

## $\rho\pi$ -RESONANCES

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In this letter we present a study of the distributions of two-pion effective masses from the decay of the  $A^+$  meson [1], now resolved into two peaks [2, 4]  $A$  and  $R$ . These distributions show evidence against the spin and parity assignments  $0^-, 1^-, 2^+$  and  $1^+$  ( $l=2$ ) for the lower mass peak,  $A$ , and against  $0^-$  and  $1^+$  ( $l=2$ ) for the upper mass peak,  $R$ . We also observe a possible enhancement in the  $\pi^+\pi^-$  mass spectrum at 550 MeV.

After analyzing about 5500 four prong events produced by  $3.5\text{ GeV}/c\pi^+$  in the Brookhaven National Laboratory 20-inch hydrogen bubble chamber we identified

1918 events as  $\pi^+ + p \rightarrow \pi^+ + p + \pi^+ + \pi^-$ .

The details of the analyzing methods have been described elsewhere. The  $M_{\pi^+\pi^-\pi^-}$  enhancements of these events have been shown to be associated both with  $\rho^0$  production and low momentum transfer,  $\Delta^2$ , to the proton. The data of Fig. 1, c in which the selection required at least one  $\rho$  and  $\Delta^2 < 36\mu^2$  as well as no  $N^*$ , suggest two peaks in agreement with the previous work of references [2, 4]. The solid curve is the expected phase space distribution for  $\pi p \rightarrow \rho\pi p$  averaged over the  $\rho$  mass, including the effect of the selection  $\Delta^2 < 36\mu^2$ . It has been normalized to the number of events above 1.53 GeV. We take the region 1040 GeV to 1210 MeV to represent the  $A$  peak and 1210 MeV to 1380 MeV to represent the  $R$  peak. Fig. 1, a is a Dalitz plot of those events in the  $A$  peak (dropping the  $\rho$  requirement) Fig. 1, b is a similar Dalitz plot for the events in the  $R$  peak. The events have been plotted twice, once above the diagonal and once below it. This has the advantage of presenting the  $\rho$  band as a straight line rather than having it make a  $90^\circ$  bend at the diagonal. Of course, the significance of the data must be judged on one-half of the plot only. The solid lines outline a band  $0.2\text{ GeV}^2$  wide and centered on the  $\rho$ .

The observed distribution of Fig. 1, c is presumably a mixture coming from  $\pi^+ + p \rightarrow A^+(R^+) + p$ ,  $\pi^+ + p \rightarrow p + 3\pi$  phase space; and  $\pi^+ + p \rightarrow p + \rho^0 + \pi^+$  without  $A^+$  or  $R^+$  formation. The last process is neglected in the following, since we do not observe it outside the  $A^+$  and  $R^+$  regions. Boson symmetrization requirements modify the two-pion effective mass spectrum from the decay of the  $A^+$  or  $R^+$  meson depending on the spin and parity ( $J^P$ ) of the  $A^+$  or  $R^+$ . These calculations have been made assuming that the  $A$  or  $R$  decay 100 percent of the time to  $\rho^0 + \pi^+$  [3]. The effects are displayed by a curve representing the profile of the Dalitz plot along the center of the  $\rho$  band. This profile has been calculated by taking the decay amplitude to be a sum of the two terms,  $A^+(R^+) \rightarrow \rho^0 + \pi_1^+$  and  $A^+(R^+) \rightarrow \rho^0 + \pi_2^+$ . The resulting density distribution has been averaged over the  $A^+(K^+)$  mass region, corrected for finite experimental resolution (estimated full-width-half-maximum = 25 MeV) and integrated over the  $0.2\text{ GeV}^2$  wide band in the Dalitz plot. Fig. 2, a shows the distribution of events along the bands of Fig. 1, a, b respectively. Care has been taken to avoid duplication of points in the cross over region. For the  $A^+$  region, we see that  $J^P = 1^-$  or  $2^+$  is a very poor fit, as is  $0^-$  or  $1^+$  ( $l=2$ ), while  $1^+$  ( $l=0$ ) or  $2^-$  is certainly satisfactory. The addition

