

# The Energy Dependence of the Underlying Event in Hadronic Collisions

Rick Field

Department of Physics, University of Florida  
Gainesville, Florida, 32611, USA

June 19, 2012

## Abstract

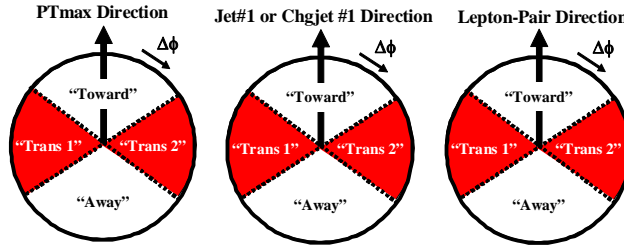
We study charged particles production ( $p_T > 0.5$  GeV/c,  $|\eta| < 1$ ) in proton-antiproton collisions at 300 GeV, 900 GeV, and 1.96 TeV. The 300 GeV and 900 GeV data are a result of the “Tevatron Energy Scan” which was performed just before the Tevatron was shut down. We use the direction of the leading charged particle in each event, PTmax, to define three regions of  $\eta$ - $\phi$  space; “toward”, “away”, and “transverse”. The “transverse” region is very sensitive to the “underlying event”. The data are corrected to the particle level and are compared with the PYTHIA 6.2 Tune A and Tune DW, and the PYTHIA 6.4 Tune Z1 at the particle level (*i.e.* generator level). The goal is to study the energy dependence of the underlying event by examining the behavior of the “transverse” region as a function of PTmax at three energies.

## I. Introduction

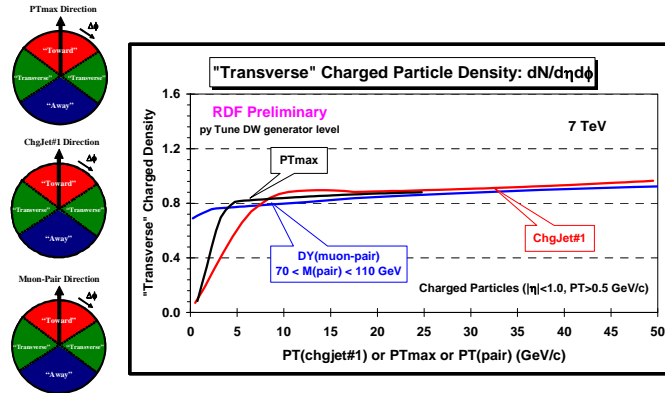
The total antiproton-proton cross section is the sum of the elastic and inelastic components,  $\sigma_{\text{tot}} = \sigma_{\text{EL}} + \sigma_{\text{IN}}$ . Three distinct processes contribute to the inelastic cross section; single diffraction, double-diffraction, and everything else which is referred to as “non-diffractive”. For elastic scattering neither of the beam particles breaks apart (*i.e.* color singlet exchange). For single and double diffraction one or both of the beam particles are excited into a high mass color singlet state (*i.e.*  $N^*$  states) which then decays. Single and double diffraction also corresponds to color singlet exchange between the beam hadrons. When color is exchanged the outgoing remnants are no longer color singlets and one has a separation of color resulting in a multitude of quark-antiquark pairs being pulled out of the vacuum. The “non-diffractive” component,  $\sigma_{\text{ND}}$ , involves color exchange and the separation of color. However, the “non-diffractive” collisions have both a “soft” and “hard” component. Most of the time the color exchange between partons in the beam hadrons occurs through a soft interaction (*i.e.* no high transverse momentum) and the two beam hadrons “ooze” through each other producing lots of soft particles with a uniform distribution in rapidity and many particles flying down the beam pipe. Occasionally, there is a hard scattering among the constituent partons producing outgoing particles and “jets” with high transverse momentum.

Min-bias (MB) is a generic term which refers to events that are selected with a “loose” trigger that accepts a large fraction of the overall inelastic cross section. All triggers produce some bias and the term “min-bias” is meaningless until one specifies the precise trigger used to collect the data. The CDF MB trigger requires at least one charged particle in the forward region  $3.2 < \eta < 5.9$  and simultaneously at least one charged particle in the backward region  $-5.9 < \eta < -3.2$ . The underlying event (UE) consists of the beam-beam remnants (BBR) and the multiple parton interactions (MPI) that accompany a hard scattering. The UE is an unavoidable background to

hard-scattering collider events. MB and UE are not the same object! The majority of MB collisions are “soft” while the UE is studied in events in which a hard-scattering has occurred. One uses the structure of the hard hadron-hadron collision to experimentally study the UE. As shown in Fig. 1, on an event-by-event bases, a “leading object” is used to define three regions of  $\eta$ - $\phi$  space. The pseudo-rapidity  $\eta = -\log(\tan(\theta_{\text{cm}}/2))$ , where  $\theta_{\text{cm}}$  is the center-of-mass polar scattering angle and  $\phi$  is the azimuthal angle of outgoing charged particles. In particular, the “transverse” region is roughly perpendicular to the plane of the hard 2-to-2 parton-parton scattering and is therefore very sensitive to the UE. The “leading object” can be the leading charged particle jet or calorimeter jet. It can also be the leading charged particle, PTmax, or a Z-boson.



**Fig. 1:** Illustration of correlations in azimuthal angle  $\Delta\phi$  relative to the direction of a “leading object” in the event. The relative angle  $\Delta\phi = \phi - \phi_L$ , where  $\phi_L$  is the azimuthal angle of the “leading object” and  $\phi$  is the azimuthal angle of a charged particle. The “toward” region is defined by  $|\Delta\phi| < 60^\circ$  and  $|\eta| < \eta_{\text{cut}}$ , while the “away” region is  $|\Delta\phi| > 120^\circ$  and  $|\eta| < \eta_{\text{cut}}$ . The two “transverse” regions  $60^\circ < -\Delta\phi < 120^\circ$ ,  $|\eta| < \eta_{\text{cut}}$  and  $60^\circ < \Delta\phi < 120^\circ$ ,  $|\eta| < \eta_{\text{cut}}$  are referred to as “transverse 1” and “transverse 2”. The overall transverse region corresponds to combining the transverse-1 and transverse-2 regions.



**Fig. 2:** Shows the charged particle density in the “transverse” region for charged particles ( $p_T > 0.5$  GeV/c,  $|\eta| < 1$ ) at 7 TeV as defined by the leading charged particle, PTmax, the leading charged particle jet, chgjet#1, and the muon-pair in Z-boson production as predicted from PYTHIA 6.2 Tune DW at the particle level. For Z-boson production the muon-pair are excluded from the charged particle density. Charged particle jets are constructed using the Anti-KT algorithm with  $d = 0.5$ .

In Run 1 at CDF we looked only at charged particles and used the leading charged particle jet to define the “transverse” region [1]. Later in Run 2 we studied the UE using the leading calorimeter jet and Z-bosons [2]. Figure 2 shows the charged particle density in the “transverse” region for charged particles at 7 TeV as defined by PTmax, PT(chgjet#1), and PT(muon-pair) as predicted from PYTHIA Tune DW. QCD Monte-Carlo generators such as PYTHIA [3] have parameters which may be adjusted to control the behavior of their event modeling. A specified set of these parameters that has been adjusted to better fit some aspects of the data is referred to as a tune [4,5]. The CDF PYTHIA 6.2 tune A was determined by fitting the CDF Run 1 UE data [1] and the PYTHIA 6.2 Tune DW does a very nice job in describing both the CDF Run 1 and Run 2 UE data [2]. However, Tune DW does not reproduce perfectly all the features of the LHC

data and after seeing the data one can construct improved LHC UE tunes [6]. The first CMS LHC tune was the PYTHIA 6.4 Tune Z1 [7]. Early LHC UE data used the PTmax approach to study the UE.

