g2r2i1z
2014 OQ394	22.29 (0.09)	152	114	55	79	90 90	7	7	8	3r2i1z
2014 OR394	22.7 (0.1)	241	165	100	185	90 90	4	4	5	1r1i1z
2014 QA442	21.113 (0.003)	272	290	114	52	90 90	10	10	26	2g4r2i2z
2014 QC442	23.3 (0.1)	2772	683	363	58	90 90	4	5	9	1g1r1l1z
2014 QE442	23.73 (0.05)	4058	2250	90	104	90 200	10	17	37	3g1r4i

Table 5 continued

Table 5 (continued)

Object	App. Mag.	RA-3 σ	DE-3 σ	$\sigma_{\alpha}\cos\delta$	σ_{δ}	Exposure	Positions	Detections	Images	Filters
Id.	^a	(mas) ^b	(mas)	mas)	mas)	min. (s) max.	(8)	(9)	(10)	(11)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
2014 QF442	23.8 (0.3)	5780	5998	149	151	90 90	13	14	25	3g4r2i
2014 QG442	23.03 (0.05)	3160	3239	140	272	90 90	14	14	22	4g4r6i
2014 QL441	22.8 (0.2)	2024	683	136	130	90 200	73	102	111	11g14r16i29z
2014 QM441	23.5 (0.2)	1225	470	152	110	90 200	70	86	153	6g15r21i21z
2014 QR441	23.7 (0.1)	1625	2738	130	87	90 200	83	93	177	11g22r19i17z
2014 QU441	26.0 (0.1)	5857	3317	117	104	90 200	27	29	106	1g8r5i1z
2014 SK349	22.7 (0.1)	248	190	33	54	90 90	21	22	22	6g5r6i4z
2014 SQ350	24.00 (0.08)	3726	2697	112	126	90 400	44	53	208	5g9r12i22z
2014 SZ348	24.44 (0.08)	911	1313	131	115	90 400	197	239	515	7g36r52i45z
2014 TT85	23.6 (0.2)	620	845	168	149	90 200	31	39	260	6r6i
2014 UF224	24.1 (0.1)	1050	1558	158	163	90 400	84	105	499	3g15r14i7z
2014 UZ224	23.75 (0.02)	2322	3439	89	75	90 90	13	13	19	2g4r5i1z
2014 XY40	23.01 (0.05)	2780	2735	138	87	90 90	13	13	15	3g4r3i3z
2015 PD312	23.6 (0.1)	5337	2765	172	125	90 200	16	21	55	1g4r4i
2015 PF312	22.82 (0.07)	1832	726	75	68	90 200	37	39	57	8g10r8i7z
2015 RR245	22.624 (0.001)	118	90	19	54	90 90	5	5	6	2g2r1i
2015 RT245	22.9 (0.1)	1582	1000	113	70	90 90	9	9	16	3r4i2z
2015 RU245	23.9 (0.2)	4749	799	88	111	90 90	9	13	20	1g2r2i
2015 RW245	23.11 (0.09)	5624	5717	655	445	90 90	6	6	16	1r1i1z
2015 TS350	23.06 (0.09)	866	2444	51	79	90 90	7	8	11	1g1r4z
2015 UK84	23.22 (0.08)	5265	5214	40	98	90 90	14	14	19	2g3r4i5z
(119956) 2002 PA149	23.2 (0.1)	2322	1471	177	139	90 90	11	11	16	1g2r4i2z
(120348) 2004 TY364	21.01 (0.09)	182	209	71	28	90 90	19	19	19	4g6r4i4z
(134210) 2005 PQ21	23.5 (0.1)	1828	1179	89	50	90 90	8	8	18	1g2r2i
(136199) Eris 2003 UB313	19.05 (0.02)	120	109	8	8	90 90	21	22	22	6g3r5i7z
(137295) 1999 RB216	23.1 (0.1)	777	382	143	82	90 90	25	25	26	6g6r6i6z

Table 5 *continued*

Table 5 (continued)