	$J^P$	Percent $3\pi$ phase space	
		0	25
$R^+$	$1^-, 2^+$	.005	.01
	$2^+$	.008	.10
	$1^+ (l=0), 2^-$	.07	.10
	$0^-, 1^+ (l=2)$	<.001	<.001
$A^+$	$1^-, 2^+$	<.001	<.001
	$1^+ (l=0), 2^-$	.70	.70
	$0^-, 1^+ (l=2)$	<.001	.09

of  $3\pi$  phase space to the theoretical curves will not appreciably improve the fits except

for the  $0^-$  case, but it is still not favored. Table shows the  $\chi^2$  probabilities obtained for 25%

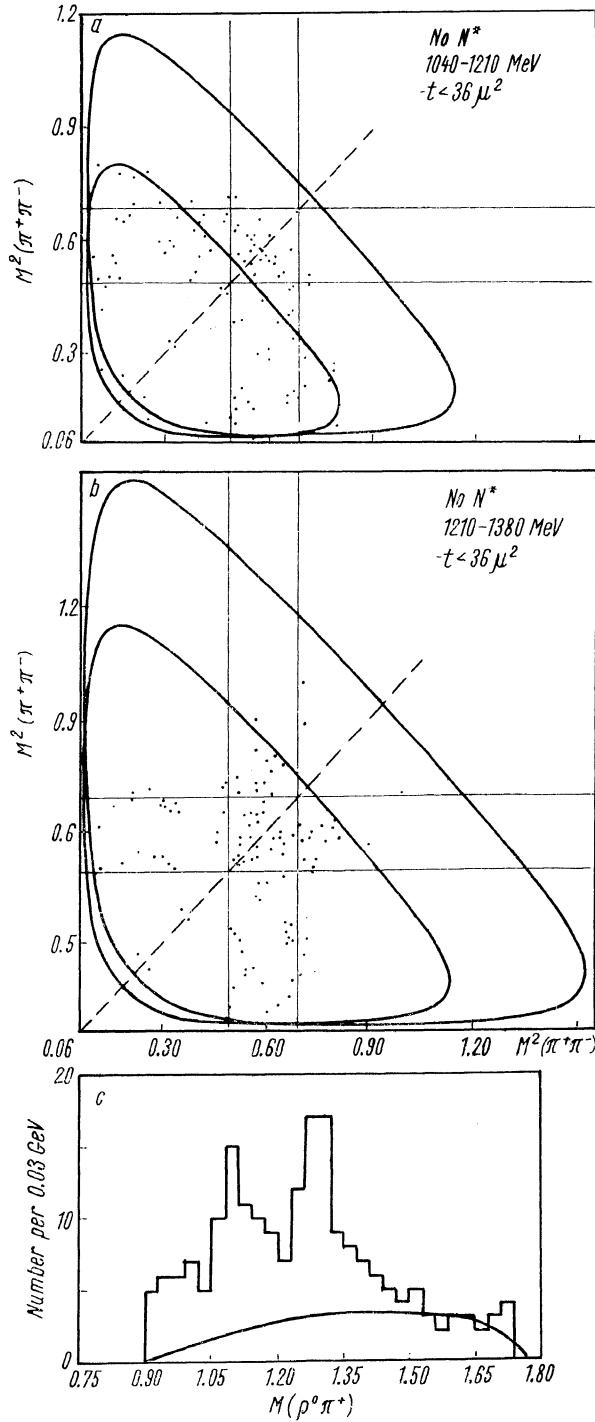


Fig. 1. (a) Dalitz plot of the three pions from the events with no  $N^*$  (1120-1320),  $-t(p, p) < 36 \mu^2$  and  $1040 \text{ MeV} < M(\pi^+\pi^+\pi^-) < 1210 \text{ MeV}$ ; (b) Similar to 1 (a) but with  $1210 \text{ MeV} < M(\pi^+\pi^+\pi^-) < 1380 \text{ MeV}$ ; (c) Effective mass plot of those events with no  $N^*$  (1120-1320),  $-t(p, p) < 36 \mu^2$  and  $q(\pi^+\pi^-)$  present.

