






Jet Archaeology and Forecasting: Image Variability and Magnetic Field Configuration

Yuh Tsunetoe^{1,2} , Ramesh Narayan^{1,3} , and Angelo Ricarte^{1,3} ¹ Black Hole Initiative, Harvard University, 20 Garden Street, Cambridge, MA 02138, USA; ytsunetoe@fas.harvard.edu² Center for Computational Sciences, University of Tsukuba, 1-1-1 Tennodai, Tsukuba, Ibaraki 305-8577, Japan³ Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA

Received 2024 November 12; revised 2025 February 24; accepted 2025 March 3; published 2025 April 8

Abstract

We investigate how magnetic field variations around accreting black holes (BHs) on event horizon scales affect the morphology of magnetically driven jets on larger scales. By performing radiative transfer calculations on general relativistic magnetohydrodynamics simulations, we find that temporal variation in the magnetic flux on the event horizon and the jet power are imprinted on the variability of jet width up to several hundred gravitational radii. When the magnetic flux around the BH drops and then rises, the jet initially narrows or becomes truncated, then widens, creating a thin-thick pattern that propagates down the jet. This suggests that extended jet observations can provide a history record of horizon-scale magnetic field dynamics, and conversely, upcoming changes in the jet image can be predicted from direct observation of the magnetized accreting plasma near the BH. Furthermore, the pattern of jet width variations shows acceleration up to the relativistic regime as it moves away from the BH, aligning with plasma bulk motion. We also find in time-averaged images that both the bulk plasma motion and magnetic field configuration in the jet-launching region, which are sensitive to BH spin, shape diverse features through relativistic beaming and aberration. Higher BH spins result in more poloidal bulk motion and toroidal magnetic fields, leading to more symmetric jet images and linear polarization patterns. These results suggest a new method for testing the magnetically arrested disk model and the Blandford–Znajek process, and for determining the BH spin through observations bridging horizon and jet-launching scales.

Unified Astronomy Thesaurus concepts: [Black hole physics \(159\)](#); [Event horizons \(479\)](#); [Relativistic jets \(1390\)](#); [Active galactic nuclei \(16\)](#); [Radio jets \(1347\)](#); [Radiative transfer \(1335\)](#); [Polarimetry \(1278\)](#)

Materials only available in the online version of record: [animation](#)

1. Introduction

In recent years, very long baseline interferometer observations by the Event Horizon Telescope Collaboration have achieved direct imaging of supermassive black holes (BHs) in the centers of nearby galaxies on event horizon scales (Event Horizon Telescope Collaboration et al. 2019a, 2022; see also R.-S. Lu et al. 2023). M87, one of the primary targets, has a well-studied jet that has now been imaged from scales of sub-Mpc to ~ 80 kpc (e.g., F. de Gasperin et al. 2012; K. Hada et al. 2016; R. C. Walker et al. 2018; R.-S. Lu et al. 2023). Upgrades and extensions to the Event Horizon Telescope (EHT) via the next-generation EHT (ngEHT) project and Black Hole Explorer (BHEX) will achieve at least a resolution of $5 \mu\text{as}$ (microarcseconds) at 230 GHz and a dynamic range close to 1000, from which movies connecting the inner accretion disk to the jet will be possible (S. S. Doeleman et al. 2023; M. D. Johnson et al. 2024). Thus, jet simulations providing detailed predictions at high resolution and in the time domain are of timely importance.

So far, polarized EHT images favor strongly magnetized magnetically arrested disk (MAD) models over their more weakly magnetized standard and normal evolution counterparts, the latter of which tend to be more weakly polarized and less consistent with multiwavelength constraints (Event Horizon Telescope Collaboration et al. 2021a, 2019b, 2024a). In MAD models, the magnetic field advected along with the

accreting plasma saturates and becomes dynamically important, leading to non-axisymmetric structures in the inflow and efficient launching of jets (I. V. Igumenshchev et al. 2003; R. Narayan et al. 2003). MADs also exhibit disruptive magnetic reconnection or “flux eruption events,” which offer an electron acceleration mechanism hypothesized to explain multiwavelength polarized flares (e.g., J. Dexter et al. 2020; K. Chatterjee & R. Narayan 2022; B. Ripperda et al. 2022; M. Najafi-Ziyazi et al. 2024). MAD models accelerate efficient relativistic jets powered by the spin-energy of the BH, tapped by magnetic fields threading the horizon (R. D. Blandford & R. L. Znajek 1977; BZ process; see also A. Tchekhovskoy et al. 2011). It will be important to verify predictions of MAD models with observations in the jet-launching region as well.

Previous observational studies have explored variable features of parsec-scale jets after X- and gamma-ray flares (for example, light curve; A. B. Pushkarev et al. 2010; relativistic blobs; S. G. Jorstad et al. 2001, 2013; jet orientation; B. Rani et al. 2014; and jet base; K. Niinuma et al. 2015; M. M. Lisakov et al. 2017; see also O. Porth et al. 2021 for infrared flares in the Galactic center). These high-energy flares can be associated with eruptive events in the vicinity of the BH (F. Tavecchio et al. 2010; B. Rani et al. 2014; A. E. Broderick & A. Tchekhovskoy 2015; see also F. K. Schinzel et al. 2012; A. P. Marscher 2014 for another possibility of the flares taking place far from the BH). Most recently, the Event Horizon Telescope-Multi-wavelength science working group et al. (2024b) reported changes in the position angle of the M87 jet orientation and the bright spot on the M87* ring at the same time with a gamma-ray flare in 2018, though the emission



Original content from this work may be used under the terms of the [Creative Commons Attribution 4.0 licence](#). Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.

origin of the flare and its relation to the jet orientation are uncertain.

Polarization images can also be a strong tool to address the magnetically driven jet mechanism and have attracted a large interest. An ordered linear polarization (LP) vector pattern has been detected around the photon ring (Event Horizon Telescope Collaboration et al. 2021b) and the extended jet (e.g., R. C. Walker et al. 2018), which implies the existence of a persistent magnetic field structure bridging these scales.

In theoretical approaches, polarization images have been suggested as a tool for inferring BH spin (D. C. M. Palumbo et al. 2020; A. Chael et al. 2023; R. Emami et al. 2023; R. Qiu et al. 2023; A. Ricarte et al. 2023b; Event Horizon Telescope Collaboration et al. 2024a), although interpreting these images can be challenging due to Faraday effects, particularly Faraday rotation. Studies have also investigated the Faraday effects on the polarization images around the BH (M. Mościbrodzka et al. 2017; A. Ricarte et al. 2020; Y. Tsunetoe et al. 2022), as well as relativistic effects from accelerated plasma bulk motion (R. A. Laing 1981; M. Lyutikov et al. 2005; A. E. Broderick & J. C. McKinney 2010; E. Murphy et al. 2013). It has also been suggested that circular polarization (CP) images can shed new light on the jet mechanism (Y. Tsunetoe et al. 2020, 2021; M. Mościbrodzka et al. 2021; A. Ricarte et al. 2021; Event Horizon Telescope Collaboration et al. 2023; A. V. Joshi et al. 2024).

On the scale of more extended jets, the effect of magnetic field helicity combined with viewing angle was examined in R. A. Laing (1981) and E. Murphy et al. (2013) using one-zone cylindrical jet models. J. A. Kramer & N. R. MacDonald (2021) calculated polarization images based on relativistic MHD jet models with different magnetic field configurations, obtaining a bimodal pattern of horizontal and vertical LP vectors to the jet (see also V. I. Pariev et al. 2003; O. Porth et al. 2011). J. Davelaar et al. (2023) also investigated the effect of waves on shearing flow surfaces on the LP features.

Motivated by this previous activity and by upcoming observations, we examine the relationship between the horizon-scale dynamical variability in MAD simulations and the polarized morphology of the jet-launching region in synthetic images. R. Narayan et al. (2022) surveyed the jet and disk morphology in MAD GRMHD simulations for a variety of BH spins and found that the prograde spin cases give wider jets up to $100 r_g$ scale than the retrograde cases (see Section 2.1 for details). Here, $r_g = GM/c^2$, G is the gravitational constant, M is the BH mass, and c is the speed of light. K. Chatterjee et al. (2023) also pointed out that the jet opening and tilt angles at $10 r_g$ are correlated and anticorrelated with the normalized magnetic flux, respectively. Recently, K. Moriyama et al. (2024) also started surveying the jet image variability and the spin dependence.

Here, we focus on the transverse structure of the inner jet image for an M87-like system on a scale $\lesssim 100 r_g$ ($\sim 0.003 \text{ pc} \sim 0.37 \text{ mas}$; milliarcseconds), which corresponds to $\lesssim 300 r_g$ if deprojected with the observer's inclination angle of $i = 163^\circ$ (or 17°). Since the plasma on these scales is being accelerated up to the relativistic regime, the jet morphology in the images is affected by relativistic beaming and aberration effects on the synchrotron radiation. With this in mind, we perform polarimetric general relativistic radiative transfer (GRRT) calculations based on MAD GRMHD models, to obtain theoretical prediction of images and investigate the

relationship between the plasma dynamics and observable image features.

This paper is organized as follows. Our methodology is introduced in Section 2, which consists of GRMHD simulations (Section 2.1) and GRRT calculations (Section 2.2). We describe our main results in Section 3, regarding the variability of jet shape in Sections 3.1 and 3.2 and the averaged image features in Section 3.3. Applications of our results are addressed in Section 4, including an estimation of the jet acceleration profile in Section 4.1, the variability of the jet width in Section 4.2, the correlation between the jet power and width in Section 4.3, the spin dependence of polarization images in Section 4.4, and comparison with observations and contribution of nonthermal electrons in Section 4.5. Finally, we present a summary and conclusions in Section 5.

2. Method

2.1. MAD GRMHD Models

We use as our starting point the GRMHD simulations in R. Narayan et al. (2022), in which the authors surveyed MAD models for nine BH spin values: $a_* \equiv a/M_* \in \{0, \pm 0.3, \pm 0.5, \pm 0.7, \pm 0.9\}$. They found that the prograde spin models ($a_* > 0$) had wider jets and thinner disks than the retrograde models ($a_* < 0$). In addition, they also pointed out that models with larger absolute spin values $|a_*|$ exhibited more variability in ϕ_{BH} , the normalized magnetic flux threaded on the event horizon ϕ_{BH} . Here,

$$\phi_{\text{BH}} \equiv \frac{\Phi_{\text{BH}}}{\sqrt{\dot{M} r_g^2 c}}, \quad (1)$$

$$\Phi_{\text{BH}} = \frac{1}{2} \iint \sqrt{-g} |B^r|_{r=r_{\text{H}}} d\theta d\phi, \quad (2)$$

where g is the determinant of the metric, B^r is the radial component of the three-vector magnetic field, and r_{H} is the radius of the event horizon.

Here, we select a subset of five BH spins, $a_* \in \{\pm 0.9, \pm 0.5, 0\}$. For each model, we ray trace snapshots separated by $50 t_g$ over a total duration of $5000 t_g$ in quasi-steady state, where $t_g = r_g/c$. The duration of $5000 t_g$ corresponds to about 5 yr in M87*, assuming $M_* = 6.5 \times 10^9 M_\odot$ (e.g., Event Horizon Telescope Collaboration et al. 2019b).

To determine the electron temperature, we implement the R - β prescription,

$$\frac{T_i}{T_e} = R_{\text{low}} \frac{1}{1 + \beta^2} + R_{\text{high}} \frac{\beta^2}{1 + \beta^2}, \quad (3)$$

where T_i and T_e are proton and electron temperatures, respectively, and β is the thermal-to-magnetic pressure ratio (M. Mościbrodzka et al. 2016). Here, the two parameters are set to $R_{\text{low}} = 1$ and $R_{\text{high}} = 160$, where we choose the latter because polarized studies of M87* prefer large values (Event Horizon Telescope Collaboration et al. 2023).

2.2. GRRT

We ray traced each GRMHD model snapshot using our polarimetric GRRT code SHAKO to calculate a series of images, or a movie (see Y. Tsunetoe 2023 for the details of code composition. See also the Appendix of Y. Tsunetoe et al. 2024 for comparison with another GRRT code ipole

(M. Mościbrodzka & C. F. Gammie 2018; G. N. Wong et al. 2022). It is well known that assuming thermal electron distribution functions (eDFs) is sufficient to explain the emission from the innermost accretion flow, but nonthermal electrons are required to reproduce extended jets (e.g., J. Davelaar et al. 2019; A. Cruz-Orsorio et al. 2022; C. M. Fromm et al. 2022). Therefore, we assume a combination of thermal and nonthermal synchrotron-emitting electrons, the latter of which are distributed in a power law (see Y. Tsunetoe 2023 and Y. Tsunetoe et al. 2024 for the radiative coefficients for thermal and power-law synchrotron emission, respectively).