Object Id.	App. Mag. a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha}\cos\delta$ (mas)	σ_{δ} (mas)	Exposure min. (s) max.	Positions (8)	Detections (9)	Images (10)	Filters (11)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
(139775) 2001 QG298	22.5 (0.2)	127	101	44	46	90 90	14	14	14	4g4r2i4z
(143707) 2003 YU117	20.97 (0.08)	128	99	20	82	90 90	3	3	4	1i2z
(144897) 2004 UX10	21.00 (0.02)	75	76	48	20	90 90	6	6	6	1g3r1i1z
(145452) 2005 RN43	20.36 (0.08)	104	77	8	10	90 90	11	11	11	3g2r2i4z
(145474) 2005 SA278	22.6 (0.1)	153	138	43	25	90 90	19	19	22	7g4r5i2z
(145480) 2005 TB190	21.65 (0.09)	108	73	79	30	90 90	19	19	19	6g4r4i4z
(184212) 2004 PB112	23.9 (0.2)	1376	1124	122	101	90 90	8	8	10	1g2r3i1z
(303775) 2005 QU182	21.26 (0.03)	140	128	88	50	90 90	9	9	10	1g1r3i4z
(307616) 2003 QW90	22.25 (0.03)	99	76	31	50	90 90	16	17	19	4g3r5i4z
(309239) 2007 RW10	21.67 (0.07)	89	91	47	20	90 90	16	17	17	4g3r5i4z
(385191) 1997 RT5	23.3 (0.2)	2466	1746	116	58	90 90	7	7	16	3r4i
(385199) 1999 OE4	23.16 (0.05)	594	498	60	31	200 200	6	6	6	6r
(385201) 1999 RN215	22.9 (0.3)	1936	1607	127	247	90 90	6	6	17	3r2i
(385458) 2003 SP317	23.49 (0.04)	2827	1930	101	34	90 90	6	6	21	2r1z
(437360) 2013 TV158	22.8 (0.1)	101	121	52	46	90 400	438	467	504	44g72r10i1214z
(44594) 1999 OX3	20.972 (0.005)	90	66	14	20	90 90	9	9	9	2g3r2i2z
(451657) 2012 WD36	24.0 (0.1)	376	416	156	129	90 200	46	51	195	4g12r6i2z
(455171) 1999 OM4	23.2 (0.1)	584	574	32	76	200 200	6	6	6	6r
(469372) 2001 QF298	22.0 (0.1)	123	97	34	49	90 90	16	16	16	4g4r4i4z
(469750) 2005 PU21	23.24 (0.07)	137	97	122	73	90 90	19	20	21	4g4r4i5z
(47171) Lempo 1999 TC36	20.59 (0.04)	76	66	32	18	90 90	11	12	12	2g2r4i3z
(471954) 2013 RM98	22.4 (0.2)	121	92	79	67	90 150	18	18	21	7g3r5i3z
(472262) 2014 QN441	22.8 (0.2)	113	148	60	40	90 200	90	94	109	14g19r20i36z
(480017) 2014 QB442	23.3 (0.1)	148	125	64	42	90 90	19	21	26	3g6r5i5z
(483002) 2014 QS441	22.2 (0.2)	586	601	70	85	90 200	26	27	49	6g6r5i9z
(491767) 2012 VU113	24.0 (0.2)	285	404	181	108	90 200	40	47	107	3g14r7i4z

Table 5 continued

Table 5 (continued)

