

# The $T_{c\bar{s}}(2900)$ as a threshold effect from the interaction of the $D^*K^*$ , $D_s^*\rho$ channels

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**Abstract.** We investigate the  $D^*K^*$  and  $D_s^*\rho$  interaction in coupled channels within the hidden gauge formalism. A structure is developed around their thresholds, short of producing a bound state, which leads to a peak in the  $D_s^+\pi^-$  mass distribution in the  $B^0 \rightarrow \bar{D}^0 D_s^+\pi^-$  decay compatible with the experimental data. We conclude that the interaction between the  $D^*K^*$  and  $D_s^*\rho$  is essential to produce the cusp structure that we associate to the recently seen  $T_{c\bar{s}}(2900)$ , and that its experimental width is mainly due to the decay width of the  $\rho$  meson. The peak obtained together with a smooth background reproduces fairly well the experimental mass distribution observed in the  $B_0 \rightarrow \bar{D}^0 D_s^+\pi^-$  decay.

## 1 Introduction

The  $D^*K^*$  system was investigated in [1] and three states were found corresponding to  $I = 0$ ;  $J^P = 0^+$ ,  $1^+$  and  $2^+$ . The  $2^+$  state was identified with the  $D_{s2}^*(2573)$  state, and served to set the scale for the regularization of the loops, allowing predictions in the other sectors. There, the  $I = 1$  interaction of the  $D^*K^*$  and  $D_s^*\rho$  channels was also studied and, a cusp was found for  $J = 0$  and  $J = 1$  around the  $D_s^*\rho$  threshold.

Recently, the LHCb Collaboration has observed an state in the  $D_s^+\pi^-$ ,  $D_s^+\pi^+$  mass distributions in the  $B^0 \rightarrow \bar{D}^0 D_s^+\pi^-$  and  $B^+ \rightarrow D^- D_s^+\pi^+$  decays, respectively, at 2900 MeV [2, 3]. Indeed, the state branded as  $T_{c\bar{s}}(2900)$  with  $J^P = 0^+$ , as seen in  $D_s^+\pi^-$  and  $D_s^+\pi^+$ , exhibits an  $I = 1$  character and it has also been associated with  $J^P = 0^+$ . On the other hand, 2900 MeV is just the threshold of the  $D^*K^*$  channel. Thus, one is finding a  $I = 1$   $J^P = 0^+$  state in the threshold of  $D^*K^*$  (the  $D_s^*\rho$  is only 14 MeV below neglecting the  $\rho$  width), which could correspond to the cusp found in [1].

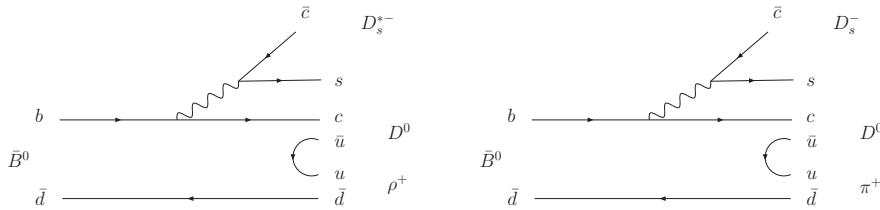
In the present work we look again at the interaction of  $D^*K^*$  and  $D_s^*\rho$  channels, taking into account the  $K^*$  and  $\rho$  widths and also the decay of the states found into the  $D_s\pi$  channel where it has been observed, comparing our results with the recent experimental findings.

## 2 Formalism

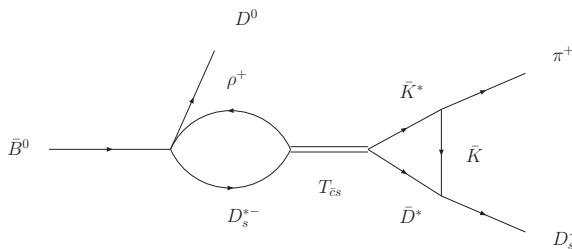
In Ref. [2] a peak is found in the  $D_s\pi$  invariant mass in the  $B^0 \rightarrow \bar{D}^0 D_s^+\pi^-$  and  $B^+ \rightarrow D^- D_s^+\pi^+$  decays. In order to have a  $b$  quark rather than a  $\bar{b}$  quark, we look at the reaction

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**Figure 1.** Left:  $\bar{B}^0$  decay to  $D_s^{*-} c \bar{d}$  with hadronization of the  $c \bar{d}$  pair to produce  $D_s^{*-} D^0 \rho^+$ . Right:  $\bar{B}^0$  decay into  $D_s^- D^0 \pi^+$  (contribution to the background).