The electron temperature of the thermal component is given by Equation (3). The power-law index and minimum and maximum Lorentz factors of the nonthermal electrons are fixed to $p = 2.5$, $\gamma_{\min} = 30$, and $\gamma_{\max} = 10^6$ in the whole region. The energy partition between thermal and power-law electrons, $u_{e,pl} = 0.03 u_{e,th}$, is assumed to determine the number density of power-law electrons (F. Yuan et al. 2003; J. Dexter et al. 2012; see also Section 4.5).

We set the observer’s screen at a distance of $r = 10^4 r_g$ with an inclination angle of $i = 163^\circ$ (17°) to the z -axis for the prograde (retrograde) spin cases. The radiative transfer is performed under the assumption of fast light, in which the plasma is stationary during the propagation of light rays. We cut out the region with the magnetization $\sigma_m \equiv b^2/4\pi\rho c^2 > 10$ to avoid regions where the density floor, used in the GRMHD code to maintain numerical stability, artificially injects material. Regions beyond $R = r \sin\theta > 200 r_g$ are also cut out because the accretion flow there may not be in equilibrium. We scale the particle density and magnetic fields from the scale-invariant ideal GRMHD simulation to reproduce an average flux of ~ 1 Jy at 230 GHz for each model. This is larger by a factor of 2 than the value of 0.5 Jy adopted for most EHT studies (e.g., Event Horizon Telescope Collaboration et al. 2019b) since we now include emission from the jet region, not just the “compact” shadow region around the BH.

In the following, we show the 86 GHz images with 260×520 pixels, convolved with a circular Gaussian beam with a full width at half-maximum (FWHM) of $40 \mu\text{as}$ (similar resolution to R.-S. Lu et al. 2023),⁴ unless otherwise noted.

3. Results

3.1. Truncation of Jet Associated with a Deficit of Magnetic Flux

We show eight total intensity snapshot images for the $a_* = -0.9$ model in Figure 1. Although $a_* = -0.9$ may be intrinsically unlikely (e.g., A. Ricarte et al. 2025), we showcase this model due to an illustrative flux eruption event we identified. They exhibit a large variability in jet morphology, reflecting large fluctuations in the magnetic field in the underlying MAD model. In particular, we focus on the two squared images at $t = 79,600 t_g$ and $81,300 t_g$. These two images exhibit a truncation and broadening of the approaching jet, exemplifying the dramatic temporal variability possible in MAD models.

⁴ We do not see a ring feature in the innermost region of the convolved images, while the observational images in R.-S. Lu et al. (2023) exhibit a ring with a diameter of $\approx 64 \mu\text{as}$. This is because the size of the photon ring, $\approx 10 r_g \approx 37 \mu\text{as}$, is smaller than the beam size $40 \mu\text{as}$ and remains unresolved. T. Ogiwara et al. (2024) obtained an $\sim 60 \mu\text{as}$ ring using a semianalytic funnel jet model, which consists of emission from the stagnation surface between the inflow and outflow plasmas in the funnel region.

Here, we focus on the variability of the normalized magnetic flux on the event horizon, ϕ_{BH} defined in Equation (1), as shown in the profile in Figure 1. In addition, we plot the jet power P_{jet} , the outflowing energy flux estimated from GRMHD data. The two bold dashed lines in the bottom panel of Figure 1 denote the times of the squared snapshot images at the top. During the time period marked with a blue arrow, ϕ_{BH} sharply drops, corresponding to a magnetic reconnection or “flux eruption” event. Since the jet power follows $P_{\text{jet}} \propto \phi_{\text{BH}}^2$ (R. D. Blandford & R. L. Znajek 1977; A. Tchekhovskoy et al. 2010), the jet temporarily loses power. The “truncated” jet in the top left panel thus represents a shorter newly recovered jet. In the time period marked by the orange arrow, the magnetic flux rapidly increases, leading to an increase in jet power. As a result, the jet profile becomes wider. At the slightly later time in the second dashed line, the jet has returned to a more moderate width as in the seventh panel at $t = 81,850 t_g$.

The above comparison shows that variations in ϕ_{BH} lead to variations in the jet width as a function of distance, due to causal variations in the jet power. In this way, the temporal history of ϕ_{BH} is encoded in the spatial variation of the jet width.⁵

3.2. Correlation of Jet Widths and Magnetic Flux

To verify the hypothesis of ϕ_{BH} -jet width correlation, we introduce a measure of jet width at altitudes of $y = 25, 50, 75, 100, 125$, and $150 r_g$ on the image.⁶ Here, we measure the width as the offset between the two edges, defined as the leftmost and rightmost pixels on the transverse profile where the total intensity exceeds 10^{-3} times the peak intensity. We set the peak intensity to $1 \times 10^{-4} [\text{erg s}^{-1} \text{cm}^{-2} \text{Hz}^{-1}] \approx 4.4 \times 10^{10} [\text{K}]$ in the brightness temperature, based on an average intensity over $5000 t_g$. The jet widths for a snapshot are denoted by the green horizontal lines in the left panel of Figure 2. In the right panel, we plot jet width as a function of time, along with the time variation of ϕ_{BH} and the total flux density at 86 GHz, which is obtained by integrating the total intensity over the image. Here, we disregard the absolute scales of the profiles and offset them for illustrative purposes.

We can see at a glance that the jet widths exhibit similar temporal variability to both ϕ_{BH} and the total flux, but with a time lag. As mentioned in the previous subsection, it is confirmed that the large drop in ϕ_{BH} around $t = 79,000 t_g$ is followed by a series of jet narrowing or truncation from downstream (small y) to upstream (large y), while the rise around $t = 81,000 t_g$ is followed by a horizontal expansion of the jet. The total flux also tends to show a similar variability to ϕ_{BH} , with a shorter time lag. This result implies that there is a strong connection between the horizon-scale dynamics and the extended jet image at scales hundreds of times larger. Thus, high-resolution imaging would enable “jet archeology” by allowing us to infer the temporal variation in ϕ_{BH} from the spatial variation in width. At the same time, light curves would enable “jet forecasting” by allowing us to predict future jet width profiles from variations in total flux.

⁵ In observations, K. Hada et al. (2016) reported a “constricted” structure at $\sim 0.2\text{--}0.3 \text{ mas}$ in M87 jet.

⁶ Note that because of the inclination, these y distances correspond to real physical distances of 85, 170, 255, 340, 425, and $510 r_g$ from the BH, respectively.

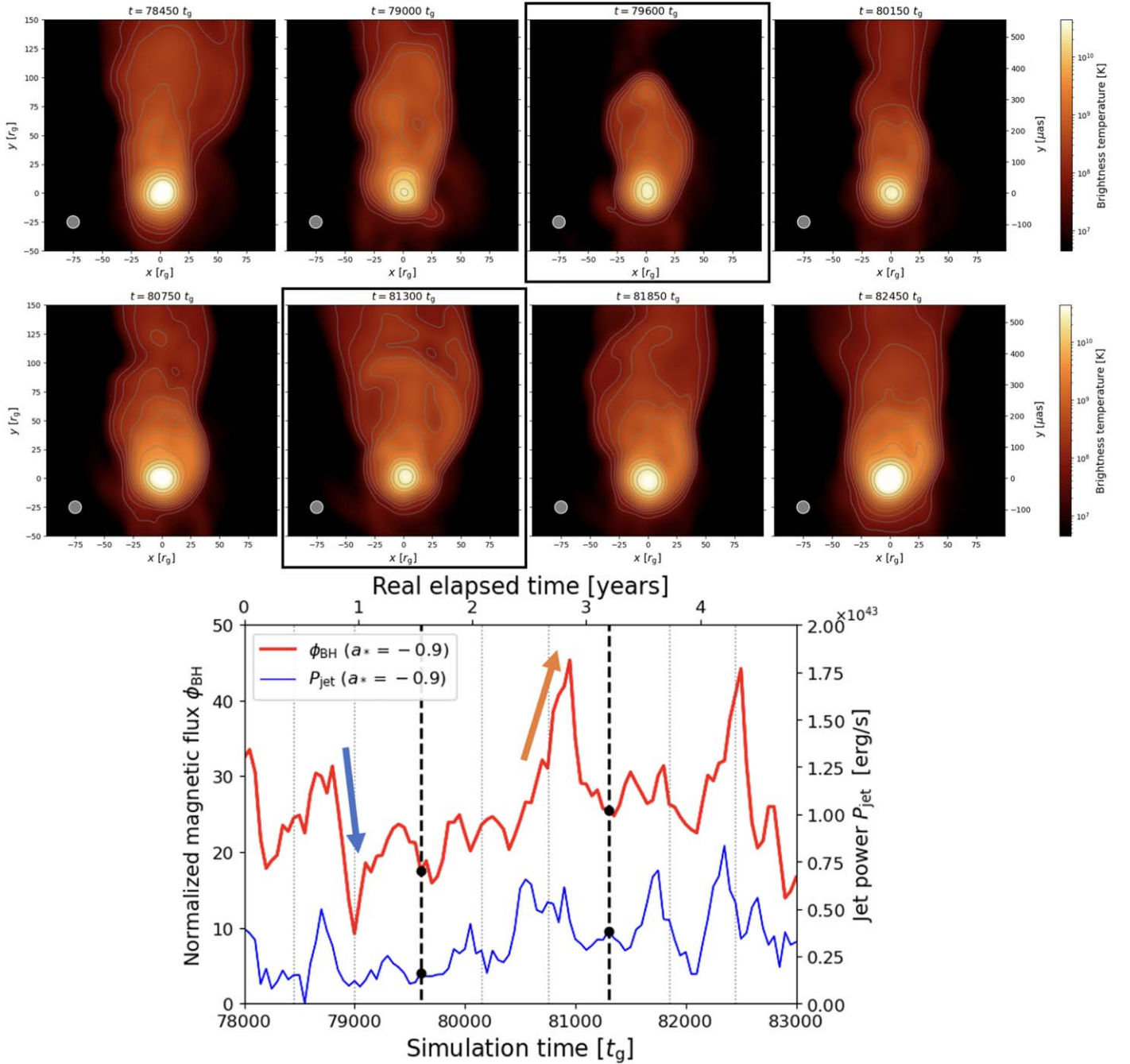


Figure 1. Top: eight snapshot images of the total intensity at 86 GHz for a GRMHD model with $a_* = -0.9$. The projection of the BH spin axis and the orientation of the approaching jet on the sky both point upward in the images. The contour levels increase in steps of two. The gray circle in the bottom left of the images shows the size of the FWHM of the circular Gaussian convolution beam. Bottom: the profiles of the normalized magnetic flux on the event horizon ϕ_{BH} and the jet power P_{jet} for the $a_* = -0.9$ model as a function of time. The two bold dashed lines and six dotted lines correspond to the times of the eight snapshots at the top. The blue and orange arrows indicate a drop and rise in ϕ_{BH} , respectively, prior to the two snapshots at $t = 79,600 t_g$ and $81,300 t_g$. An animation is available in the online journal (see Figure 2) and via <https://youtu.be/FwiKsplXjZk>. The $a_* = -0.9$ model is shown from 0 to 12 s, which covers the duration of $5000 t_g$ in the bottom panel.

To evaluate the strength of these correlated variations, we introduce the correlation function

$$\text{corr}(\Delta t) \equiv \int_{t_{\text{ini}}}^{t_{\text{fin}}} dt w_{\text{jet}}^-(t + \Delta t) \phi_{\text{BH}}^-(t), \quad (4)$$

where $w_{\text{jet}}(t)$ is the jet width at time t and the bar over the variables denotes normalization over a duration of $5000 t_g$. The obtained correlations at each altitude on the image are plotted

in the left panel of Figure 3, along with the correlation between ϕ_{BH} and the total flux.

We find that the jet widths show a stronger correlation with ϕ_{BH} , peaking at around 0.8, than the total flux. This means that while the total flux is a good indicator, dominated by radiation from the photon ring and strongly reflecting the magnetic flux, the jet widths serve as an even better indicator of the variability in ϕ_{BH} . The Δt_{peak} , time lag, is larger for higher y , as evident already in Figure 2.