**Table 1.** Observables examined in this analysis as they are defined at the particle level and the detector level. Charged tracks are considered “good” if they pass the selection criterion given in Table 3. These observables are constructed in the “toward”, “away”, and “transverse” regions as defined by the leading charged particle, PTmax, as shown in Fig. 1. Events are required to have at least one charged particle with  $p_T > 0.5$  GeV/c and  $|\eta| < 1$  and PTmax is not included in the “toward” observables. For the average  $p_T$  and the PTmax we require that there is at least one charge particle present, while the charged particle and PTsum densities are taken to be zero if there are no charged particles present.

Observable	Particle Level	Detector level
$dN/d\eta d\phi$	Number of charged particles per unit $\eta$ - $\phi$ ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ )	Number of “good” charged tracks per unit $\eta$ - $\phi$ ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ )
$dPT/d\eta d\phi$	Scalar $p_T$ sum of charged particles per unit $\eta$ - $\phi$ ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ )	Scalar $p_T$ sum of “good” charged tracks per unit $\eta$ - $\phi$ ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ )
$\langle p_T \rangle$	Average $p_T$ of charged particles ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ ) Require at least 1 charged particle	Average $p_T$ of “good” charged tracks ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ ) Require at least 1 “good” track
PTmax	Maximum $p_T$ charged particle ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ ) Require at least 1 charged particle	Maximum $p_T$ “good” charged tracks ( $p_T > 0.5$ GeV/c, $ \eta  < 1$ ) Require at least 1 “good” track

The data for this analysis are collected with the CDF MB trigger and we study charged particles ( $p_T > 0.5$  GeV/c,  $|\eta| < 1$ ) that are produced in association with the leading charged particle, PTmax. As shown in Table 1, the observables are constructed in the “toward”, “away”, and “transverse” regions as defined by the leading charged particle, PTmax, as illustrated in Fig. 1. Events are required to have at least one charged particle with  $p_T > 0.5$  GeV/c and  $|\eta| < 1$  and PTmax is not included in the “toward” observables. For the average  $p_T$  and the PTmax we require that there is at least one charge particle present, while the charged particle and PTsum density is taken to be zero if there are no charged particles present. At present this note contains results only for the “transverse” charged particle density with  $p_T > 0.5$  GeV/c and  $|\eta| < 1$ . Soon this note will be updated to include the other observables. In addition, to compare with LHC UE studies [8] we will include all the observables also for the range  $p_T > 0.5$  GeV/c and  $|\eta| < 0.8$ .

In Section II we discuss the data and vertex selection and the track cuts. In Section III we correct the data to the particle level and construct the systematic errors. The techniques employed here are identical to those used in our previous CDF UE analyses and are documented in several CDF notes [9-11]. The results and comparisons with the PYTHIA tunes are shown in Section IV. Section V is reserved for summary and conclusions.

## II. Data Selection and Track Cuts

### (1) Data and Vertex Selection

Table 2 shows the data used in this analysis. We use all the 300 GeV and 900 GeV MB data. At 1.96 TeV we are currently including the MB data through period 10. At each energy we consider two sets of data. One set (V01) requires zero or one quality 12 vertex within  $|z| < 60$  cm and the other set (V1) requires events to have one and only one quality 12 vertex within  $|z| < 60$  cm.

**Table 2.** Number of MB events at 1.96 TeV (period 0-10), 900 GeV, and 300 GeV with 0 or 1 quality 12 vertex (V01) and with one and only one quality 12 vertex (V1).

Event Selection	1.96 TeV	900 GeV	300 GeV
“Good” Events	47,860,199	54,061,290	12,000,290
V01: 0 or 1 Q12 ZVtx, $ z  < 60$ cm	35,718,812	47,183,876	10,662,585
V1: 1 Q12 ZVtx, $ z  < 60$ cm	26,684,272	29,921,921	5,251,686

**Table 3.** Track selection criterion, where  $d_0$  is the transverse impact parameter. For events with one quality 12 vertex we require  $|z - z_{Q12}| < \Delta Z_{\text{cut}}$ , where  $z - z_{Q12}$  is the longitudinal distance between the measured track and the primary quality 12 vertex. For events with no quality 12 vertex we require  $|z - z_{\text{max}}| < 2\Delta Z_{\text{cut}}$ , where  $z - z_{\text{max}}$  is the longitudinal distance between the measured track and the leading track (*i.e.* PTmax).

Track Selection (loose)	Track Selection (tight)
COT measured tracks	COT measured tracks
$ d_0  < 1.0$ cm (beam corrected)	$ d_0  < 0.5$ cm (beam corrected)
$\Delta Z_{\text{cut}} = 3$ cm	$\Delta Z_{\text{cut}} = 2$ cm
NumAXseg(COT) $\geq 2$	NumAXseg(COT) $\geq 2$
NumAXhits(COT) $\geq 10$	NumAXhits(COT) $\geq 10$
$\chi^2(\text{track fit})/\text{DoF} < 10$	$\chi^2(\text{track fit})/\text{DoF} < 10$
$0.5 \text{ GeV}/c < p_T < 150 \text{ GeV}/c$	$0.5 \text{ GeV}/c < p_T < 150 \text{ GeV}/c$
$ \eta  < 1$	$ \eta  < 1$

### (2) Track Cuts (Loose and Tight)

We consider only COT measured charged tracks in the region  $0.5 < p_T < 150 \text{ GeV}/c$  and  $|\eta| < 1$  where efficiency is high. The upper limit of  $150 \text{ GeV}/c$  is chosen to prevent miss-measured tracks with very high  $p_T$  from contributing to the observables in Table 2 (at high  $p_T$  the track resolution deteriorates). As Table 3 shows, we employ both a “loose” and a “tight” track criterion. For both the “tight” and “loose” case the transverse impact parameter is corrected for the beam position. Both the “loose” and “tight” data are corrected to the particle level (with different correction factors) and the differences are used as a systematic error. Table 4 shows the

remaining number of events with at least one charged particle with  $p_T > 0.5$  GeV/c and  $|\eta| < 1.0$  at each energy for the three datasets: TC1\_V01, LC1\_V01, and TC1\_V1.