Object	App. Mag.	RA-3 σ	DE-3 σ	$\sigma_{\alpha}\cos\delta$	σ_{δ}	Exposure	Positions	Detections	Images	Filters
Id.	^a	(mas) ^b	(mas)	(mas)	min. (s) max.	(s)	(8)	(9)	(10)	(11)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
(491768) 2012 VV113	23.6 (0.1)	448	545	163	139	90 200	32	38	196	4r8i2z
(495189) 2012 VR113	23.3 (0.1)	359	310	97	92	90 200	74	78	114	7g16r17i21z
(495190) 2012 VS113	23.5 (0.1)	515	426	119	68	90 400	191	200	254	24g32r52i70z
(495297) 2013 TJ159	23.2 (0.1)	2334	1310	77	58	90 150	17	18	24	1g3r5i4z
(503883) 2001 QF331	23.458 (0.007)	344	271	138	89	90 90	11	11	17	2g3r3i1z
(504555) 2008 SO266	22.3 (0.2)	121	134	38	51	90 90	19	19	19	6g6r4i3z
(504847) 2010 RE188	22.8 (0.1)	286	198	99	45	90 90	4	4	5	1g1r1i1z
(505412) 2013 QO95	23.4 (0.1)	439	371	76	105	90 200	46	52	81	7g10r12i12z
(505446) 2013 SP99	23.3 (0.2)	416	280	178	132	90 90	8	8	17	2r2i
(505447) 2013 SQ99	23.2 (0.1)	322	239	129	57	90 90	10	10	19	1g2r4i
(505448) 2013 SA100	23.4 (0.3)	352	258	65	83	90 90	15	15	20	2g4r6i2z
(505476) 2013 UL15	23.8 (0.2)	392	253	78	69	90 90	4	4	11	1g3r
(508338) 2015 SO20	22.5 (0.1)	127	105	49	27	90 90	17	19	20	4g4r5i3z
(87555) 2000 QB243	23.8 (0.1)	2956	2056	68	102	90 90	6	6	7	1g2r2i1z
Centaur										
2004 DA62	23.30 (0.03)	1471	4914	90	36	90 90	4	4	15	2r2i
2007 UM126	22.5 (0.1)	4629	815	83	54	90 90	18	19	22	7g4r5i1z
2011 SO277	23.3 (0.1)	420	368	45	64	90 90	16	17	19	4g1r6i4z
2012 PD26	22.72 (0.09)	1591	783	311	172	90 90	11	13	15	5g2r1i2z
2013 RG98	23.3 (0.1)	264	780	85	78	90 400	207	224	271	23g31r4i97zY
2014 OX393	22.70 (0.06)	779	452	86	62	90 90	4	4	5	1g1r1i1z
2014 QO441	23.63 (0.06)	254	350	87	97	90 400	119	145	301	13g19r3i134z
2014 QP441	23.8 (0.3)	866	593	111	95	90 400	74	123	436	2g17r17i11z
2014 SB349	23.80 (0.04)	2793	1964	110	39	90 200	12	18	62	2g3r4i2z

Table 5 *continued*

Table 5 (continued)

Object Id.	App. Mag. ^a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha}\cos\delta$ (mas)	σ_{δ} (mas)	Exposure min. (s) max.	Positions (8)	Detections (9)	Images (10)	Filters (11)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
2014 SS303	22.07 (0.05)	5559	2124	71	52	90 90	4	5	7	1r1i2z
2015 RV245	23.61 (0.07)	2878	3169	260	23	90 90	4	4	7	2g1r1i
2015 VV1	21.77 (0.03)	85	87	27	36	90 90	4	4	4	1g2r1i
(2060) Chiron 1977 UB	18.5 (0.2)	53	50	18	13	90 90	7	7	7	3g1r1i2z
(47265) 2014 SR303	22.0 (0.2)	95	79	27	30	90 90	18	19	22	6g6r3i3z

NOTE—Column (1): Object identification. Those discovered by the DES are highlighted. Column (2): Average magnitude as obtained from the bluest filter. Columns (3) and (4): 3σ uncertainty in the ephemeris position in RA and Dec, respectively. Columns (5) and (6): standard deviations as obtained from the observed positions minus those from the respective JPL ephemeris, in RA and Dec respectively. Column (7): minimum and maximum exposure times of the images from which a position was obtained. Columns (8),(9), and (10): number of detections delivered by the astrometric code (all positions, no eliminations), and total number of images with exposure times greater than or equal to 50 seconds, respectively. Column (11): Number of magnitudes per filter found to a given object in the DES database. Note that the total number of filters in each row of column (11) is always less than or equal to the respective number of positions in Column (8). This is because either a magnitude was not found in the DES database for a given position or the position itself was not found in the DES database.

^aBluest magnitude from the DES. If no magnitude from the DES is available, V magnitude given the the JPL - Horizons System

^b is used.

^b As provided by the JPL, Horizons System.

Table 6. Statistics from the reduction of TNOs and Centaurs - extension sources.