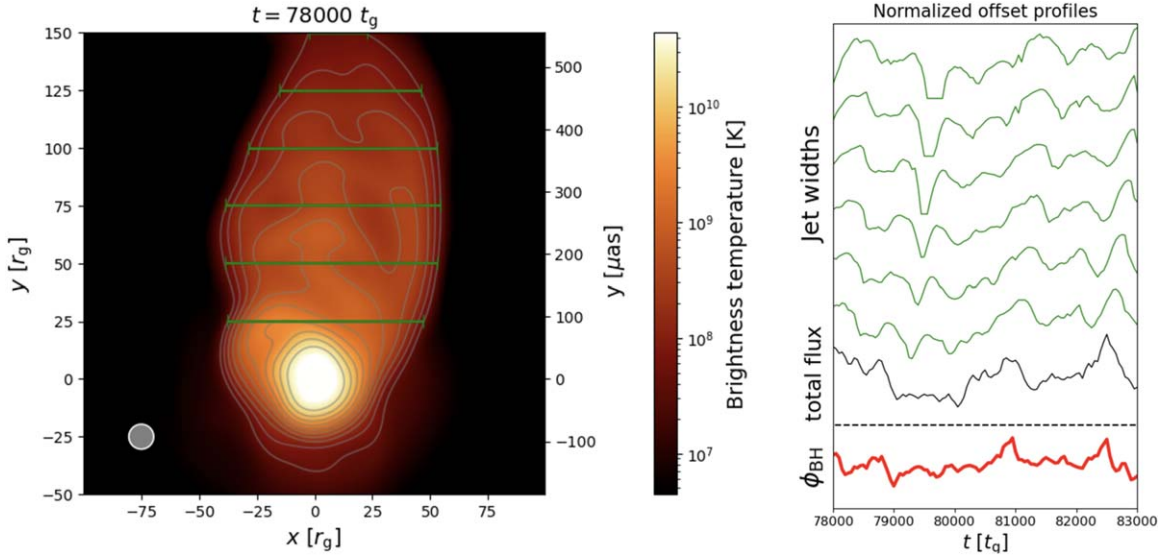


Figure 2. Left: total intensity snapshot at time $t = 78,000 t_g$ for the $a_* = -0.9$ model where our calculated jet widths are visualized using green lines, at six projected altitudes $y = 25 r_g, 50 r_g, 75 r_g, 100 r_g, 125 r_g,$ and $150 r_g$. Here, we define the two edges of the jet as the outermost points in the transverse profile at which the intensity is greater than 10^{-3} times the peak color contour. Right: variability profiles of ϕ_{BH} (red), the total flux (black), and the six jet widths (green) defined as in the left for a duration of $5000 t_g$. The absolute scales of the profiles are ignored here. An animation is available in the online journal and via <https://youtu.be/FwiKspIXjZk>. The $a_* = -0.9$ model is shown from 0 to 12 s, which covers the duration of $5000 t_g$. The static version of the figure corresponds to the first snapshot image.

(An animation of this figure is available in the [online article](#).)

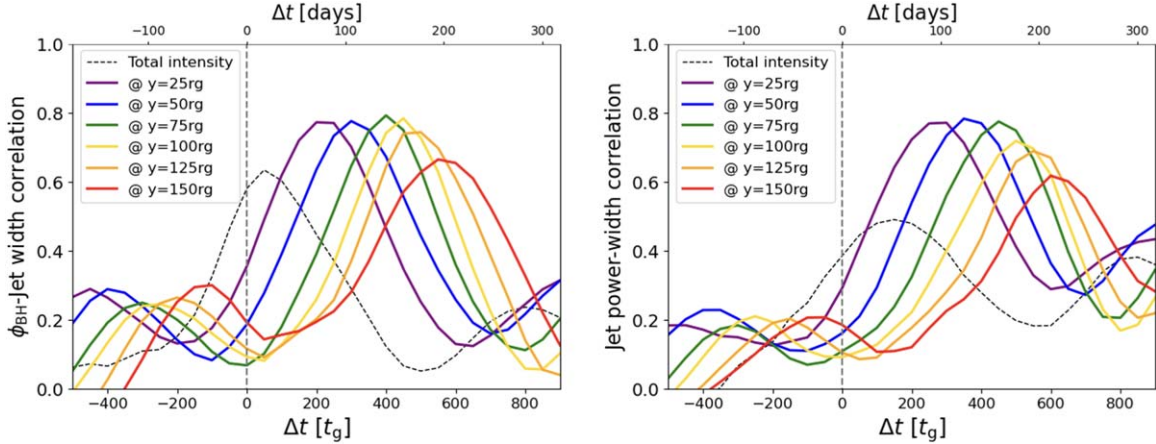


Figure 3. Left: correlation functions between ϕ_{BH} and the jet widths (solid lines), along with that between ϕ_{BH} and total flux (dashed line). Right: correlation functions between the jet power P_{jet} and jet widths.

In the above, we saw the strong connection between the horizon-scale dynamics and the extended jet shape for the $a_* = -0.9$ model.⁷ In Appendix A, we show qualitatively similar results for the other spinning BH models $a_* = +0.9, \pm 0.5$ (see the next subsection for the absence of jet in the nonspinning case). It is confirmed for the four spinning models that the jet widths strongly reflect the ϕ -variability as long as both edges of the jet are captured.

In the following subsections, we analyze the general features of time-averaged images and their spin dependence. As part of further analyses, we also discuss the statistical deviation of jet widths in Section 4.1 and examine the jet acceleration profile using the jet width profiles in Section 4.2, as well as calculating the correlation between the jet power P_{jet} and the jet width in Section 4.3.

⁷ We also confirm in Appendix B that the correlation holds for various model parameters.

3.3. Time-averaged Images, Magnetic Fields, and Plasma Bulk Motion

In the following subsections, we analyze the features of time-averaged images at 86 GHz. We have confirmed that the image features are essentially the same at 230 and 345 GHz due to the low optical depths at these frequencies for self-absorption and Faraday effects in the jet, although the intensity is lower.

3.3.1. Total Intensity Images

Here, we examine the magnetic field configuration and relativistic plasma bulk motion that can be extracted from images of the jet-launching region. The time-averaged total intensity images over $5000 t_g$ for the five spin cases are shown in Figure 4.

The images overall successfully produce an extended approaching jet, except in the nonspinning case. As shown in

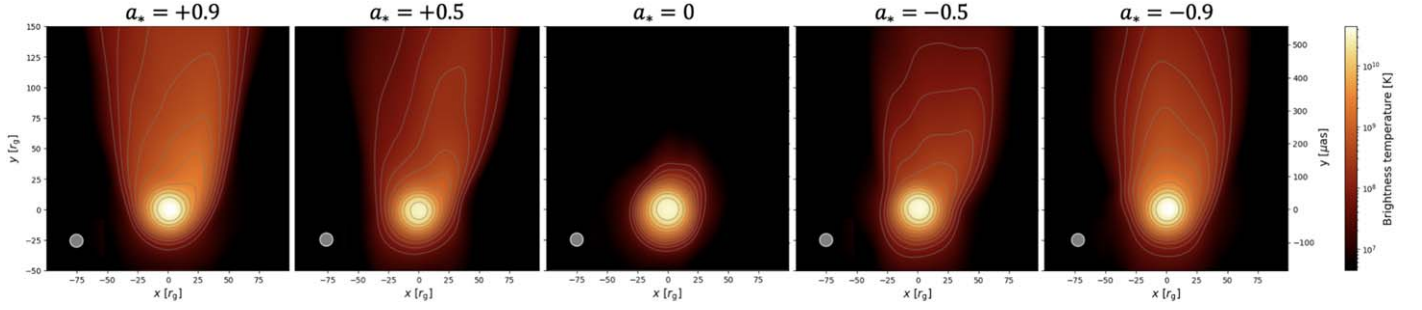


Figure 4. Time-averaged total intensity images for the five selected models ($a_* = +0.9, +0.5, 0, -0.5, -0.9$), averaged over $5000 t_g$.

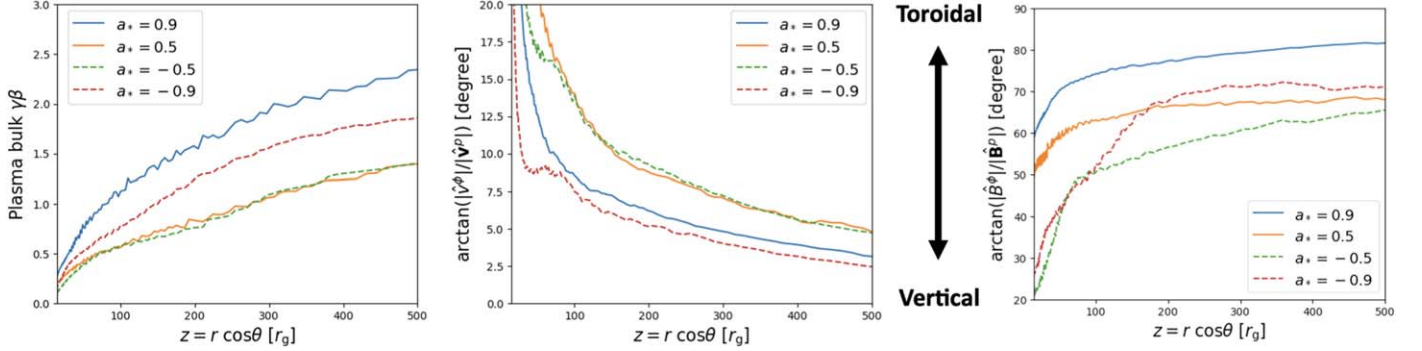


Figure 5. Profiles vs. z of the plasma bulk velocity multiplied by the Lorentz factor $\gamma\beta$ (left), the helicity angle of plasma bulk motion $|\hat{v}^\phi|/|\hat{v}^p|$ (middle) and of magnetic fields in the ZAMO frame $|\hat{B}^\phi|/|\hat{B}^p|$ (right) in four GRMHD models with spinning BHs. Each quantity is averaged over a duration of $5000 t_g$ and over an azimuthal angle $[0, 2\pi)$. The highly magnetized jet region with $\sigma \in [5, 10]$ is considered in calculating the profiles. Note that the scales of the vertical axis are different in the central and right panels.

R. Narayan et al. (2022), the $a_* = 0$ (Schwarzschild) BH does not produce highly magnetized relativistic plasma in the outer region, or if it does exist, it is only temporary. As a result, this model cannot produce a bright jet through the relativistic Doppler-beaming effect, unlike in the other cases. It is notable that our nonthermal eDF prescription naturally produces this effect.

Comparing the spinning cases, we find that the moderate spin cases, $a_* = \pm 0.5$, produce a less vertically extended and more asymmetric jet than the fast spin cases, $a_* = \pm 0.9$. This can be explained by the Doppler-beaming effect due to the helical bulk motion of the plasma. Since the present 86 GHz image shows a relatively symmetric jet (R.-S. Lu et al. 2023), this itself may be an important spin constraint (though it should be ultimately discussed bearing the observed limb-brightened feature in mind, as mentioned in Section 4.5). The robustness of this signal with respect to the nonthermal eDF prescription must be investigated in future work, but we find that the signal originates from the fluid itself (GRMHD as opposed to GRRT).

In the left and central panels of Figure 5, the time- and azimuthal-averaged GRMHD profiles of the plasma bulk velocity multiplied by the Lorentz factor $\gamma\beta$ and its helicity angle $\arctan(|\hat{v}^\phi|/|\hat{v}^p|)$ are plotted along the z -axis, respectively. Here, $\gamma = \alpha u^t$, α is the lapse, and $\beta = \sqrt{1 - \gamma^{-2}}$ (thus $\gamma\beta = \sqrt{\gamma^2 - 1}$); $\hat{v}^\phi = \sqrt{g_{\phi\phi}} u^\phi / u^t$ and $\hat{v}^p = (\sqrt{g_{rr}} u^r \hat{r} + \sqrt{g_{\theta\theta}} u^\theta \hat{\theta}) / u^t$ are the toroidal and poloidal components of the velocity field, respectively; and the profiles are calculated for the jet region with $\sigma_m \in [5, 10]$.

In the left panel in Figure 4, we see that the spinning BHs show persistent acceleration of plasma up to the relativistic regime $\gamma\beta > 1$ within $500 r_g$ along the jet.⁸ The profiles also show spin dependence, where higher spins result in stronger plasma acceleration compared to lower spins, both in the prograde and retrograde cases. This directly explains the less vertically extended jets in the lower spin cases, due to weaker Doppler beaming.