**Table 4.** Number of events with at least one charged particle with  $p_T > 0.5$  GeV/c and  $|\eta| < 1.0$ .

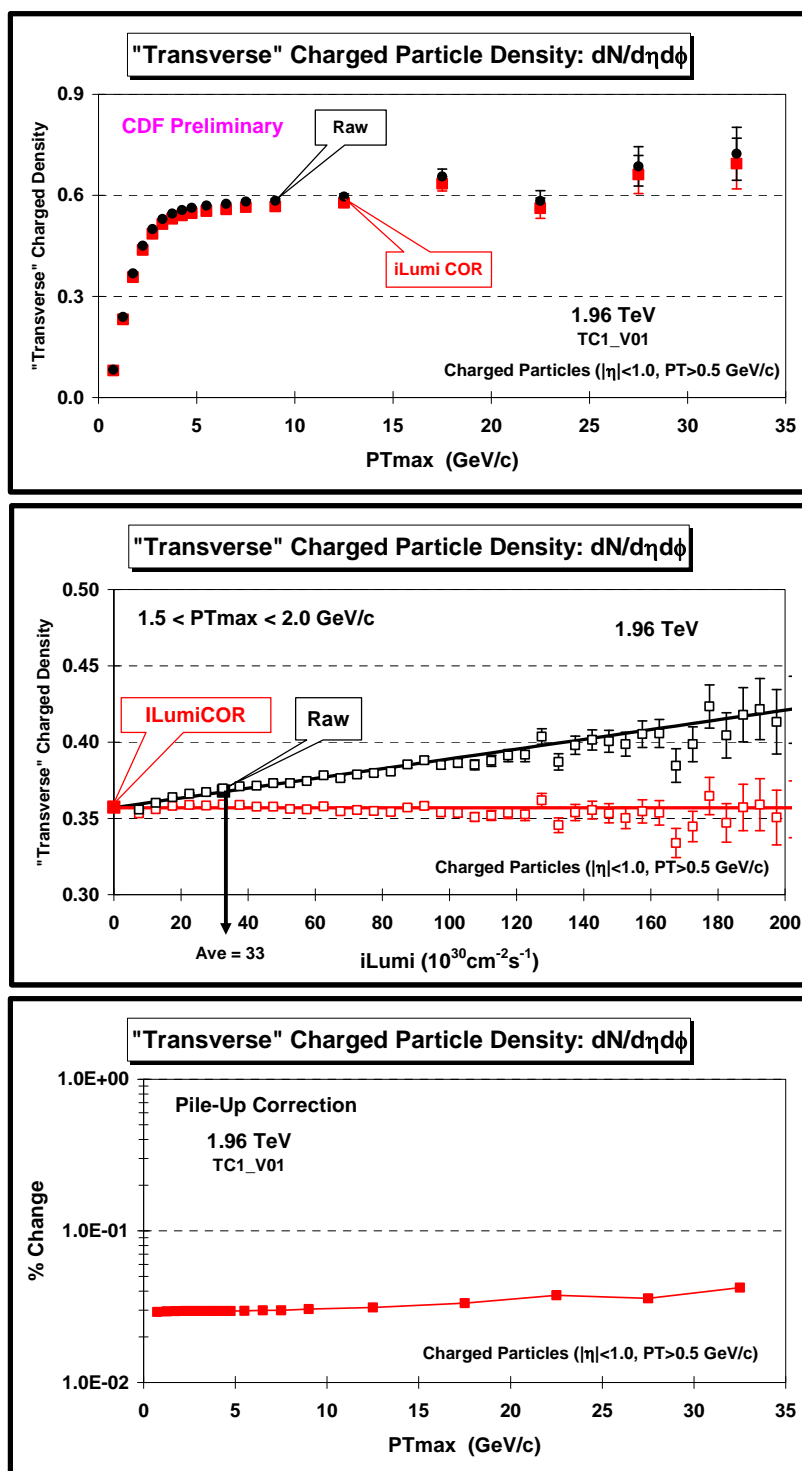
Data Set	1.96 TeV	900 GeV	300 GeV
TC1_V01: (0 or 1 ZVtx, tight track cuts)	30,262,961	37,075,521	7,233,840
LC1_V01: (0 or 1 ZVtx, loose track cuts)	30,986,931	38,306,127	7,484,571
TC1_V1: (1 ZVtx, tight track cuts)	25,371,145	28,524,566	4,886,354

### III. Correcting the Data to the Particle Level

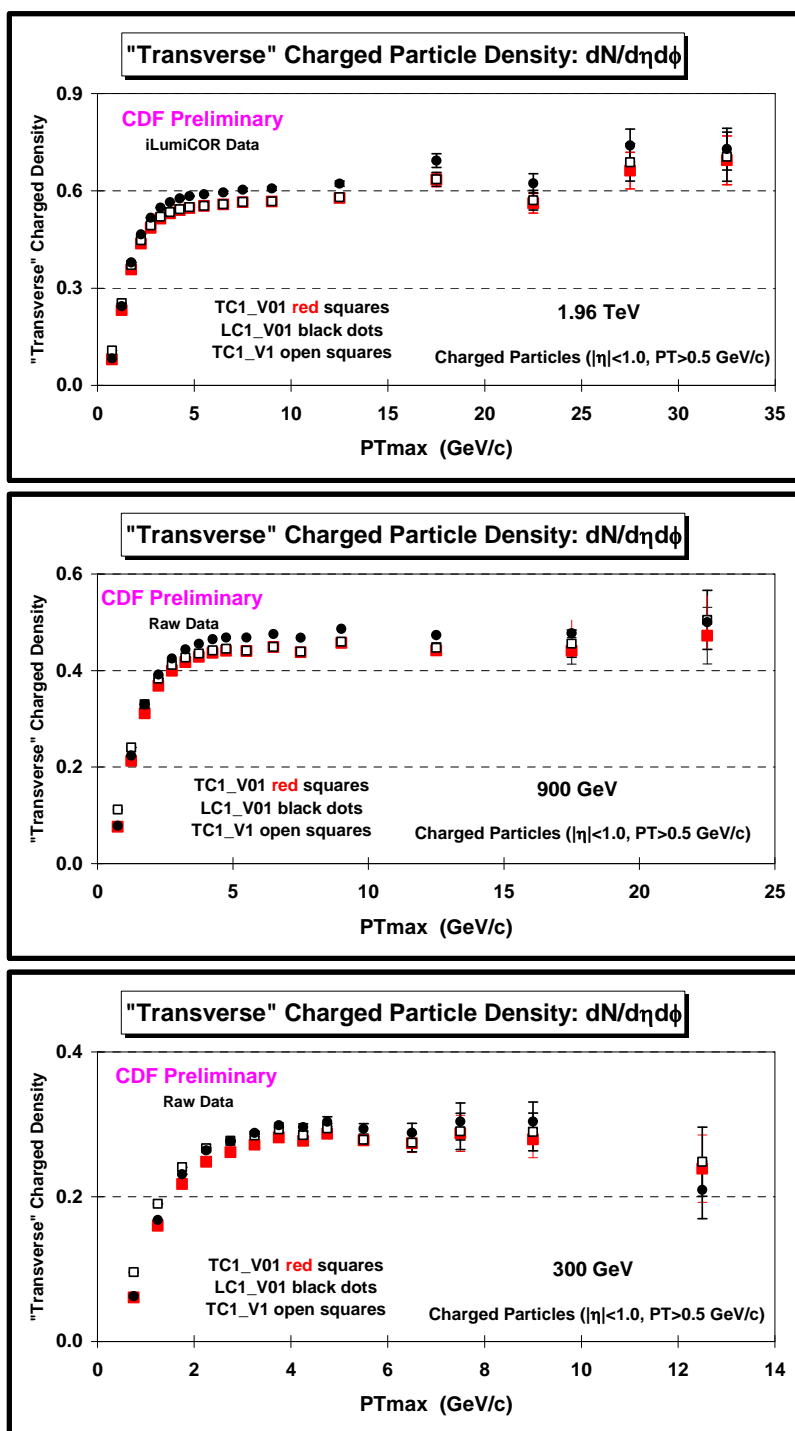
#### (1) Pile-Up Corrections at 1.96 TeV

Although we require zero or one quality 12 vertex, the observables in Table 1 can still be affected by pile-up (*i.e.* more than one proton-antiproton collision in the event). Tracks are required to point back to the primary vertex, but the track observables are affected by pile-up when two vertices overlap. Vertices within about 3 cm of each other merge together as one. Fig. 3 shows how pile-up affects the “transverse” charged particle density at 1.96 TeV. Large luminosity implies more pile-up. The average luminosity in this data set about  $33 \times 10^{30} \text{ cm}^{-2}\text{s}^{-1}$ . Fig. 3 shows the dependence of the raw data on the instantaneous luminosity for the “transverse” charged particle density at 1.96 TeV as defined by the leading charged particle,  $PT_{\text{max}}$ , with  $1.5 < PT_{\text{max}} < 2.0$  GeV/c. Each  $PT_{\text{max}}$  bin is plotted versus the instantaneous luminosity,  $iLumi$ , and fit to a straight line. This function is then used to correct the data for pile-up on an event-by-event bases resulting in the corrected ( $iLumiCOR$ ) values shown in Fig. 3. As can be in Fig. 3 the pile-up corrections are less than 4%. The luminosities at 300 GeV and 900 GeV are so small that there is no need for pile-up corrections at these energies.