**Figure 2.** Mechanism by means of which the resonance is produced and decays into  $\pi^+ D_s^-$ .

$\bar{B}^0 \rightarrow D^0 D_s^{*-} \rho^+$ . We produce this state with the external emission Cabibbo favored decay shown in Fig. 1 (left). In Fig. 1 (right) we depict the direct decay  $\bar{B}^0 \rightarrow D_s^- D^0 \pi^+$  considered as background.

We evaluate the scattering matrix using the Bethe-Salpeter equation in the  $D^* K^*$  and  $D_s^* \rho$  channels,

$$T = [1 - VG]^{-1} V, \quad (1)$$

with  $G$  the diagonal loop function for the intermediate mesons and  $V$  the transition potential. However, the state is observed in  $D_s \pi$ , hence, the mechanism by means of which the reaction proceeds is given in Fig. 2. The amplitude for the process of Fig. 2 is given by,

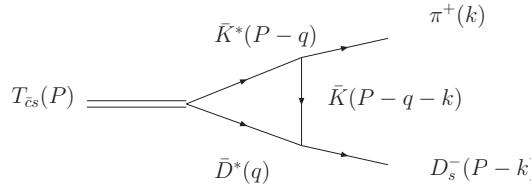
$$t = a G_{\rho D_s^*} (M_{\text{inv}}) t_{\rho D_s^* K^* D^*} (M_{\text{inv}}) \tilde{V} (\pi D_s, M_{\text{inv}}), \quad (2)$$

where  $a$  is a normalization constant that we do not evaluate, unnecessary to show the shape of the  $\pi D_s$  mass distribution in the  $\bar{B}^0$  decay, and  $M_{\text{inv}}$  is the invariant mass distribution of the  $D_s \pi$  final state. The vertex function  $\tilde{V}$  corresponding to the triangle loop of Fig. 3 can be easily evaluated.

We assume the resonance to be in  $J = 0$ , and that the vectors have small momenta with respect to their masses. Then, the structure of the triangle diagram of Fig. 3 is given by

$$\tilde{V} = -i \int \frac{d^4 q}{(2\pi)^4} \epsilon_{\bar{K}^*}^l \epsilon_{\bar{D}^*}^l \epsilon_{\bar{K}^*}^i \epsilon_{\bar{D}^*}^j \frac{(2k + q)^i (2k + q)^j}{(P - q - k)^2 - m_{\bar{K}}^2 + i\epsilon} \frac{\theta(q_{\text{max}} - q)}{(P - q)^2 - m_{\bar{K}^*}^2 + i\epsilon} \frac{1}{q^2 - m_{D^*}^2 + i\epsilon}. \quad (3)$$

The loop function  $\tilde{V}$  is naturally regularized with a cutoff  $q_{\text{max}}$ , the same one used to regularize the  $D^* K^*$  and  $D_s^* \rho$  loops when studying their interactions. The equivalent  $q_{\text{max}}$  used in [1] was 1100 MeV. We find,



**Figure 3.** Triangle diagram accounting for the  $R \rightarrow \pi \bar{D}_s$  decay of the  $R$  resonance of  $I = 1$  generated with the  $\rho \bar{D}_s$ ,  $\bar{D}^* \bar{K}^*$  coupled channels.

$$\tilde{V} = - \int \frac{d^3 q}{(2\pi)^3} \frac{(2\vec{k} + \vec{q})^2}{8\omega_{K^*}(q)\omega_{D^*}(q)\omega_K(\vec{q} + \vec{k})} \frac{1}{P^0 - \omega_{D_s^*}(q) - \omega_{K^*}(q) + i\epsilon} \\ \times \left\{ \frac{1}{P^0 - k^0 - \omega_{D^*}(q) - \omega_K(\vec{q} + \vec{k}) + i\epsilon} + \frac{1}{k^0 - \omega_{K^*}(q) - \omega_K(\vec{q} + \vec{k}) + i\epsilon} \right\}, \quad (4)$$

which shows the different cuts of the loop diagram when pairs of the internal particles of the loop are placed on-shell.

Then, we consider that the transition amplitude for  $\bar{B}^0 \rightarrow D^0 D_s^- \pi^+$  is given by a constant background (considering the dominance of s-wave in the coupling of the bottom meson to the pseudoscalars), see Fig. 1 (right), together with the scattering amplitude of the diagram in Fig. 2, which accounts for the interaction of the  $VV$  coupled channels. It reads as

$$t' = a G_{\rho D_s^*}(M_{\text{inv}}) t_{\rho D_s^*, K^* D^*}(M_{\text{inv}}) \tilde{V}(\pi D_s, M_{\text{inv}}) + b. \quad (5)$$

Therefore, the mass distribution of  $\pi D_s^-$  in the  $\bar{B}^0$  decay is given by,