The central panel exhibits vertical plasma velocity overall, but more helical motion for the lower spins. The helical motion of the plasma results in a gap in the beaming effect between the two sides of the jet in the image. In the images shown in Figure 4, the right side of the jet approaches the observer and gains more beaming, while the left side recedes and experiences less beaming. This tendency is amplified with more helical plasma flow, leading to greater asymmetry for lower spin values. Since the helicity angles are close to the observer's viewing angle of $i = 163^\circ$ (17°), even a small difference in the angle results in a significant difference in the images.

This explains one edge- or spine-brightened features in the jet-launching region in the time-averaged total intensity images. In Section 4.5, we compare these features with existing observations based on the nonthermal electron prescription.

3.3.2. LP Images

Time-averaged LP maps are shown for the four spinning models in Figure 6. Overall, they show an asymmetric pattern of horizontal LP vectors in the right edge (beaming side) and

⁸ $\gamma\beta = 1$ and 2 correspond to $\beta \sim 0.71c$ and $\sim 0.89c$, respectively.

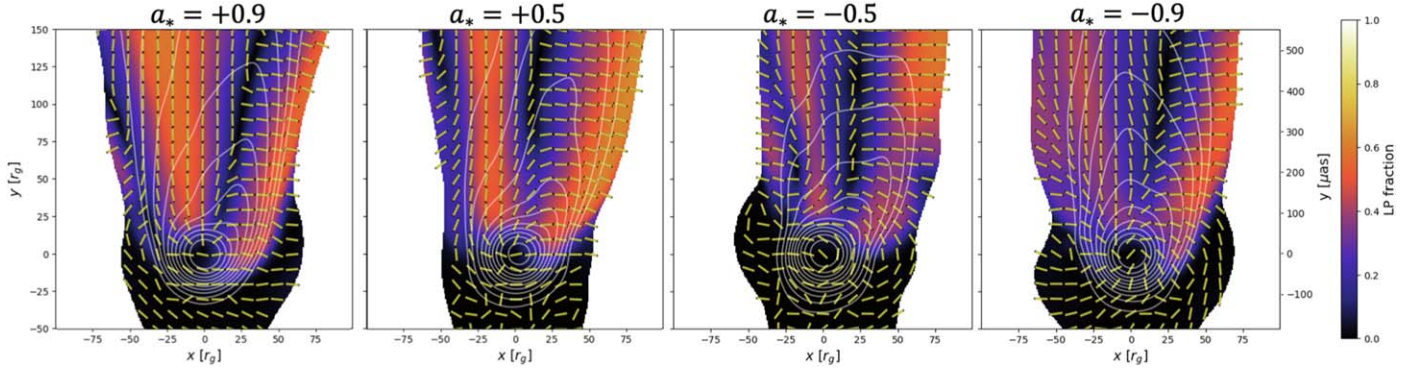


Figure 6. LP maps for four models with spinning BHs, averaged over $5000 t_g$. The line and color contours denote the total intensity (same as in Figure 4) and the LP fraction, respectively. The LP vector EVPAs are overwritten as ticks.

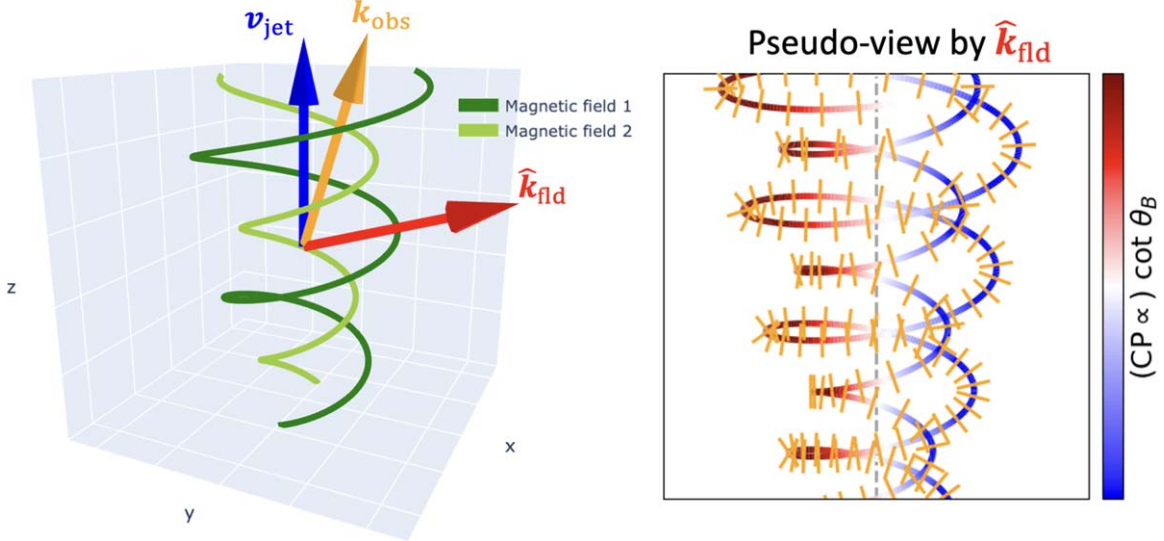


Figure 7. Left: schematic picture of helical magnetic field lines 1 (outer, green) and 2 (inner, light green) and the relativistic aberration between the light propagation vector in the observer frame, k_{obs} (orange arrow), and that in the fluid rest frame, \hat{k}_{fld} (red arrow), by the bulk velocity of jet v_{jet} (blue arrow). Here, the bulk motion is assumed to be purely vertical. Right: pseudo-view of the two field lines and their polarization as viewed by the aberrated \hat{k}_{fld} . The two field lines are overplotted with LP vector ticks. The red-blue contour of the lines describes $\cot \theta_B$, to which the CP components are proportional (see Appendix D for CP images). Here, θ_B is the angle between the light propagation vector and the magnetic field line. Note that these are the projections of polarization components obtained in the fluid rest frame onto the pseudo-screen for \hat{k}_{fld} . We actually observe these on the projection onto the observer’s screen for k_{obs} after transforming them into the observer’s frame.

vertical in the center (spine) and left edge (de-beamed side). We also see a horizontal pattern in a narrow region near the left edge. In addition, the counter jet and disk show low LP fractions close to zero due to strong Faraday rotation and depolarization in the low electron temperature ($R_{\text{high}} = 160$) disk gas near the BH (M. Mościbrodzka et al. 2017; A. Ricarte et al. 2020; Y. Tsunetoe et al. 2022).

The asymmetric LP vector pattern in the jet does not straightforwardly imply an asymmetry in the magnetic field configuration since the combination of axisymmetric helical fields and the inclination of the observer’s viewing angle can cause an asymmetric pattern (see, for example, O. Porth et al. 2011; E. Murphy et al. 2013). In the right panel of Figure 5, we show the helicity angle of the magnetic field in the zero-angular momentum observer (ZAMO) frame, $\arctan(|\hat{B}^\phi|/|\hat{B}^p|)$, for the four models. Here, \hat{B}^ϕ and \hat{B}^p are defined in the same way as \hat{v}^ϕ and \hat{v}^p , respectively. As a whole, the magnetic fields are in a helical configuration.

The key factor in interpreting the LP vector patterns in Figure 6 is a combination of the relativistic aberration effect

and helical magnetic field configuration. In the left panel of Figure 7, we picture two helical magnetic field lines in the rest frame of the plasma which is moving in the z -direction with velocity v_{jet} . The radiation observed at a certain viewing angle in the observer’s frame, which is now $i = 163^\circ$ (or 17°) and denoted by k_{obs} in the picture, is emitted at a larger angle in the plasma rest frame, denoted by \hat{k}_{fld} .

If the magnetic fields were projected onto this pseudo-screen for \hat{k}_{fld} , they would form vertically compressed “ α ,” or “ $c + x$ ” shapes as in the right panel of Figure 7. The LP vectors and CP components in the fluid rest frame are denoted by the ticks and color contour of the line, respectively. We obtain an ordered vertical LP vector pattern in the broad region on the left side, reflecting the pattern on compressed “ c ” shapes in the central panel, and a horizontal pattern in the edge region of the right side, reflecting that on the right side of the “ x .” (Though there are horizontal vectors in the left edge of “ c ” shapes, they are limited to narrow regions and subordinate to the dominant vertical vectors.) In the inside region of the right side, around the cross points of “ x ,” the vectors are disordered and cancel each other out.

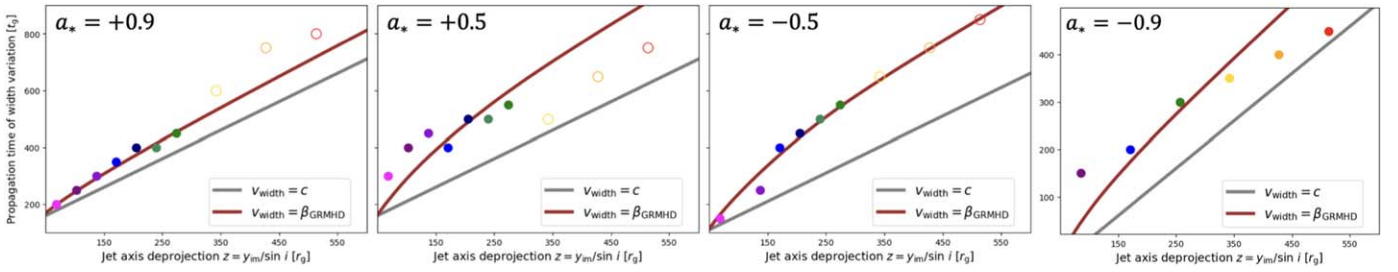


Figure 8. Profile of the propagation time of changes in the jet width along the jet axis for the spinning BH models. The vertical positions of the colored dots show Δt_{peak} , which corresponds to the time lag of the peak of the correlation functions between the total intensity flux and the jet width at each y , i.e., the time gap between when a fluctuation in the total flux occurs and when its effect is seen in the jet width profiles in Figures 2, 10, 11, and 12 (see also Appendix A for the other spin models than the $a_* = -0.9$ model). The horizontal axes correspond to the y coordinate on the image deprojected onto the z -axis in the fluid model coordinates by the observer’s viewing angle $i = 163^\circ$ (17°). The black line corresponds to propagation at speed c . The brown line is the predicted profile if changes in the jet width propagate at the average plasma bulk velocity in the GRMHD model β_{GRMHD} , i.e., by integrating $dt = dz/\beta_{\text{GRMHD}}$ from $z = 40 r_g$ to each z . Here, the plasma bulk velocity β_{GRMHD} is obtained as in the left panel of Figure 5. In the rightmost panel, an offset of $-50 t_g$ is added to the two profiles since the total intensity flux is delayed by $50 t_g$ relative to ϕ_{BH} , as shown in the left panel of Figure 3. The same applies to the other panels, based on the ϕ_{BH} -total flux offset in each model.

Here, we should note that these polarization components are actually observed on the observer’s screen for \mathbf{k}_{obs} , after transformed into the observer’s rest frame (see V. I. Pariev et al. 2003; M. Lyutikov et al. 2003; see also R. D. Blandford & A. Königl 1979 for the relativistic swing effect). Nevertheless, the larger viewing angle due to the aberration here induces a more asymmetric pattern in the images in Figure 6. In this way, the relativistic jet with helical magnetic fields gives an asymmetric pattern of LP vectors horizontally on the right side and vertically on the spine and left side of the jet. In the transition region between the two patterns, the LP vectors are inclined and the LP fraction is low (see Section 4.4; see also J. Davelaar et al. 2023 for depolarization in the shear layer.)

For comparison, we show the images and schematic picture in which the relativistic effects are turned off, in Appendix C. In this case, $\hat{\mathbf{k}}_{\text{fld}}$ coincides with \mathbf{k}_{obs} as pictured in Figure 15, showing a symmetrical pattern that reflects the projection of helical magnetic field lines from the face-on-like view in Figure 14.

So far, we have observed that relativistic aberration generally produces an asymmetric LP vector pattern in the images of the jet-launching region. In Section 4.4, we discuss the BH spin dependence of the asymmetry in the LP images, focusing on the magnetic field helicity and jet acceleration profiles. In addition, we also note a symmetrical bipolar CP component pattern in the jet images and its spin dependence in Appendix D.

4. Discussion

4.1. Estimate of Jet Acceleration from Observables

In Section 3.2, we showed that the jet widths in the image and the total intensity flux are strongly correlated with the normalized magnetic flux at the event horizon ϕ_{BH} , with the time delay increasing monotonically with distance. This result implies that the change in jet widths propagates from the BH to the jet, and motivates us to explore whether it might be possible to estimate the plasma acceleration profile by observing variations in the jet width.