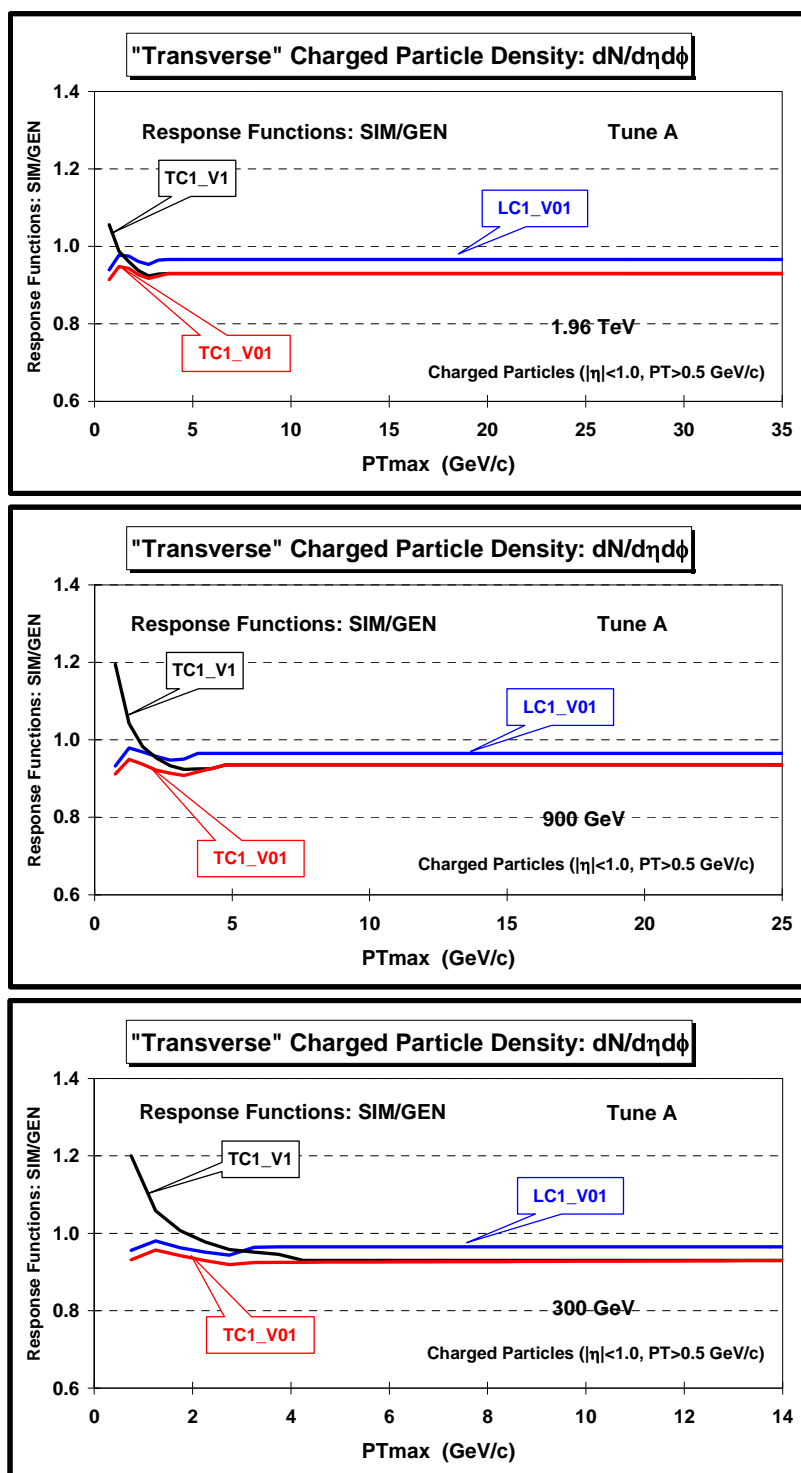
Figure 4 shows the pile-up corrected data on the “transverse” charged particle density at 1.96 TeV for the three datasets: TC1\_V01, LC1\_V01, TC1\_V1. Fig. 4 also shows the raw data at 300 GeV and 900 GeV for the three data sets. For  $PT_{\text{max}} < 4$  GeV/c there is a sizable difference between TC1\_V01 and TC1\_V1. Requiring at least one quality 12 vertex biases the data toward more active events. Most events with  $PT_{\text{max}} > 4$  GeV/c, however, have at least one quality 12 vertex and hence TC1\_V01 and TC1\_V1 become the same. TC1\_V01 and LC1\_V01 differ slightly at all  $PT_{\text{max}}$  values. The “loose” track cuts accept more tracks than the “tight” track cuts.



**Fig. 3.** (top) Shows the raw data (TC1\_V01) and the pile-up corrected data (iLumiCOR) on the “transverse” charged particle density at 1.96 TeV as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (middle) Shows the dependence of the raw data (TC1\_V01, black open squares) and the pile-up corrected data (iLumiCOR, red open squares) on the the instantaneous luminosity for the “transverse” charged particle density at 1.96 TeV as defined by the leading charged particle,  $PT_{max}$ , with  $1.5 < PT_{max} < 2.0$  GeV/c. The overall raw data point (solid black square) is plotted at the average instantaneous luminosity value of  $33 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$  and the pile-up corrected data point (solid red square) is plotted at zero instantaneous luminosity. (bottom) Shows the percent change due to the pile-up corrections versus  $PT_{max}$ .