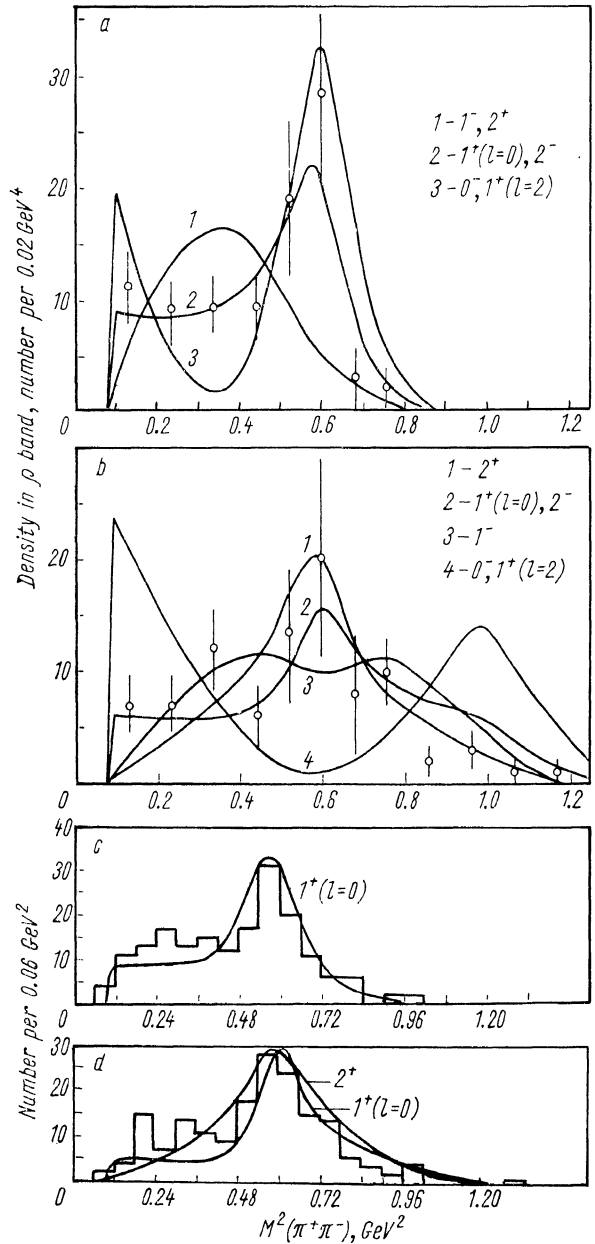


Fig. 2. (a) Distribution of the density of points on the Dalitz plots of Fig. 1 (a) within a band centered on the  $q$  and  $0.2 \text{ GeV}^2$  wide. The curves are theoretical expectations assuming  $A \rightarrow q + \pi$  without background; (b) Similar to 2 (a) but for the data of Fig. 1 (b); (c) Projection of the Dalitz plot of Fig. 1 (a); (d) Projection of the Dalitz plot of Fig. 1 (b).

$3\pi$  phase space background. For the  $R^+$  region the assignment  $0^-$  or  $1^+$  ( $l=2$ ) is very unlikely,  $1^-$  is better but also unlikely,  $1^+$  ( $l=0$ )

or  $2^-$  is quite possible, and  $2^+$  is also quite possible with the addition of  $3\pi$  phase space background. The  $0^-$  assignment is not appreciably improved by mixtures of  $3\pi$  background. The  $1^-$  assignment is possible with the addition of  $3\pi$  background, although  $1^+$  and  $2^+$  seem favored. Fig. 2, *c* and 2, *d* show the projections of the two Dalitz plots along with the theoretical curves for the more likely  $J^P$  choices.

If the  $K\bar{K}$  enhancement [2] at 1300 MeV is an alternate decay mode of the  $R$ , then  $2^+$

If the  $A^+$  is this kind of peak, it would not have definite angular momentum and our analysis would not apply.

The Bronzan-Low quantum number [6] for a  $\rho\pi$  state is  $-1$ , while for a  $K\bar{K}$  it is  $+1$ . Thus the  $K\bar{K}$  mode reported for the  $R$  meson would violate the conservation of this quantum number in strong interactions. The ratio  $\left(\frac{R^+K^+K^0}{R^+\rightarrow\rho\pi}\right)$  would indicate how much this quantum number is violated.