We calculate the correlation function between the total flux and the jet width at each y on the image for the spinning BH models (the black and green profiles in the right panel of Figure 2 for the $a_* = -0.9$ model and in the leftmost panels of Figures 10, 11, and 12 for the other spin models). The delay Δt_{peak} as a function of the deprojected distance along the jet

axis, $z = y/\sin i$, is plotted in Figure 8. The delays correspond to the time it takes for changes in the jet width to propagate along the axis, up to each y position in the image.

We also plot two model curves for comparison. The straight gray line corresponds to the jet width variation propagating at a constant speed of $v=c$. The brown line assumes that the propagation speed is the average plasma bulk velocity in the GRMHD model, i.e., we integrate $dt = dz/\beta$ (and $dt = dz/c$ for the $v=c$ line) from $z = 40 r_g$ to each z , where the plasma bulk velocity β is obtained as in the left panel of Figure 5. We here add an offset of Δt_{peak} of the ϕ_{BH} -total flux correlation to the two profiles, since the total intensity flux is delayed (or precedes) relative to ϕ_{BH} , as shown in the left panel of Figure 3.⁹

Figure 8 suggests that there is acceleration up to the relativistic regime, 70% to 90% of the speed of light, for all the spinning BH models. They also persistently show reasonable agreement with the average bulk velocity from GRMHD up to $z \sim 300 r_g$. These results suggest that it may be possible to measure the jet acceleration profile from jet width measurements. Note that the times shown in the plots correspond to coordinate time in the simulation frame, while the observed time lags will be shorter because of relativistic Doppler beaming. This has not been included in the calculations presented here.

4.2. Variability of Jet Width and Φ_{BH}

R. Narayan et al. (2022) pointed out that the variability of the un-normalized magnetic flux on the event horizon, Φ_{BH} , increases with the BH spin value for retrograde models, while it remains almost constant for prograde models.

To check the relationship between the variability in GRMHD models and GRRT images, we calculate the variability of jet width at $y = 50 r_g$ on the image for the five models. Here, the variability is calculated for each duration of $1000 t_g$, dividing the snapshots into five bins, and is then averaged over the bins, following R. Narayan et al. (2022).

Figure 9 shows the variability of Φ_{BH} and jet width. First, our $5000 t_g$ duration data successfully reproduce the Φ_{BH} variability shown in R. Narayan et al. (2022) for the longer duration of $50,000 t_g$. Second, the variability of the jet width shows similar values to the variability in Φ_{BH} , preserving the

⁹ Here, we assume that the change in jet shape begins to propagate downstream at the moment the change in ϕ_{BH} occurs.

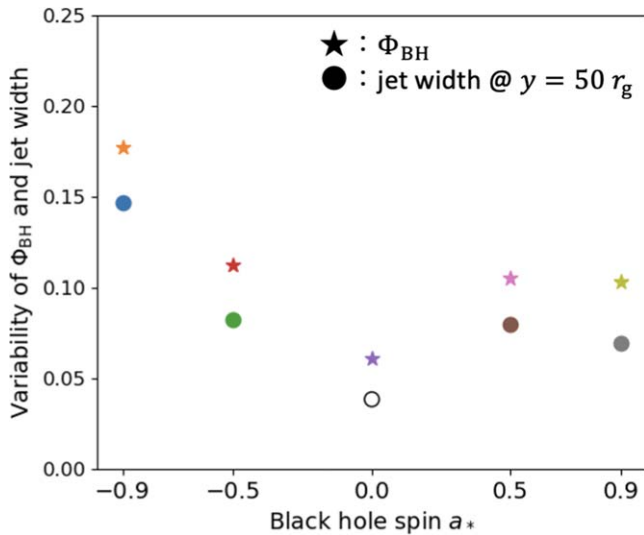


Figure 9. The variability σ/μ (rms fluctuations divided by the mean) of the non-normalized magnetic flux on the event horizon Φ_{BH} (denoted by the stars) and jet widths at $y = 50 r_g$ on the images (circles) for the five models. Note that the jet width for $a_* = 0$ (empty circle) is exceptionally measured at $y = 10 r_g$.

dependence on BH spin. The slight decrease in the magnitude of the variability can be attributed to the mock-observational blurring in the images, which tends to smooth out subtle changes in the jet shape.

We also find that the variability in the jet width reproduces the behavior of Φ_{BH} rather than ϕ_{BH} . The latter shows variability increasing with the spin value for both retrograde and prograde models (R. Narayan et al. 2022). Furthermore, we also confirmed that the jet widths show a slightly better correlation with Φ_{BH} than ϕ_{BH} , while they yield an insignificant correlation with the mass accretion rate M . Based on this, we can say that the jet widths selectively reflect the dynamics of magnetic flux on the horizon, not the mass accretion process onto the BH.

In this way, we saw that the jet width gives the variability monotonically increasing with BH spins for the retrograde models, and the almost unchanging variability for the prograde models. This tendency is consistent with the variability of the absolute magnetic flux Φ_{BH} . This result suggests that we can expect to determine the handedness and value of BH spin through long-term observations of the jet-launching region.

4.3. Jet Power-width Correlation

The result in the last subsection leads us to another important quantity in the BZ process: the jet power. In the right panel of Figure 3, we show the correlation functions between the jet power P_{jet} (see the bottom panel of Figure 1 for the variability profile) and the jet width at each y position on the image for the $a_* = -0.9$ model. All the jet widths exhibit strong correlations with the jet power, which are comparable to those with ϕ_{BH} .

These results suggest that the jet widths are also a good indicator of jet power. Thus, we can expect to survey the jet power and efficiency, which serves as a litmus test of the BZ process. In addition, since the jet power derived from the rotational energy of the BH results in spin-down (R. Narayan et al. 2022; A. Ricarte et al. 2023a, 2025), the observation of jet width can provide a foothold for investigating the BH spin evolution.

4.4. Spin Dependence of the LP Maps

The LP maps in Figure 6 show a spin dependence, and we noted their general asymmetric appearance in Section 3.3.2. Lower spins show more asymmetric patterns than the higher ones, as seen in the difference in the location of the zero LP fraction line which demarcates the horizontal pattern in the right edge and the vertical pattern in the middle.

This is triggered by the spin dependence of the helicity angle of the magnetic field. As shown in the right panel of Figure 5, the lower spin cases consistently show a less toroidal (more vertically dominated) field structure compared to the higher spins, which wind up the field lines more strongly.

If the plasma bulk motion is the same, this results in more compressed “c + x” shapes, or “<” shapes of projected magnetic field lines, as shown in Figure 17 in Appendix D. In such a case, the border of vertical and horizontal patterns is shifted to the left side with the cross point of “x,” as also shown in E. Murphy et al. (2013). Therefore, the lower spins give a more asymmetric pattern, with the horizontal LP vector filling a larger area on the right side of the jet.

J. A. Kramer & N. R. MacDonald (2021) calculated images based on relativistic MHD models with three kinds of magnetic field configuration. Their helical model exhibits a horizontal vector pattern on the beamed side of the jet, while their toroidal model shows a symmetrical pattern of vertical vectors in the spine and horizontal vectors in the two edges, as in our nonrelativistic image in Figure 14. Our images in Figure 6 are in between their models, showing the asymmetric pattern, which reflects the helicity of magnetic fields from the relativistically aberrated view.

In addition, our LP maps also show inclined vectors in the transition between horizontal and vertical patterns. They indicate whether the radiation comes from the front or back side of the jet (though the polarization fraction is low). As shown in Figures 7 and 17, the “/” ticks come from the back of the jet, while the “\” ticks come from the front. These features can be a tracer of jet morphology along the axis, if detected.

These results in the LP maps suggest a new method for investigating the magnetic field configuration, the plasma acceleration profile, and the BH spin.

Recently, Z. Gelles et al. (2024) surveyed the LP maps using semi-analytical force-free jet models. Our and their results are qualitatively consistent in the tendency that the moderate spin $|a_*| = 0.5$ model tends to exhibit a more asymmetric pattern in the inner and outer jet than the high spin $|a_*| = 0.9$ model, reflecting less toroidal magnetic field configuration due to larger light cylinder radius (Z. Gelles, private communication).

Meanwhile, they also pointed out that the LP vector pattern switches from radial to azimuthal at the light cylinder radius, where the plasma bulk velocity becomes relativistic and starts to suppress the magnetic field component parallel to the motion. In contrast, our LP images do not show such a transition due to moderate acceleration. As in the left panel of Figure 5, plasma bulk motion in the region with $\sigma < 10$ barely reaches $\gamma\beta \sim 1.2$ in the $a_* = 0.9$ model and ~ 0.5 – 0.7 in the other spins at $z = 100 r_g$, while their force-free models yield ~ 3 . Addressing this gap between the force-free and GRMHD models is an important task for future studies.

In observational approaches, S. P. O’Sullivan & D. C. Gabuzda (2009) reported the detection of the vertical and horizontal LP vector patterns along active galactic nucleus jets at centimeter wavelengths on the tens of parsec scale.

R. C. Walker et al. (2018) detected a persistent LP vector pattern on the sub-millisecond scale in the M87 jet, implying the presence of significant toroidal magnetic field components. Upcoming observations of M87* with high angular resolution and high sensitivity will shed new light on the BH jet mechanism.

4.5. Comparison with Observations and Nonthermal Contribution

In Section 3.3.1, we saw single-edge or spine-brightened jets in time-averaged images. Meanwhile, observations of the base region of M87's jet at 86 GHz show a double-edged, limb-brightened morphology (e.g., J. Y. Kim et al. 2018; R.-S. Lu et al. 2023). There is a large gap by a factor of ~ 5 between the intensities in the edges and the spine at $y = 0.25$ mas ($\approx 68 r_g$ on our image) along the jet (J.-S. Kim et al. 2024).

This discrepancy should be addressed with future work, surveying the nonthermal electron prescription. In introducing nonthermal electrons in the electron energy distribution in this work, we assumed energy partition, with the energy in the nonthermal electrons being only 3% of that in the thermal electrons, as mentioned in Section 2.2. This naturally makes the nonthermal component subordinate to thermal in the eDF, and is a conservative or passive choice. We have confirmed that the contribution of nonthermal emission in the image is overall $\lesssim 10\%$ in the jet region. C. M. Fromm et al. (2022) calculated GRRT images based on the kappa-eDF (see, for example, A. Pandya et al. 2016), finding that a nonthermal-dominant prescription in partition with the magnetic energy produced emission over a longer region of the jet.

In addition, the power-law index p is fixed to 2.5 in the whole region in this work. D. Ball et al. (2018) and C. Meringolo et al. (2023) suggested that the spectral slope is steeper in weakly magnetized regions with $\sigma \leq 1$. Recently, H. Yang et al. (2024) started investigating spatially variable p based on particle acceleration via magnetic reconnection. In the nonthermal-dominant regime, energy prescription should be surveyed, bearing in mind various acceleration mechanisms and the synchrotron cooling effect.

In addition, there is uncertainty in the sigma cutoff we applied. Recently, A. Chael (2024) developed a hybrid model of GRMHD and force-free electrodynamics, which avoids the need for a density floor. They pointed out that traditional GRMHD simulations are relatively safe up to $\sigma \approx 25$. We found that using a high σ cutoff value gives a more extended jet image (as also seen in C. M. Fromm et al. 2022) but less edge-brightened jets. It is an urgent task to identify the parameters that reproduce the observational results.

5. Conclusions

In this work, we investigated the variability and large-scale structure of magnetic fields in the jet-launching region up to several hundred gravitational radii r_g , through GRRT image calculations based on GRMHD models. We focus on the science attainable with improvements to dynamic range, spatial resolution, and temporal resolution, which will be made possible by ngEHT and BHEX. Our conclusions are summarized as follows;

1. *Jet archeology and forecasting.* Variations in the jet width reflect those of the normalized magnetic flux on the event horizon, ϕ_{BH} , with a time delay. This enables

archeology of magnetic field dynamics on the BH through measurements of the extended jet width, as well as forecasting upcoming changes in the jet morphology from variations in the total intensity flux or high-energy eruptive events. By examining the variability in magnetic flux and jet morphology through these methods, we can expect to verify the MAD model. Note that this paper is focused on the innermost regions of the jet at distances below $10^3 r_g$. At larger distances, jet width variations are likely influenced more by fluctuations in the ambient medium rather than magnetic field variability at the BH (see, for example, A. S. Nikonov et al. 2023 for helical structures and the Kelvin–Helmholtz instability).