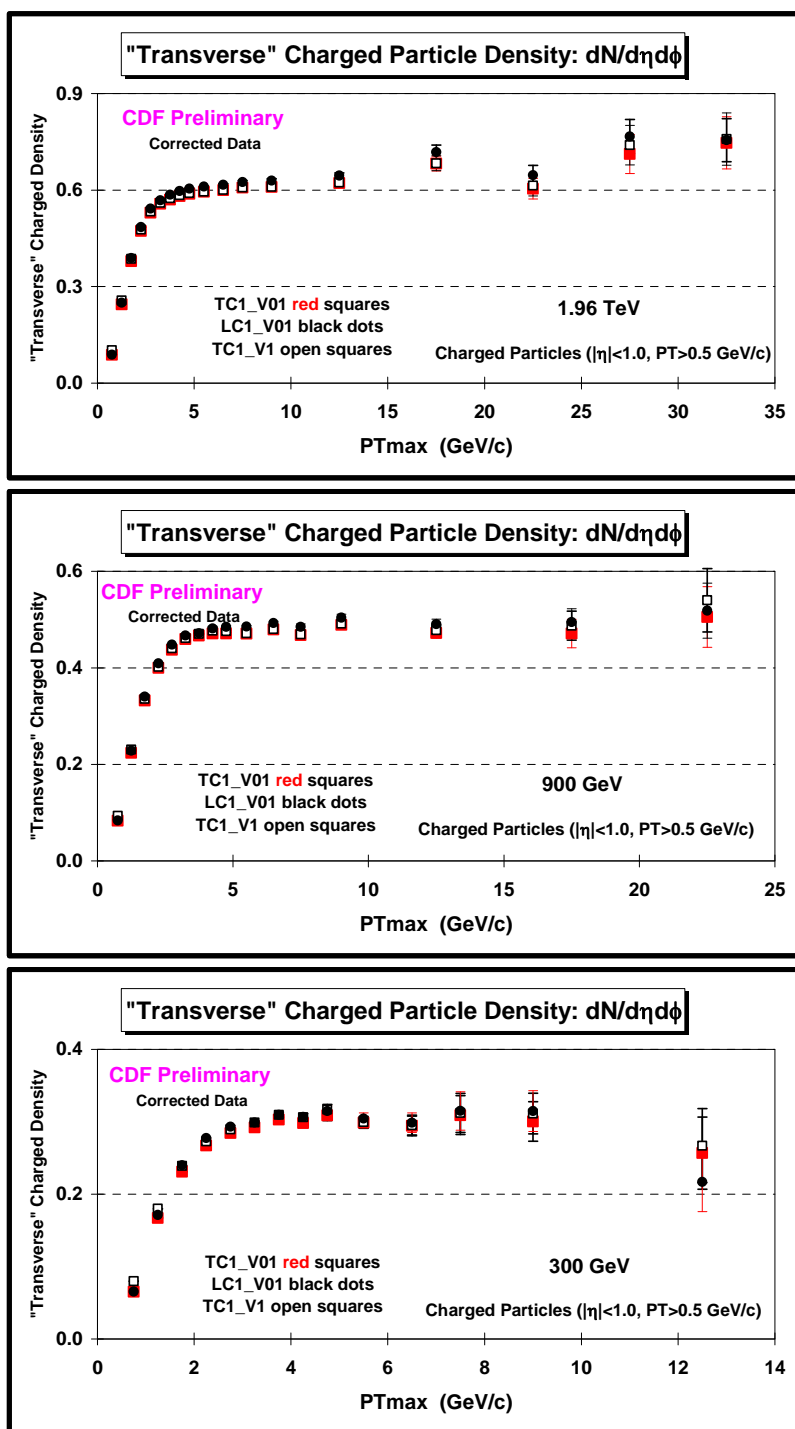


**Fig. 4.** (top) Shows the pile-up corrected data (TC1\_V01, LC1\_V01, TC1\_V1) on the “transverse” charged particle density at 1.96 TeV as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (middle) Shows the raw data (TC1\_V01, LC1\_V01, TC1\_V1) on the “transverse” charged particle density at 900 GeV as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (bottom) Shows the raw data (TC1\_V01, LC1\_V01, TC1\_V1) on the “transverse” charged particle density at 300 GeV as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ .



**Fig. 5.** Shows the ratio of the detector level to the particle level, SIM/GEN, for TC1\_V01, LC1\_V01, and TC1\_V1 from PYTHIA Tune A (*i.e.* response factors) for the “transverse” charged particle density at 1.96 TeV (*top*), 900 GeV (*middle*), and 300 GeV (*bottom*) as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$ .





**Fig. 6.** Shows the corrected data (TC1\_V01, LC1\_V01, TC1\_V1) on the “transverse” charged particle density at 1.96 TeV (*top*), 900 GeV (*middle*), and 300 GeV (*bottom*) as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ .

## (2) “Response” and “Correction” Factors

We use the “one-step” method to correct the data to the particle level [9-11]. PYTHIA Tune A is used to calculate the observables in Table 1 at the particle level in bins of the highest  $p_T$  charged particle  $PT_{max}$  (GEN) and at the detector level in bins the highest  $p_T$  track (uncorrected) (SIM). The detector level data in bins of the highest  $p_T$  track (uncorrected) are corrected by multiplying by the QCD Monte-Carlo “correction” factor, GEN/SIM, as described in Table 5. We refer to the ratio SIM/GEN as the “response” factor with the “correction” factor being the reciprocal. Smooth curves are drawn through the QCD Monte-Carlo predictions at both the generator level (GEN) and the detector level (SIM) to aid in comparing the theory with the data and also to construct the “correction” factors. Fig. 5 shows the ratio of the detector level to the particle level, SIM/GEN, for TC1\_V01, LC1\_V01, and TC1\_V1 from PYTHIA Tune A (*i.e.* response factors) for the “transverse” charged particle density at 1.96 TeV, 900 GeV, and 300 GeV.

**Table 5.** PYTHIA Tune A is used to calculate the observables in Table 1 at the particle level in bins of the highest  $p_T$  charged particle  $PT_{max}$  (GEN) and at the detector level in bins of the highest  $p_T$  track (*uncorrected*). The detector level data in bins of the highest  $p_T$  track (*uncorrected*) are corrected by multiplying by QCD Monte-Carlo factor, GEN/SIM.

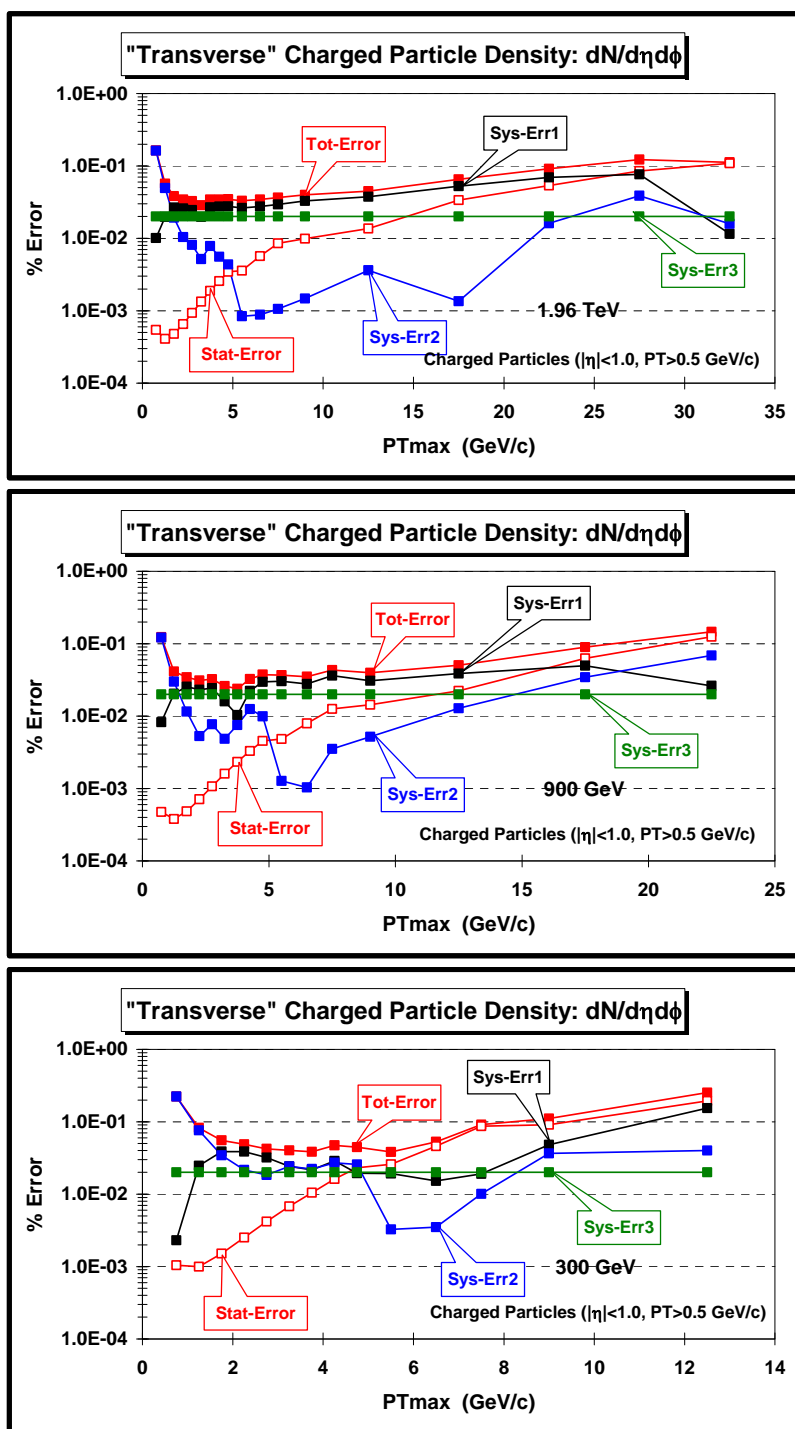
Particle Level Observable	Detector Level Observable	“Response” Factor	“Correction” Factor
GEN = Charged Particles $PT_{max}$ Bin	SIM = Good Tracks Max Track Bin	SIM/GEN	GEN/SIM