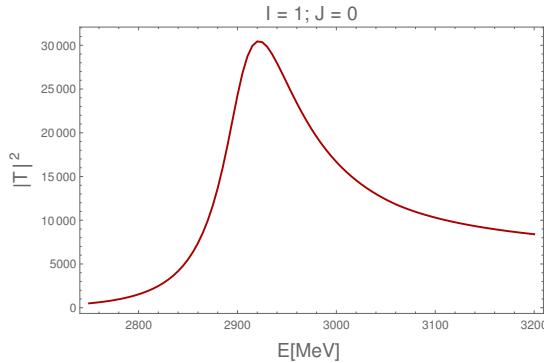
$$\frac{d\Gamma}{dM_{\text{inv}}} = \frac{1}{(2\pi)^3} \frac{1}{4M_B^2} p_{D^0} \tilde{p}_\pi |t'|^2, \quad (6)$$

$$\text{where } p_{D^0} = \frac{\lambda^{1/2}(M_B^2, m_{D^0}^2, M_{\text{inv}}^2)}{2M_B} \text{ and } \tilde{p} = \frac{\lambda^{1/2}(M_{\text{inv}}^2, m_{D_s}^2, m_\pi^2)}{2M_{\text{inv}}}.$$

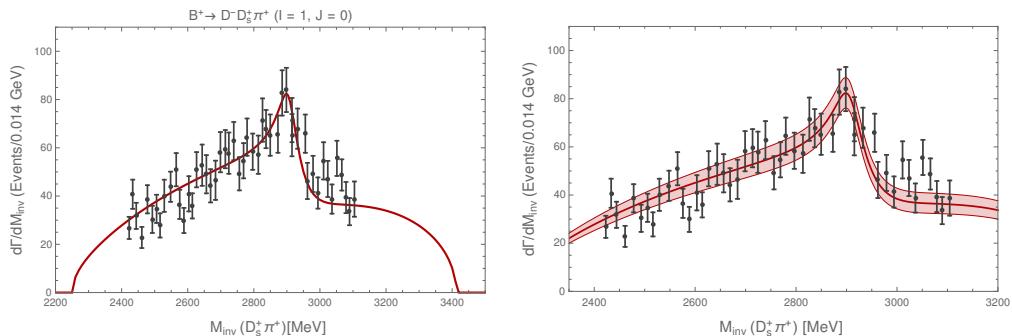
## 2.1 Results

We take into account the decay widths of the vector mesons  $K^*$  and  $\rho$  by means the convolution of the  $G$  function in Eq. (1) [4]. The result for the  $T$  matrix in  $I = 1; J = 0$  is shown in Fig. 4. The cusp obtained for  $J = 0$  has become wider. The position of the cusp is similar, it shows up slightly above the  $D^* K^*$  threshold and around 2920 MeV, with a width coming basically from the decay of the  $\rho$  into  $\pi\pi$ . We have also obtained visible peaks in the scattering amplitudes for  $J = 1$  and 2 [4].

Finally, we show the result of the invariant mass distribution of the decay  $\bar{B}^0 \rightarrow D_s^- D^0 \pi^+$ , Eq. (6), in comparison with the LHCb experimental data [2, 3] in Fig. 5 (left). In Eq. (6), we adjusted the constants  $a$  and  $b$  to reproduce well the experimental data around the  $T_{cs}(2900)$  resonance, and we obtain  $a = 2.1 \times 10^3$  and  $b = -1.45 \times 10^3$ . As can be seen, our model describes well the experimental data. A peak is obtained around the threshold of the  $D^* K^*$  channel. Since these results were obtained fixing the subtraction constant to obtain the  $T_{cs}(2900)$ , this also supports the molecular picture of this state as  $D^* \bar{K}^*$  of [5]. Thus, our



**Figure 4.**  $|T|^2$  for  $C = 1; S = 1; I = 1; J = 0$  with  $\alpha = -1.474$ .



**Figure 5.** Left: invariant mass distribution for  $D_s\pi$  from the decay  $B \rightarrow \bar{D}D_s\pi$  compared to the experimental data from Ref. [2, 3]. Right: the same but with the error band obtained by changing the parameter for the background ( $b$ ) 5% up and down.

model strongly supports the  $T_{c\bar{s}}(2900)$  as a cusp structure originated by the non-diagonal interaction  $D^*K^* \rightarrow D_s^*\rho$ , with a width mainly due to the decay of the  $\rho$  meson into  $\pi\pi$

Finally, it is interesting to give a band of errors by changing the background, we do this to show the sensitivity of the results to this background. We have done this, keeping the value of  $a$ , needed to get the strength of the peak of the distribution, by varying the parameter  $b$  of the background by 5% (up and down). This is shown in Fig. 5 (right). The band obtained overlaps with the errors of the data.

## References

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