Object Id.	App. Mag. ^a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha} \cos \delta$ (mas)	σ_{δ} min. (s) max.	Exposure (7)	Positions (8)	Detections (9)	Images (10)	Filters (11)
(1)	(2)	(3)	(4)	(5)	(6)					
TNO										
(160091) 2000 OLF67	23.2 (0.2)	15828	7732	42	61	90 90	6	6	16	2r2i1z
2013 RP98	23.58 (0.08)	20450	5490	57	62	90 90	7	7	15	2g1r3i1z
2013 RQ98	23.0 (0.2)	27691	13113	80	115	90 90	7	11	29	3r2i
(160256) 2002 PD149	23.6 (0.2)	17727	8159	150	90	90 90	7	7	14	1g2r1i1z
2003 QX111	23.0 (0.2)	9090	3775	98	106	90 90	9	11	19	2r4i3z
2014 SR350	23.1 (0.1)	20122	7973	97	88	90 90	9	12	26	4r3i
2015 PL312	23.94 (0.08)	30292	15722	112	169	90 400	9	23	199	3r
2014 UY224	23.53 (0.06)	9915	9898	103	126	90 90	12	12	19	2g4r3i1z
2014 UC225	23.39 (0.09)	11304	6057	128	97	90 90	13	13	21	3g5r3i2z
2014 UN225	23.1 (0.1)	32391	24659	43	49	90 90	14	16	17	4g3r4i2z
2014 VW37	23.3 (0.1)	3657	7506	120	93	90 90	18	18	21	4g3r5i4z
2013 RF98	24.1 (0.1)	6582	6114	87	109	200 400	30	55	301	5r71z
Centaur										
2013 PQ37	19.93 (0.06)	31300	12480	0.053	0.016	90 90	7	7	7	2r2i3z

NOTE—Same as for Table 5.

Table 7. Statistics from the reduction of TNOs and Centaurs - doubtful sources.

Object Id. (1)	App. Mag. ^a (2)	RA-3 σ (mas) ^b (3)	DE-3 σ (mas) ^b (4)	$\sigma_{\alpha} \cos \delta$ (mas) (5)	Exposure min. (s) max. (6)	Positions (7)	Detections (8)	Images (9)	(10)	(11)	Filters
TNO											
1996 RR20	22.802 (0.006)	7994	3676	221	177	90 90	4	4	15	2i1z	
1999 RG215	23.7 (0.2)	2919	1919			90 90	1	1	9	1r	
1999 RK215	24.23	2590	2135			90 90	1	1	15		
2000 PC30	23.8 (0.2)	47499	19797	174	74	200 200	4	4	6	3r	
2000 PY29	23.9 (0.2)	9129	4247	97	97	200 200	4	4	6	1r	
2000 QD226	23.65	$> 10^6$	$> 10^6$			90 90	1	1	21		
2001 QH298	22.88 (0.09)	1824	1851			90 90	1	1	16	1g	
2001 QO297	23.6 (0.2)	22524	9941	154	148	90 90	3	3	19	1g1r1i	
2002 PD155	23.53	20548	11298			90 90	1	1	22		
2002 PG150	21.61 (0.07)	$> 10^6$	$> 10^6$			90 90	1	1	13	1z	
2002 PK149	22.48 (0.09)	$> 10^6$	$> 10^6$			90 90	1	1	12	1g	
2003 QB91	23.1 (0.1)	11356	521.5	493	51	90 90	4	4	22	1r1i	
2005 PE23	26.93	$> 10^6$	$> 10^6$			90 90	1	1	21		
2005 PP21	22.88	$> 10^6$	$> 10^6$			90 90	1	1	11		
2005 SE278	22.19 (0.07)	1897	1498	47	30	90 90	2	2	3	1i1z	
2006 QC181	22.00 (0.05)	$> 10^6$	$> 10^6$			90 90	1	1	15	1g	
2006 QD181	22.88	$> 10^6$	$> 10^6$			90 90	1	1	13		
2006 QZ180	23.59	$> 10^6$	$> 10^6$			90 90	1	1	23		
2008 UA332	23.03 (0.08)	$> 10^6$	$> 10^6$			90 90	1	1	17	1g	
2010 JH124	23.2 (0.1)	20165	1810	798	1.050	90 150	3	3	43	1r1i	
2013 KZ18	21.65	136	104			90 90	1	1	4	1z	
2013 RO98	22.74 (0.08)	$> 10^6$	$> 10^6$	44	72	90 90	16	16	18	4g4r4i4z	

Table 7 continued

Table 7 (continued)