## (2) Systematic Uncertainties

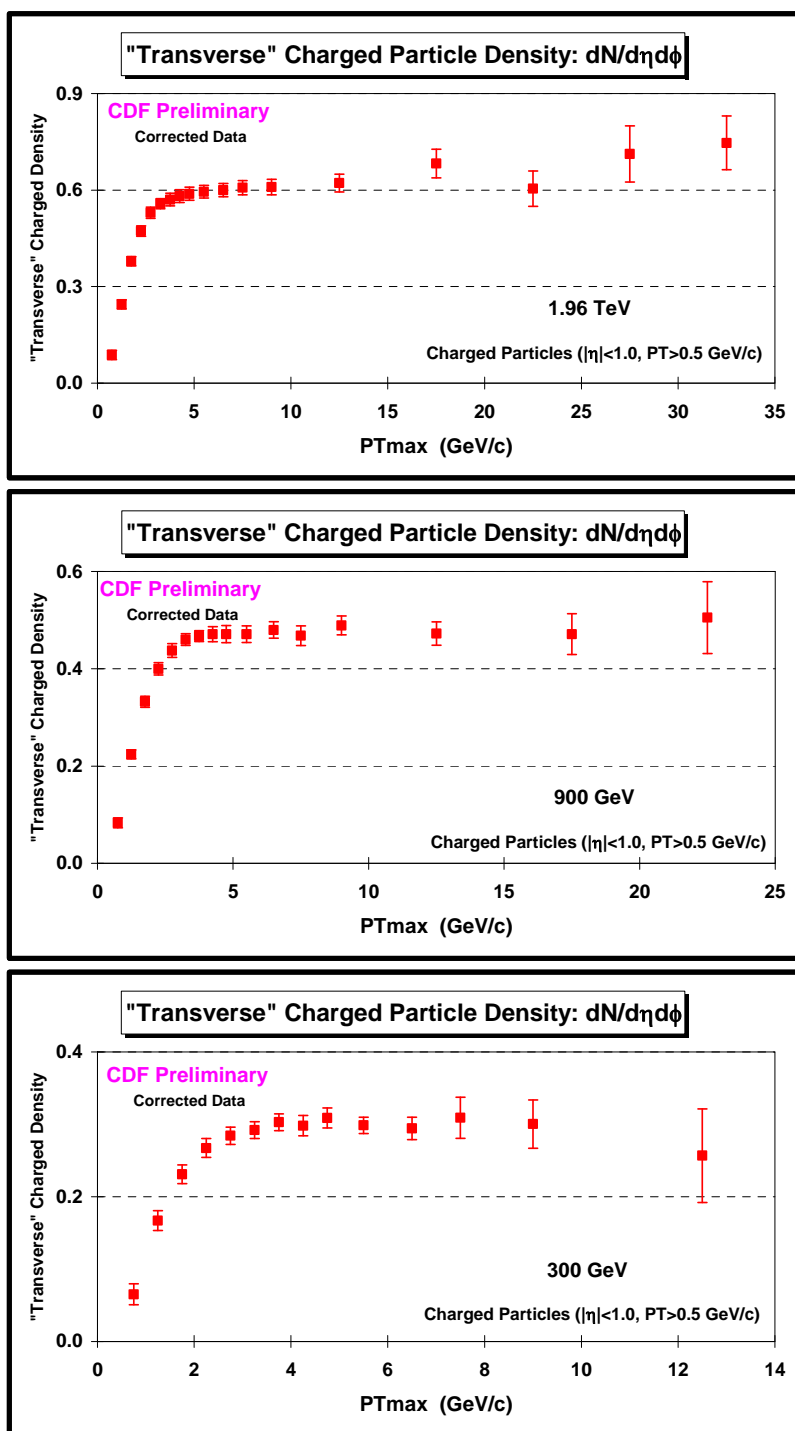
The three datasets are each corrected to the particle level using their corresponding “correction factors” as shown in Fig. 6. If PYTHIA Tune A fit the data perfectly and if CDFSIM was perfect then the corrected data from the three methods, TC1\_V01, LC1\_V01, and TC1\_V1 would all be identical. As shown in Table 6, the differences between the three methods are used as systematic errors. Fig. 7 shows the percentage statistical and systematic errors on the “transverse” charged particle density the three energies. The overall total error (Tot-Error) results from adding statistical error in quadrature with the three systematic errors. At low  $PT_{max}$  the overall error is dominated by Sys-Err2, while at large  $PT_{max}$  the overall error is predominately statistical.

**Table 6.** The errors on the corrected observables in Table 1 include both the statistical error and the systematic uncertainty (added in quadrature). The overall systematic uncertainty includes the uncertainties shown below. Sys-Err3 is included to take into account the accuracy of constructing the smooth theory curves.