The ratio predicted by phase space is about

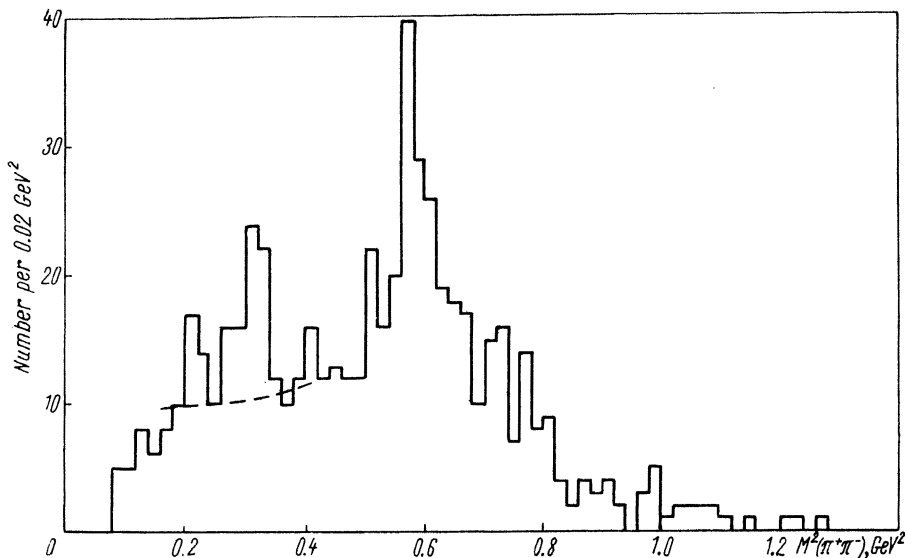


Fig. 3. Plot of the square of the effective mass  $M^2(\pi^+\pi^-)$  of the  $\pi^+$  and  $\pi^-$  from those events with no  $N^*(1120-1320)$  and with  $1040 < M(\pi^+\pi^+\pi^-) < 1380$ ,  $2 \times 294$  combinations.

is the lowest assignment allowed. The data reported here do not seriously contradict this assignment. However, the choice  $0^-$  for the  $A$  peak is favored by the data of Chung et al. [2], while our data do not lend much support at all to this assignment. Further, the  $\eta\pi$  enhancements proposed by Aderholz et al. [4] require  $J^P = 0^+, 1^-, 2^+, 3^-, 4^+$ , with the  $0^+$  forbidden if these  $\eta\pi$  enhancements represent alternate decay modes of the same resonances ( $A$  and  $R$ ) which decay to  $\rho+\pi$ . The  $A^+$  data of Fig. 2, *a* disagree rather strongly with  $1^-$  and  $2^+$ . Nauenberg and Pais [5] have discussed the possibility for peaks in meson systems due to the Peierls mechanism. They predict an enhancement in the  $\pi\rho$  system at 1090 MeV\*.

\* We have looked at the reaction  $\pi^+ + p \rightarrow p + \pi^+ + MM$  at 3.5 GeV/c where  $MM$  means two or more  $\pi^+$  mesons, and plotted the effective mass  $M(\pi^+, MM)$  of the  $\pi^+$  and the missing mass and

1.0 We have analyzed the  $\pi^+p \rightarrow \rho K^+K^0$  events in our data [7]. We do not observe the  $K^+K^0$  peak at the region of the  $R$  (due perhaps to limited statistics) but can set an upper limit of  $15 \mu\text{b}$ , which combined with the lower limit of  $100 \mu\text{b}$  for  $R(\rho^0\pi^+)$  gives an upper limit  $\sim \frac{1}{13}$  for the  $(K^+K^0/\rho\pi)$  branching.

If we remove the requirements that a  $\rho$  be present and that  $\Delta^2 < 35\mu^2$  and plot the  $M^2(\pi^+\pi^-)$  distributions for the  $A^+$  and  $R^+$  mass regions, we observe, in each case, an enhance-

observe the  $R$  (1310) but not the  $A$  (1090) in agreement with the prediction of the Peierls mechanism. On the other hand, our observations disagree with the predicted (R. J. Oakes, A. Pais, private communications) distribution in the  $\pi - \rho$  scattering angle for the  $A$  events in this paper. See D. Carmony et al. Proceeding of Dubna Conference, 1964.

cement in the region.  $26 \text{ GeV}^2 < M^2(\pi^+\pi^-) < 34 \text{ GeV}^2$ . Combining the data, we obtain the histogram of Fig. 3. As can be seen from the examples in Fig. 2, *a, b*, the theoretical curves for  $A^+ \rightarrow \rho + \pi$  and  $R^+ \rightarrow \rho + \pi$  do not produce this bump. We have studied the effect of mixing  $3\pi$  phase space with these curves and conclude that the expected distribution in the 550 region will not deviate appreciably from the dotted curve of Fig. 3. There are  $36 \pm 9$  events above this line (shaded region). This peak is not observed in the events with  $M^2 (+ + -)$  above the  $R^+$  peak, but its failure to appear in the low  $\Delta^2$  data argues against its association with the  $A$  and  $R$  peaks.

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