2. *Testing the BZ process.* The jet width variation exhibits acceleration from the upstream to the downstream, matching the velocity profile of the plasma bulk motion. Additionally, the jet widths show a strong correlation with the jet power, P_{jet} . The BZ process can be tested by detecting the acceleration profile up to the relativistic regime and measuring the jet power and efficiency.
3. *Constraining BH spin.* The variability in jet width shows a dependence on the BH spin, mirroring that of the magnetic flux, Φ_{BH} . The time-averaged total intensity images display different asymmetric beamed features depending on spin, due to variations in the plasma acceleration profile. Similarly, the time-averaged LP maps show spin-dependent vector patterns, reflecting the helicity of the magnetic field (see also Appendix D for spin dependence in CP images). Thus, both long-term and high-cadence observations of the jet-launching region may enable novel constraints on the BH spin, independent of those obtained on event horizon scales.

As is typical for these types of studies, there remains significant uncertainty in the prescription of the nonthermal eDF. The details of the nonthermal prescription are well known to impact jet morphology on large scales. In future work, it will be essential to explore a variety of prescriptions and aim to reproduce observed features across global scales at multiple frequencies for M87 and other jets.

Acknowledgments

The authors thank Dominic Pesce and Zack Gelles for constructive discussion and comments. This publication is funded in part by the Gordon and Betty Moore Foundation (grant #8273.01). It was also made possible through the support of a grant from the John Templeton Foundation (grant #62286). The opinions expressed in this publication are those of the authors and do not necessarily reflect the views of these Foundations. Y.T. is grateful for support from JSPS (Japan Society for the Promotion of Science) Overseas Research Fellowships. Numerical computations were in part carried out on Cray XC50 at the Center for Computational Astrophysics, National Astronomical Observatory of Japan.

Data Availability

The data that support the findings of this study are available from the corresponding author, Y. T., upon reasonable request.

Appendix A Magnetic Flux Jet-width Correlation for Different BH Spin Models

A snapshot image with jet width measures, the time profiles of ϕ_{BH} , total intensity flux, and jet widths, and the correlation function between them are shown in Figure 10 for the $a_* = 0.9$ model, Figure 11 for $a_* = 0.5$, and Figure 12 for $a_* = -0.5$.¹⁰ Here, we measure the jet widths at 20, ..., 80 r_g (solid lines) at the same threshold of 10^{-3} times the peak intensity, as in Section 3.2. In addition, the outer jet widths at 100, 125, 150 r_g (dashed lines) are measured with a lower intensity threshold, 10^{-4} times the peak. This enables the capture of the transverse

profile of the outer jet, which is fainter, especially on the de-beamed side.

In Figure 8 in the main text, the jet acceleration profiles are also shown for the three spin models. Here, we commonly calculate $v = c$ and GRMHD-velocity $v = \beta_{\text{GRMHD}}$ profiles from $z = 40 r_g$, and add an offset of the delay between ϕ_{BH} and total flux in each case. The points appear on the GRMHD profile up to $z \sim 300 r_g$ for all the spinning BH models, implying that the inner jet acceleration can be traced by the jet width measurement. Furthermore, this result suggests that we can infer the BH spin from the acceleration profile estimated from the jet widths.

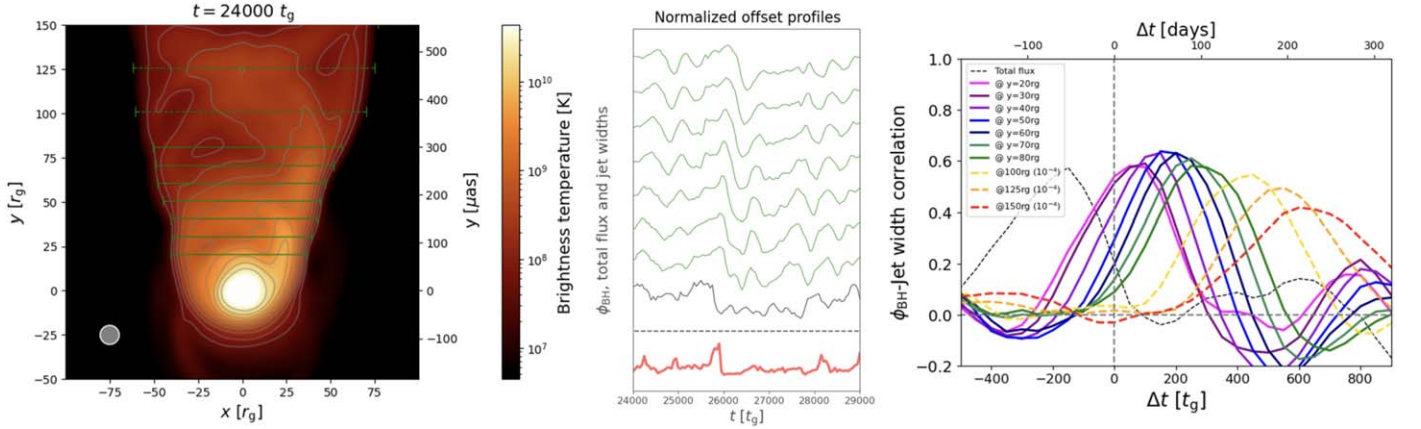


Figure 10. Left: a snapshot image for the $a_* = 0.9$ model with measures of jet widths (green lines). For the three dashed lines, we measure the two edges as the outermost points with 10^{-4} times the peak of the color contour. Center: variability profiles of ϕ_{BH} (red) and the jet widths (green) defined by the solid lines on the left for the duration of $5000 t_g$. The absolute scales of profiles are ignored. Right: correlation functions between ϕ_{BH} and the jet widths (solid and dashed lines), and total intensity flux (dotted line). An animation is available in the online journal (see Figure 2) and via <https://youtu.be/FwiKspIXjZk>. The $a_* = 0.9$ model is shown from 12 to 24 s, which covers the duration of $5000 t_g$. The static version of the figure corresponds to the first snapshot image at $t = 24,000 t_g$.

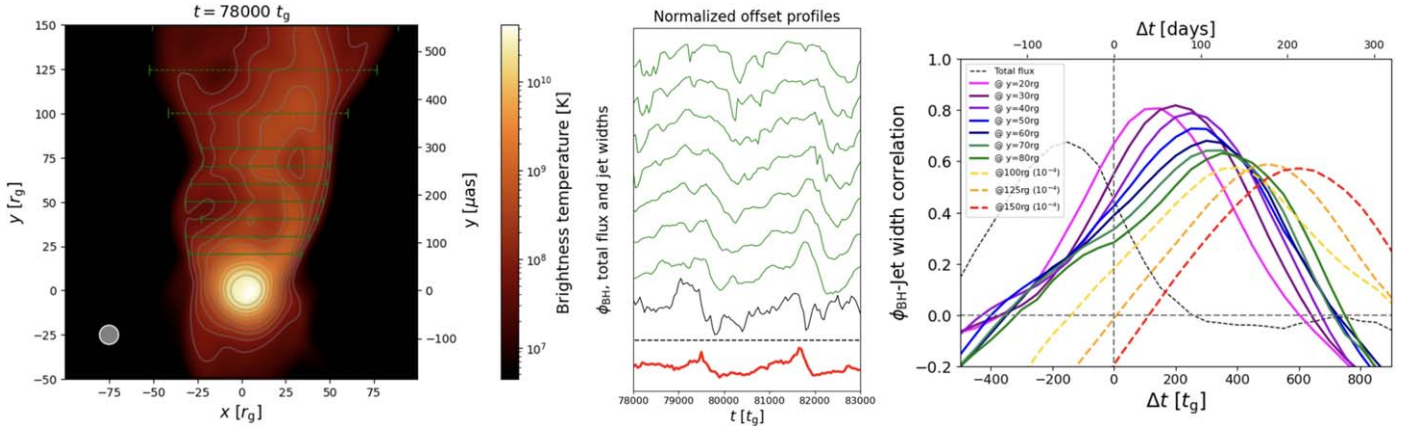


Figure 11. Same as Figure 10, but for the $a_* = 0.5$ model. An animation is available in the online journal (see Figure 2) and via <https://youtu.be/FwiKspIXjZk>. The $a_* = 0.5$ model is shown from 24 to 36 s, which covers the duration of $5000 t_g$. The static version of the figure corresponds to the first snapshot image at $t = 78,000 t_g$.

¹⁰ An animation is available in the online journal (see Figure 2) and via <https://youtu.be/FwiKspIXjZk>.

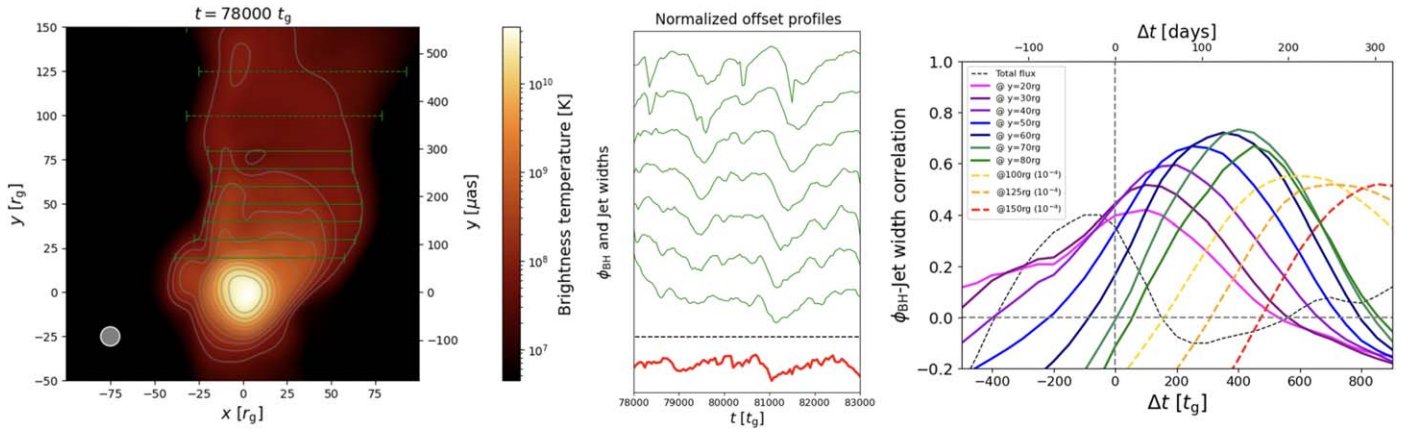


Figure 12. Same as Figure 10, but for the the $a_* = -0.5$ model. An animation is available in the online journal (see Figure 2) and via <https://youtu.be/FwiKspIXjZk>. The $a_* = -0.5$ model is shown from 36 to 48 s, which covers the duration of $5000 t_g$. The static version of the figure corresponds to the first snapshot image at $t = 78,000 t_g$.

Appendix B

Parameter Survey of the Jet-width Correlation

To check the validity of the results in this work for different model parameters, we show in Figure 13 the profiles of the magnetic flux ϕ_{BH} and jet width at $y = 50 r_g$ on image for a large inclination angle of $i = 30^\circ$, for the images at 43 and 230 GHz convolved with a circular Gaussian beam of 80 and

$20 \mu\text{as}$, and for a small value in sigma cutoff, $\sigma \leq 5$. In each case, all the other parameters are set to the fiducial values for the $a_* = -0.9$ case.