Object Id.	App. Mag. ^a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha} \cos \delta$ (mas)	σ_{δ} min. (s) max.	Exposure Position	Detections	Images	Filters	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
2013 UP15	24.06	370	260	90	90	1	1	7		
2013 VD24	24.6 (0.2)	107390	54984	113	172	330 400	5	9	408	1r
2013 VJ24	23.90	$> 10^6$	$> 10^6$	90	90	1	1	15		
2014 NB66	22.86 (0.02)	217	115	50	69	90 90	2	2	4	2g
2014 PR70	22.98 (0.07)	226	136	175	190	90 90	2	2	2	1g1z
2014 RS63	22.62 (0.06)	85434	52414	61	131	90 90	6	6	13	3l1z
2014 SN350	22.87 (0.09)	28123	37105	169	147	90 90	6	6	21	3r1i
2014 SO350	24.0 (0.2)	91741	33931	229	67	90 90	7	8	23	1g2r3i
2014 TB86	23.2 (0.1)	165206	42723	68	69	90 90	9	11	23	1g3r2l2z
2014 TE86	23.2 (0.3)	23334	38078	190	140	90 90	9	9	19	2g3r1i
2014 TF86	23.5 (0.2)	47829	27854	150	119	90 90	12	12	26	1g5r2l2z
2014 TU85	23.38 (0.02)	860527	132551	256	95	90 200	4	4	46	2r1i
2014 UA225	23.37 (0.06)	441418	196689	66	89	90 90	11	11	22	3g2r3l3z
2014 UB225	22.74 (0.05)	$> 10^6$	$> 10^6$	57	41	90 90	7	7	10	3r1l2z
2014 VT37	24.06 (0.09)	196302	93079	106	123	150 200	11	11	74	2g3r1i
2014 YL50	23.4 (0.1)	43878	78972	129	178	90 90	12	12	14	4g3r3l1z
2014 XZ40	23.53 (0.02)	72326	56308	52	128	90 90	5	5	18	2g2r1i
2015 PK312	25.01	$> 10^6$	224438	330	1.328	90 330	3	3	133	
2015 QT11	24.3 (0.2)	465277	218826	188	179	150 400	9	11	239	1g2i
2015 RS245	24.05	46613	5685	833	929	90 200	4	4	87	
2015 RX245	24.35	1320	1461	161	446	90 90	2	2	28	
2015 SV20	22.56	$> 10^6$	$> 10^6$	90	90	1	1	13		
2015 TN178	21.4 (0.5)	175	641	267	371	90 90	2	2	2	2i
2016 QP85	23.6 (0.2)	$> 10^6$	306619	660	236	90 90	3	3	13	1r
(148112) 1999 RA216	22.7 (0.1)	2402	1746	190	216	90 90	2	2	12	1i
(307982) 2004 PG115	20.63 (0.01)	132	77			90 90	1	1	1	1r

Table 7 (continued)

Table 7 (continued)

Object Id.	App. Mag. ^a	RA-3 σ (mas) ^b	DE-3 σ (mas)	$\sigma_{\alpha} \cos \delta$ (mas)	σ_{δ} min. (s) max.	Exposure Position	Detections	Images	Filters	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
(474640) 2004 VN112	23.42	748	816		90 90	1	1	1		
(501581) 2014 OB394	21.42 (0.03)	136	97	37	90 90	2	2	2		1i1z
(506121) 2016 BP81	23.2 (0.1)	397	276	74	137	90 90	2	2	3	1g1i
Centaurs										
2007 VL305	22.7 (0.1)	11377	2924	266	245	90 90	3	3	7	1r
2011 OF45	21.12 (0.04)	565	334			90 90	1	1	1	1z
2013 RN30	22.6 (0.2)	7971879	5872040	516	1.049	90 90	3	3	22	2g1z
2013 SV99	24.1 (0.1)	2145099	1273035	192	151	90 400	16	20	55	4g2r5i
2013 TS20	21.83 (0.03)	36400409	14095067			90 90	1	1	6	1g
2014 SW223	21.83 (0.05)	762	545			90 90	1	1	1	1i
2014 TK34	21.14 (0.03)	310	197			90 90	1	1	1	1i
2015 VT152	23.5 (0.1)	1501899	1234480	112	41	90 90	6	9	16	1g2r3i
2016 VF1	21.71 (0.04)	53403030	272552177	644	1.161	90 90	3	3	20	1i
(471339) 2011 ON45	21.04 (0.07)	115	74			90 90	1	1	1	1z

NOTE—Same as for Table 5.

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