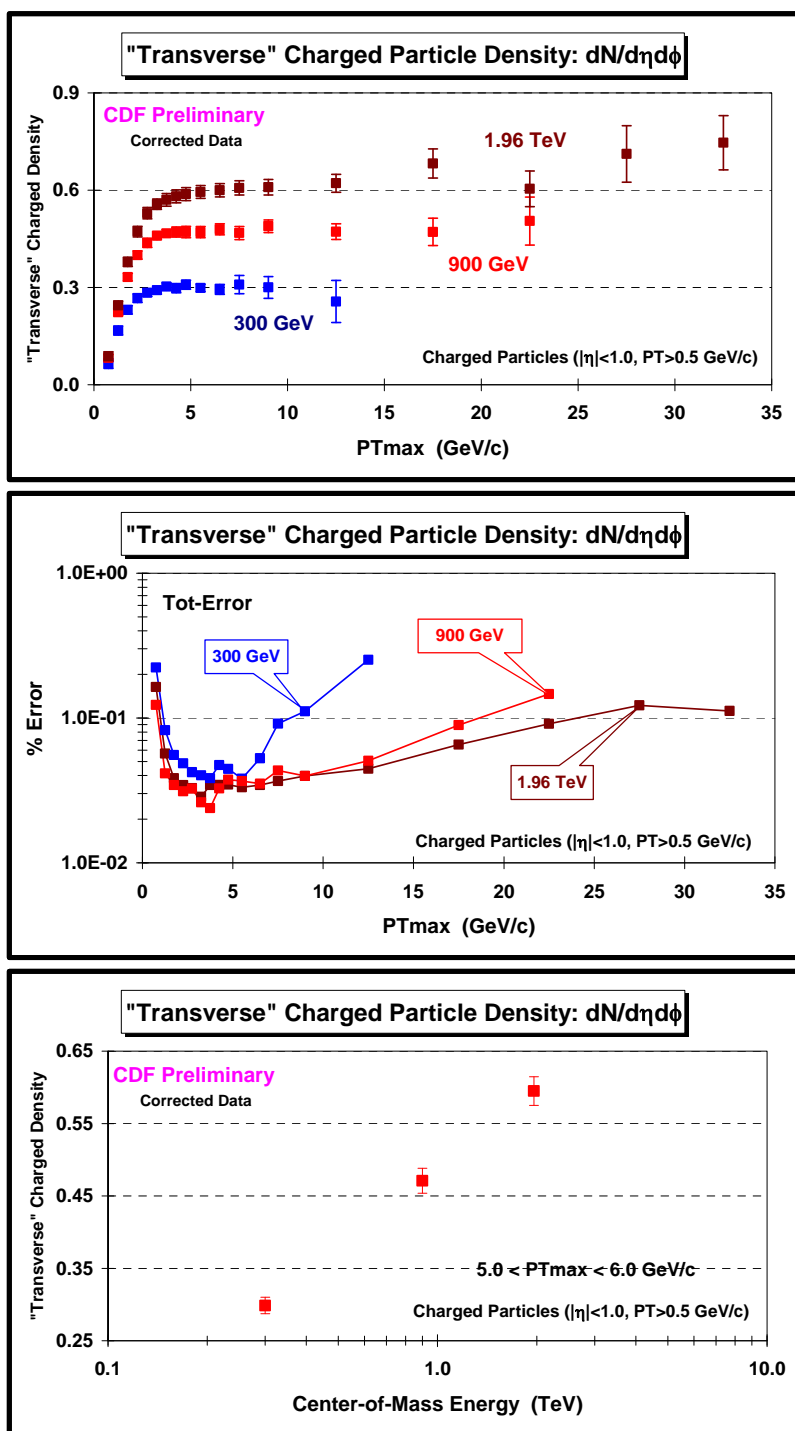
Uncertainty	Origin
Sys-Err1	Bin by bin difference between the corrected data for LC1_V01 and TC1_V01.
Sys-Err2	Bin by bin difference between the corrected data for TC1_V1 and TC1_V01.
Sys-Err3	2%



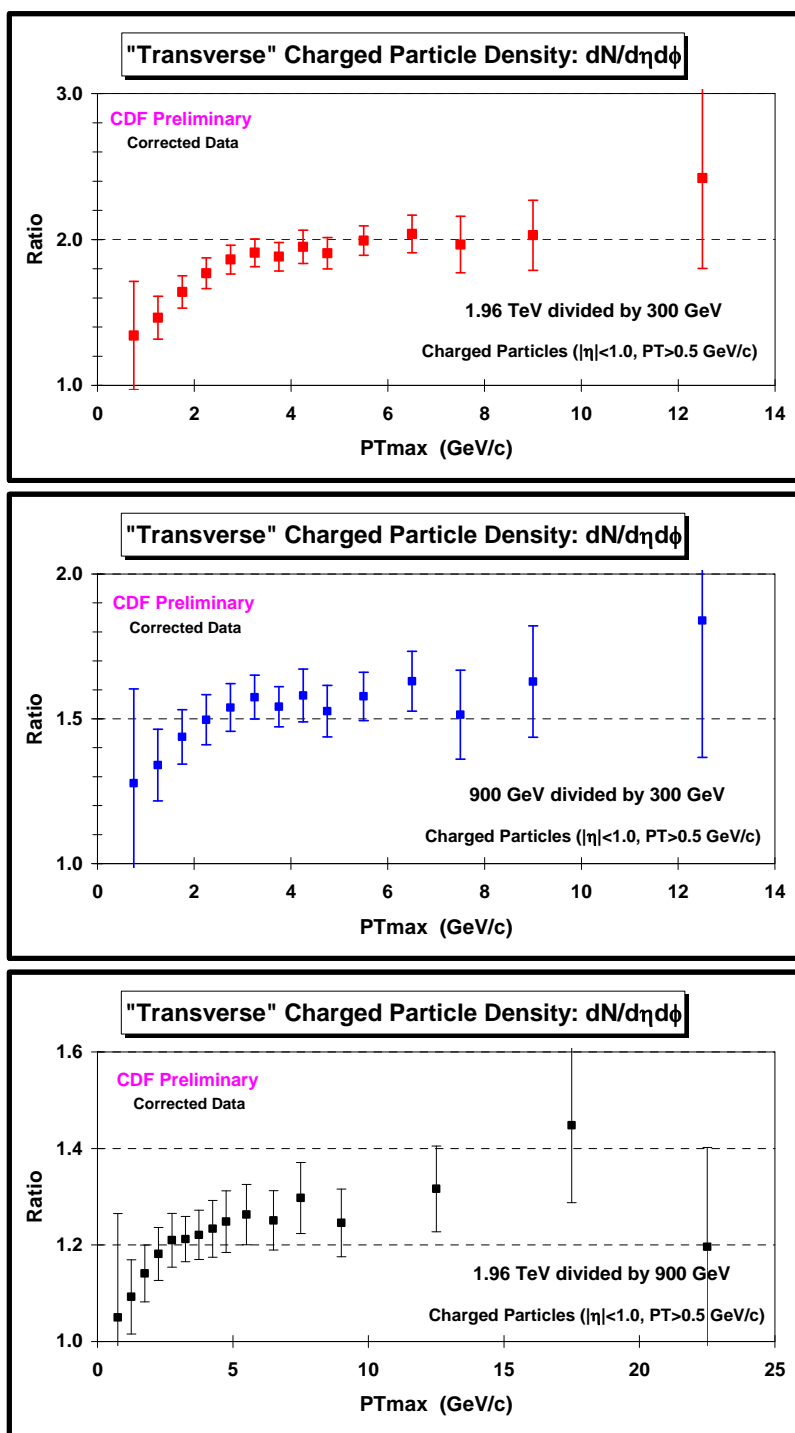
**Fig. 7.** Shows the percentage statistical and systematic errors on the “transverse” charged particle density at 1.96 TeV (*top*), 900 GeV (*middle*), and 300 GeV (*bottom*) as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . Stat-Error is the statistical error,  $Sys-Err1 = |LC1\_V01 - TC1\_V01|/TC1\_V01$ ,  $Sys-Err2 = |TC1\_V01 - TC1\_V1|/TC1\_V01$ , and  $Sys-Err3 = 2\%$ . The overall total error (Tot-Error) results from adding statistical error in quadrature with the three systematic errors.