It is confirmed that all the models give a jet width profile reflecting the magnetic flux with a peak correlation coefficient of ~ 0.8 , comparable with that in the main text. Furthermore, we can see that the large inclination case shows a shorter time

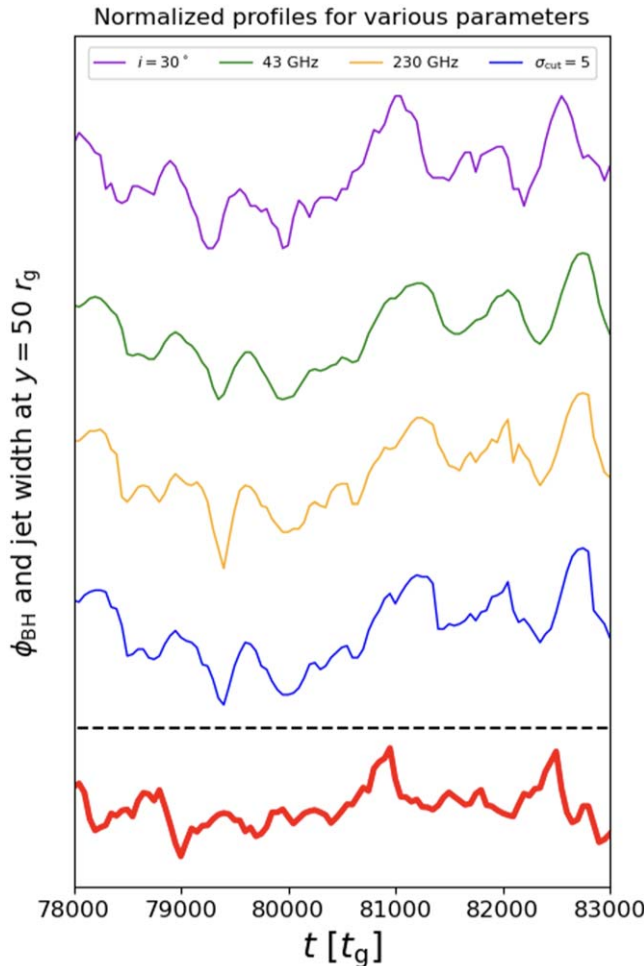


Figure 13. The magnetic flux ϕ_{BH} (red) and jet width at $y = 50 r_g$ on image for various model parameters; the inclination angle of 30° (violet), at 43 (green) and 230 GHz (yellow), and the sigma cutoff of $\sigma \leq 5$ (blue). In each case, the other parameters are fixed to the fiducial values for the $a_* = -0.9$ case. The images at 43 and 230 GHz are blurred with a circular Gaussian beam of 80 and $20 \mu\text{as}$, respectively.

delay than the other cases. This is because $y = 50 r_g$ on the image corresponds to a smaller distance from the BH for the larger inclination angle (i.e., $50 r_g / \sin 30^\circ = 100 r_g < 50 r_g / \sin 17^\circ \approx 170 r_g$). This implies that the inclination of the jet can be investigated via the jet width analysis.

Appendix C

Images in Which the Relativistic Effects Are Turned Off

In Figure 14, we show the time-averaged LP map and CP image for the $a_* = 0.9$ model in which the relativistic effects are

turned off with the four-velocity set to $u^\mu = u_{\text{ZAMO}}^\mu$. Here, u_{ZAMO}^μ is the velocity of ZAMO. The picture of helical magnetic field lines and the relativistic aberration effect is also shown in Figure 15 for the nonrelativistic case. Here, the LP map shows a symmetrical pattern of horizontal vectors in both edges and vertical vectors in the spine. Meanwhile, the CP image presents an asymmetric bipolar pattern leaning to the right (left) side in the approaching (receding) jet. This clearly demonstrates that relativistic beaming, which is spin dependent, is responsible for the transverse asymmetry in our polarized jet images.

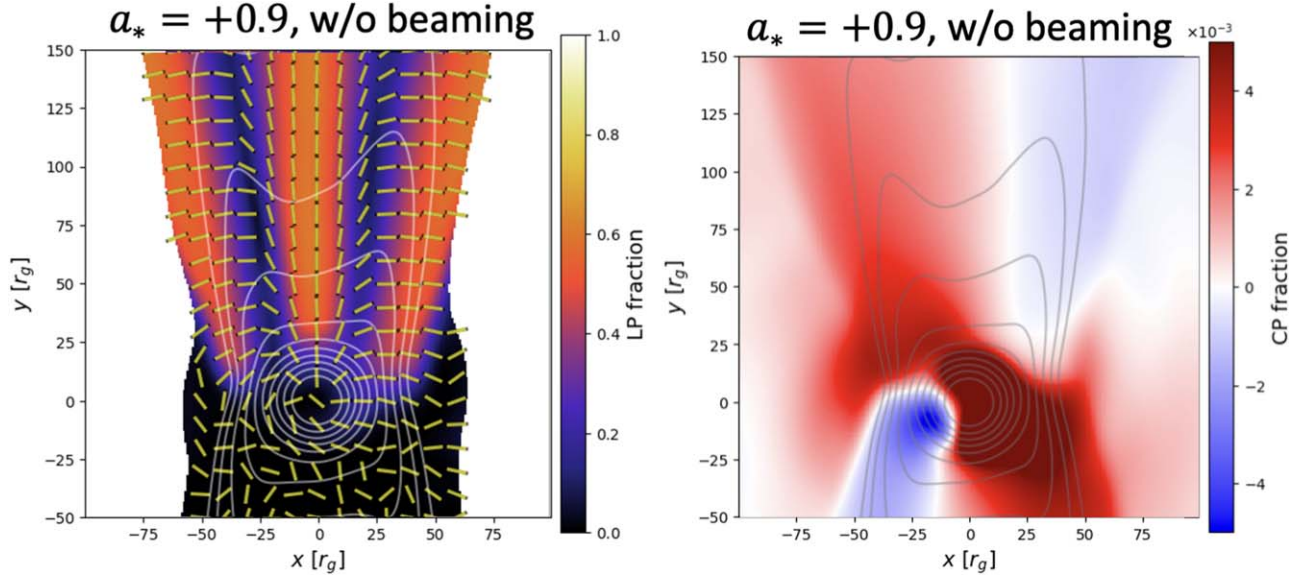


Figure 14. The time-averaged LP map (left) and CP image (right) for $a_* = 0.9$, when the relativistic effects of the plasma bulk motion are turned off. Here, the four-velocity u^μ is set to the ZAMO velocity u_{ZAMO}^μ .

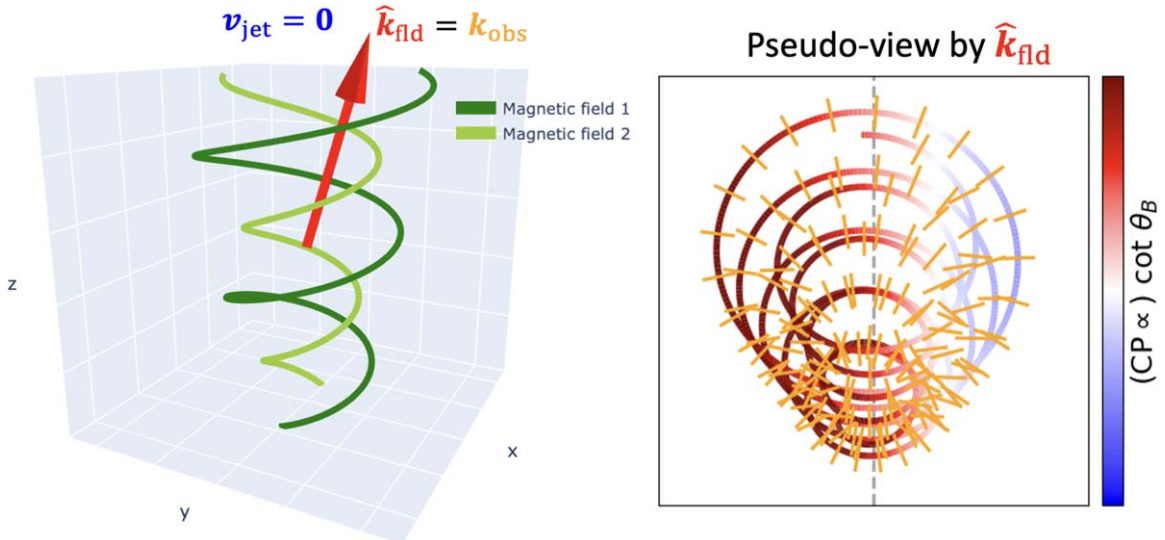


Figure 15. Same as Figure 7, when the plasma bulk is set to $v_{\text{jet}} = 0$. Here, \hat{k}_{fld} coincides with k_{obs} , and so does the pseudo-view with the observer's view. Note that the LP vectors are left-right symmetric.

Appendix D CP Images and Spin Dependence

We also investigate time-averaged CP images, shown in Figure 16, but do not find obvious signatures that we believe can be used to infer magnetic flux or spin. In the innermost region around the BH within $\sim 20 r_g$, they tend to show bright components around the photon ring due to Faraday conversion around the BH (Y. Tsunetoe et al. 2020; M. Mościbrodzka et al. 2021; A. Ricarte et al. 2021; Event Horizon Telescope Collaboration et al. 2023; A. V. Joshi et al. 2024). Meanwhile, the conversion is insignificant (less than 0.01 in the optical depth) in the approaching jet. Here, the CP components are overall characterized by a bipolar pattern in the horizontal direction. That is, the positive components are distributed on the left side, while the negative in the right, for the prograde cases. They are switched for the retrograde cases, reflecting the relation between the polarity of magnetic fields and the observer's viewing angle.¹¹

This bipolar CP pattern is again interpreted with a combination of helical magnetic fields and relativistic aberration, as in Figure 7. It was previously recognized that a helical magnetic field configuration results in a bipolar or quadrant CP pattern on the image for an edge-on view (A. Ricarte et al. 2021; Y. Tsunetoe et al. 2021). Here, the aberration effect presents an effective edge-on-like view even for a non-edge line of sight, as shown by \hat{k}_{fld} , and produces the bipolar pattern in the images in Figure 16.

In addition, the CP component is perpendicular to $\cot \theta_B$ (θ_B is the angle between the light propagation vector and the magnetic field vector) in the optically thin case (e.g., T. W. Jones & S. L. O'Dell 1977), giving a large CP fraction for well-aligned or well-antialigned case (i.e., θ_B close to 0° or 180°). This results in brighter CP components in the left, de-beamed side of the jets in Figure 16.

Meanwhile, the images exhibit a monochromatic CP feature in the counter jet, rather than a bipolar one. On the counter side, the

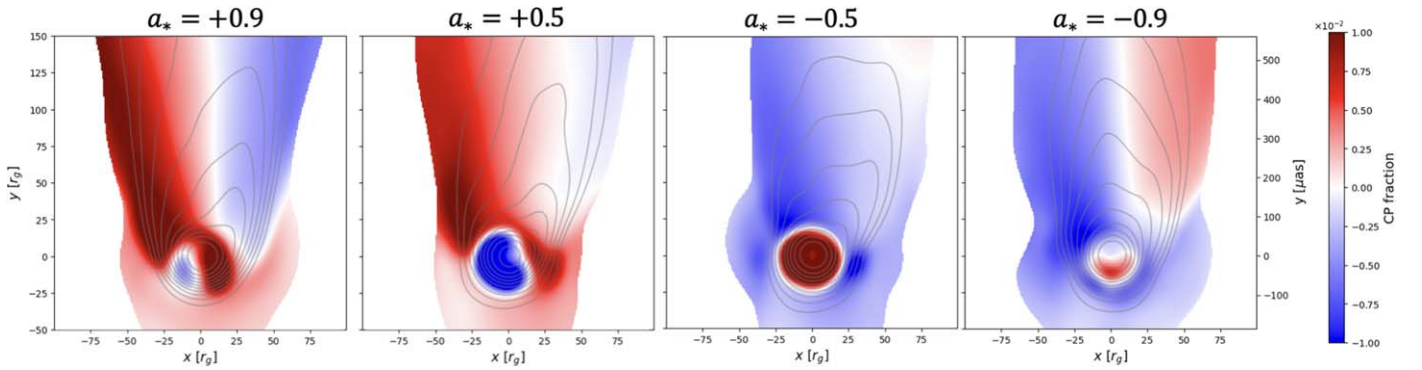


Figure 16. The CP maps for five models averaged over $5000 t_g$.

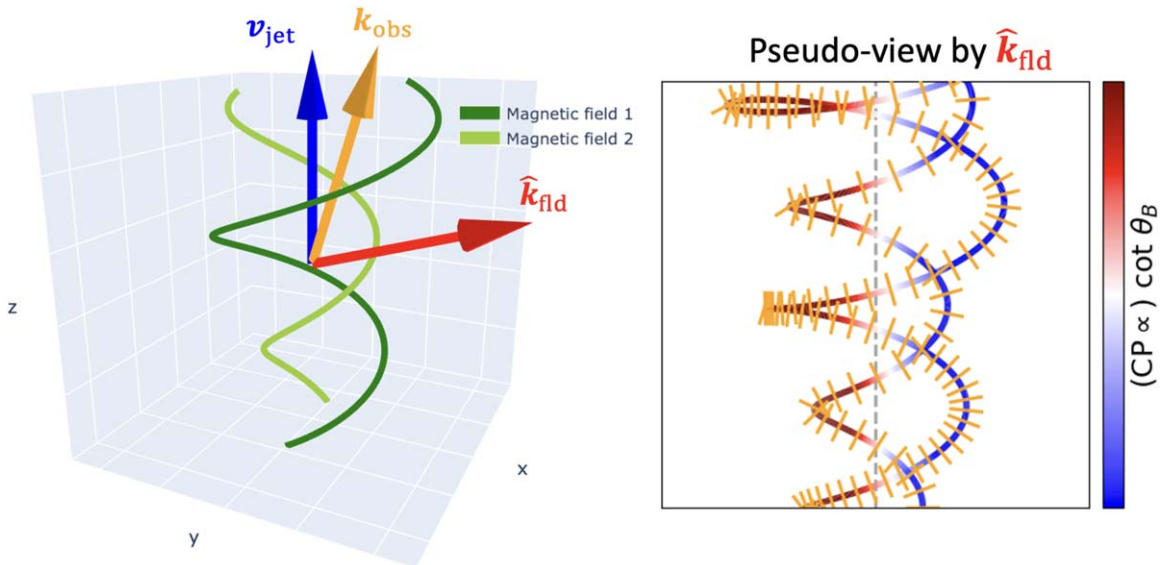


Figure 17. Same as Figure 7, but for less toroidal magnetic field lines.

¹¹ Here, the magnetic field polarity is determined by the initial setting in GRMHD simulation and is common with all the spin cases. Thus, the observer's viewing angle, $i = 163^\circ$ (prograde) and 17° (retrograde), results in the global magnetic fields pointing toward the observer in the prograde case and away from the observer in the retrograde case, respectively.

receding plasma bulk motion causes aberration, resulting in a more face-on-like view, in contrast to the approaching jet. As a result, \hat{k}_{fld} tends to align (or anti-align) with the magnetic field lines in the prograde (retrograde) spin cases, where $0 < \theta_B < 90^\circ$ ($90^\circ < \theta_B < 180^\circ$), producing positive (negative) CP components.

In the right panel of Figure 14, we show the CP image with relativistic effects turned off. Unlike the LP image, it exhibits a more asymmetric bipolar pattern, as the helical magnetic fields are viewed from a face-on-like angle. Here, the CP components along the vertical midline of the image ($x = 0$) are positive due to the vertical component of the magnetic fields, as illustrated in Figure 15. In the absence of relativistic aberration, the counter jet also displays a bipolar pattern.

The time-averaged CP images in Figure 16 also show a tendency to be more asymmetric in the lower spin cases, e.g., the borderline of the bipolar pattern is shifted to the right side for $a_* = \pm 0.5$ compared to $a_* = \pm 0.9$. This can also be explained by the presence of less toroidal magnetic fields. As shown in the pictures in Figure 17, the vertically dominated field lines weakly enhance the asymmetry of the bipolar CP pattern, causing the border to lean more to the right. Thus, they result in more asymmetric CP images in the lower spin cases.

ORCID iDs

Yuh Tsunetoe  <https://orcid.org/0000-0003-0213-7628>
 Ramesh Narayan  <https://orcid.org/0000-0002-1919-2730>
 Angelo Ricarte  <https://orcid.org/0000-0001-5287-0452>

References

- Ball, D., Sironi, L., & Özel, F. 2018, *ApJ*, 862, 80
 Blandford, R. D., & Königl, A. 1979, *ApJ*, 232, 34
 Blandford, R. D., & Znajek, R. L. 1977, *MNRAS*, 179, 433
 Broderick, A. E., & McKinney, J. C. 2010, *ApJ*, 725, 750
 Broderick, A. E., & Tchekhovskoy, A. 2015, *ApJ*, 809, 97
 Chael, A. 2024, *MNRAS*, 532, 3198
 Chael, A., Lupasca, A., Wong, G. N., & Quataert, E. 2023, *ApJ*, 958, 65
 Chatterjee, K., Liska, M., Tchekhovskoy, A., & Markoff, S. 2023, arXiv:2311.00432
 Chatterjee, K., & Narayan, R. 2022, *ApJ*, 941, 30
 Cruz-Orsorio, A., Fromm, C. M., Mizuno, Y., et al. 2022, *NatAs*, 6, 103
 Davelaar, J., Olivares, H., Porth, O., et al. 2019, *A&A*, 632, A2
 Davelaar, J., Ripperda, B., Sironi, L., et al. 2023, *ApJL*, 959, L3
 de Gasperin, F., Orrù, E., Murgia, M., et al. 2012, *A&A*, 547, A56
 Dexter, J., McKinney, J. C., & Agol, E. 2012, *MNRAS*, 421, 1517
 Dexter, J., Tchekhovskoy, A., Jiménez-Rosales, A., et al. 2020, *MNRAS*, 497, 4999
 Doleman, S. S., Barrett, J., Blackburn, L., et al. 2023, *Galax*, 11, 107
 Emami, R., Ricarte, A., Wong, G. N., et al. 2023, *ApJ*, 950, 38
 Event Horizon Telescope Collaboration, Akiyama, K., Alberdi, A., et al. 2019a, *ApJL*, 875, L1
 Event Horizon Telescope Collaboration, Akiyama, K., Alberdi, A., et al. 2019b, *ApJL*, 875, L5
 Event Horizon Telescope Collaboration, Akiyama, K., Algaba, J. C., et al. 2021a, *ApJL*, 910, L13
 Event Horizon Telescope Collaboration, Akiyama, K., Algaba, J. C., et al. 2021b, *ApJL*, 910, L12
 Event Horizon Telescope Collaboration, Akiyama, K., Alberdi, A., et al. 2022, *ApJL*, 930, L12
 Event Horizon Telescope Collaboration, Akiyama, K., Alberdi, A., et al. 2023, *ApJL*, 957, L20
 Event Horizon Telescope Collaboration, Akiyama, K., Alberdi, A., et al. 2024a, *ApJL*, 964, L26
 Event Horizon Telescope-Multi-wavelength science working group, Event Horizon Telescope Collaboration, Fermi Large Area Telescope Collaboration, et al. 2024b, *A&A*, 692, 140
 Fromm, C. M., Cruz-Orsorio, A., Mizuno, Y., et al. 2022, *A&A*, 660, A107
 Gelles, Z., Chael, A., & Quataert, E. 2024, *ApJ*, 981, 204
 Hada, K., Kino, M., Doi, A., et al. 2016, *ApJ*, 817, 131
 Igumenshchev, I. V., Narayan, R., & Abramowicz, M. A. 2003, *ApJ*, 592, 1042
 Johnson, M. D., Akiyama, K., Baturin, R., et al. 2024, *Proc. SPIE*, 13092, 130922D
 Jones, T. W., & O'Dell, S. L. 1977, *ApJ*, 214, 522
 Jorstad, S. G., Marscher, A. P., Mattox, J. R., et al. 2001, *ApJ*, 556, 738
 Jorstad, S. G., Marscher, A. P., Smith, P. S., et al. 2013, *ApJ*, 773, 147
 Joshi, A. V., Prather, B. S., Chan, C.-k., Wielgus, M., & Gammie, C. F. 2024, *ApJ*, 972, 135
 Kim, J.-S., Mueller, H., Nikonov, A. S., et al. 2024, arXiv:2409.00540
 Kim, J. Y., Krichbaum, T. P., Lu, R. S., et al. 2018, *A&A*, 616, A188
 Kramer, J. A., & MacDonald, N. R. 2021, *A&A*, 656, A143
 Laing, R. A. 1981, *ApJ*, 248, 87
 Lisakov, M. M., Kovalev, Y. Y., Savolainen, T., Hovatta, T., & Kutkin, A. M. 2017, *MNRAS*, 468, 4478
 Lu, R.-S., Asada, K., Krichbaum, T. P., et al. 2023, *Natur*, 616, 686
 Lyutikov, M., Pariev, V. I., & Blandford, R. D. 2003, *ApJ*, 597, 998
 Lyutikov, M., Pariev, V. I., & Gabuzda, D. C. 2005, *MNRAS*, 360, 869
 Marscher, A. P. 2014, *ApJ*, 780, 87
 Meringolo, C., Cruz-Orsorio, A., Rezzolla, L., & Servidio, S. 2023, *ApJ*, 944, 122
 Moriyama, K., Cruz-Orsorio, A., Mizuno, Y., et al. 2024, *ApJ*, 960, 106
 Mościbrodzka, M., Dexter, J., Davelaar, J., & Falcke, H. 2017, *MNRAS*, 468, 2214
 Mościbrodzka, M., Falcke, H., & Shiokawa, H. 2016, *A&A*, 586, A38
 Mościbrodzka, M., & Gammie, C. F. 2018, *MNRAS*, 475, 43
 Mościbrodzka, M., Janiuk, A., & De Laurentis, M. 2021, *MNRAS*, 508, 4282
 Murphy, E., Cawthorne, T. V., & Gabuzda, D. C. 2013, *MNRAS*, 430, 1504
 Najafi-Ziyazi, M., Davelaar, J., Mizuno, Y., & Porth, O. 2024, *MNRAS*, 531, 3961
 Narayan, R., Chael, A., Chatterjee, K., Ricarte, A., & Curd, B. 2022, *MNRAS*, 511, 3795
 Narayan, R., Igumenshchev, I. V., & Abramowicz, M. A. 2003, *PASJ*, 55, L69
 Niinuma, K., Kino, M., Doi, A., et al. 2015, *ApJL*, 807, L14
 Nikonov, A. S., Kovalev, Y. Y., Kravchenko, E. V., Pashchenko, I. N., & Lobanov, A. P. 2023, *MNRAS*, 526, 5949
 Ogihara, T., Kawashima, T., & Ohsuga, K. 2024, *ApJ*, 969, 22
 O'Sullivan, S. P., & Gabuzda, D. C. 2009, *MNRAS*, 393, 429
 Palumbo, D. C. M., Wong, G. N., & Prather, B. S. 2020, *ApJ*, 894, 156
 Pandya, A., Zhang, Z., Chandra, M., & Gammie, C. F. 2016, *ApJ*, 822, 34
 Pariev, V. I., Istomin, Y. N., & Beresnyak, A. R. 2003, *A&A*, 403, 805
 Porth, O., Fendt, C., Meliani, Z., & Vaidya, B. 2011, *ApJ*, 737, 42
 Porth, O., Mizuno, Y., Younsi, Z., & Fromm, C. M. 2021, *MNRAS*, 502, 2023
 Pushkarev, A. B., Kovalev, Y. Y., & Lister, M. L. 2010, *ApJL*, 722, L7
 Qiu, R., Ricarte, A., Narayan, R., et al. 2023, *MNRAS*, 520, 4867
 Rani, B., Krichbaum, T. P., Marscher, A. P., et al. 2014, *A&A*, 571, L2
 Ricarte, A., Narayan, R., & Curd, B. 2023a, *ApJL*, 954, L22
 Ricarte, A., Natarajan, P., Narayan, R., & Palumbo, D. C. M. 2025, *ApJ*, 980, 136
 Ricarte, A., Prather, B. S., Wong, G. N., et al. 2020, *MNRAS*, 498, 5468
 Ricarte, A., Qiu, R., & Narayan, R. 2021, *MNRAS*, 505, 523
 Ricarte, A., Tiede, P., Emami, R., Tamar, A., & Natarajan, P. 2023b, *Galax*, 11, 6
 Ripperda, B., Liska, M., Chatterjee, K., et al. 2022, *ApJL*, 924, L32
 Schinzel, F. K., Lobanov, A. P., Taylor, G. B., et al. 2012, *A&A*, 537, A70
 Tavecchio, F., Ghisellini, G., Bonnoli, G., & Ghirlanda, G. 2010, *MNRAS*, 405, L94
 Tchekhovskoy, A., Narayan, R., & McKinney, J. C. 2010, *ApJ*, 711, 50
 Tchekhovskoy, A., Narayan, R., & McKinney, J. C. 2011, *MNRAS*, 418, L79
 Tsunetoe, Y. 2023, PhD Thesis, Kyoto Univ.
 Tsunetoe, Y., Kawashima, T., Ohsuga, K., & Mineshige, S. 2024, *PASJ*, 76, 1211
 Tsunetoe, Y., Mineshige, S., Kawashima, T., et al. 2022, *ApJ*, 931, 25
 Tsunetoe, Y., Mineshige, S., Ohsuga, K., Kawashima, T., & Akiyama, K. 2020, *PASJ*, 72, 32
 Tsunetoe, Y., Mineshige, S., Ohsuga, K., Kawashima, T., & Akiyama, K. 2021, *PASJ*, 73, 912
 Walker, R. C., Hardee, P. E., Davies, F. B., Ly, C., & Junor, W. 2018, *ApJ*, 855, 128
 Wong, G. N., Prather, B. S., Dhruv, V., et al. 2022, *ApJS*, 259, 64
 Yang, H., Yuan, F., Li, H., et al. 2024, *SciA*, 10, eadn3544
 Yuan, F., Quataert, E., & Narayan, R. 2003, *ApJ*, 598, 301