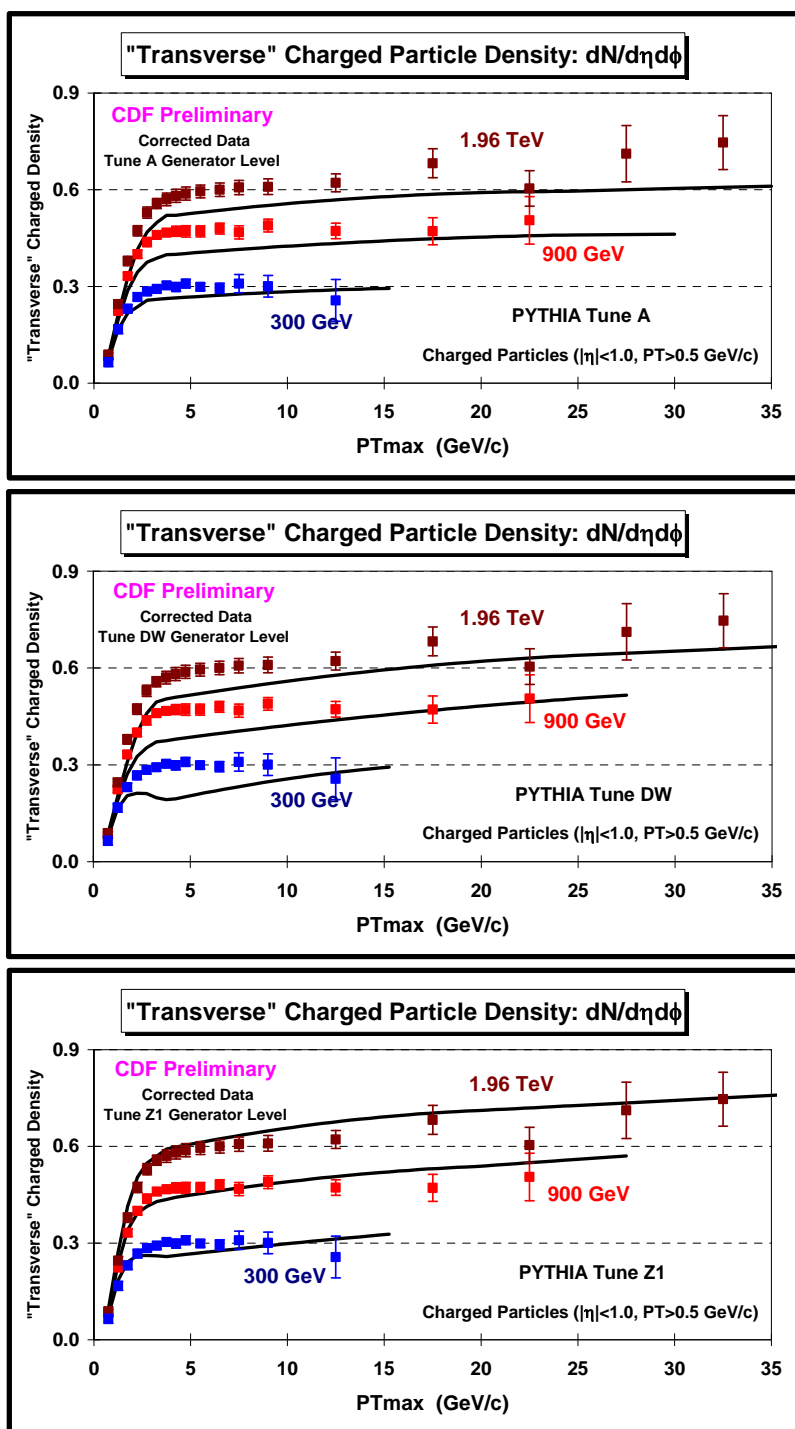
**Fig. 8.** Data at 1.96 TeV (*top*), 900 GeV (*middle*), and 300 GeV (*bottom*) on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . The data are corrected to the particle level with errors that include both the statistical error and the systematic uncertainty.



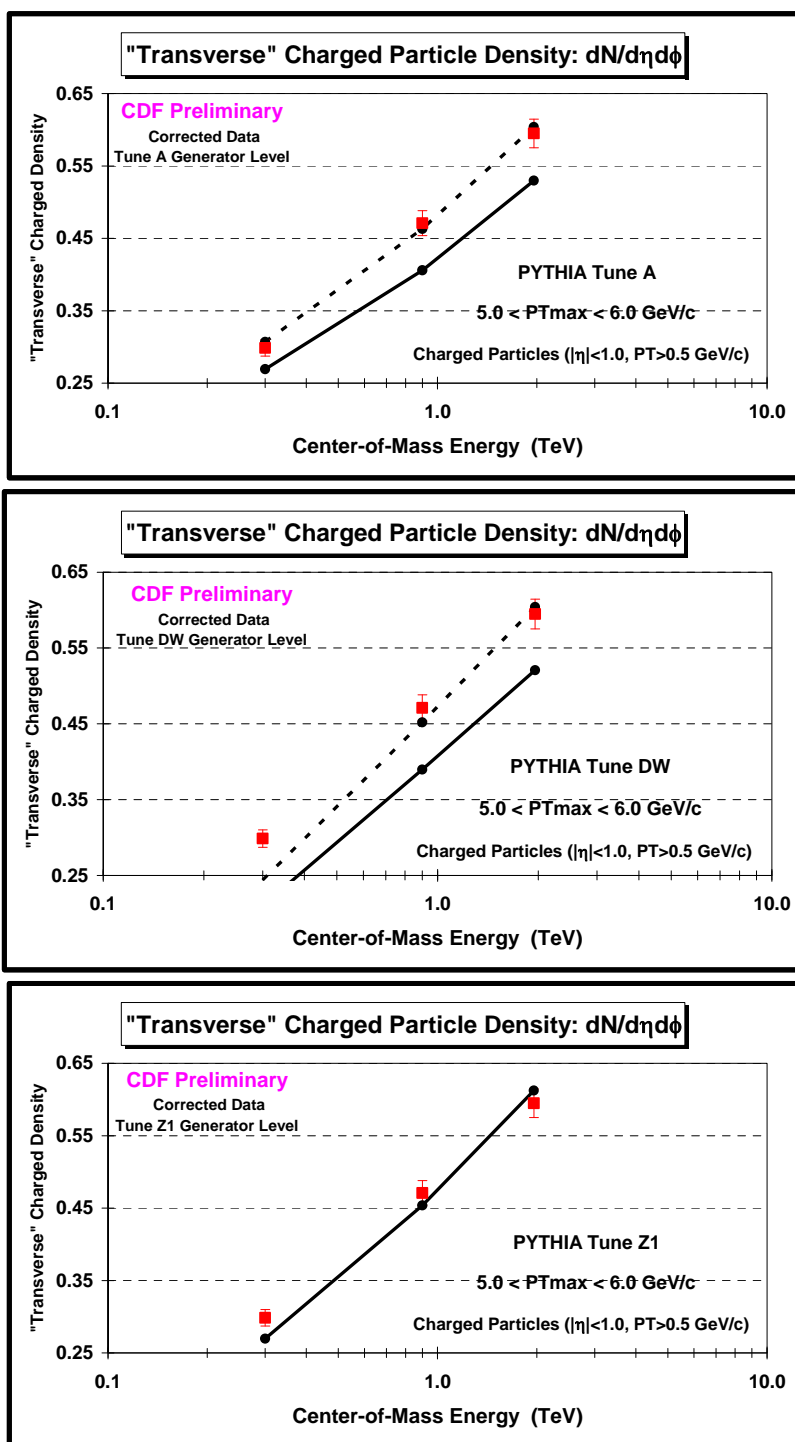
**Fig. 9.** (top) Data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . The data are corrected to the particle level with errors that include both the statistical error and the systematic uncertainty. (middle) Percentage total error for the data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (bottom) Data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , for  $5.0 < PT_{max} < 6.0$  GeV/c plotted versus the center-of-mass energy (on a log scale).



**Fig. 10.** (top) Bin-by-bin ratio of the data at 1.96 TeV and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (middle) Bin-by-bin ratio of the data at 900 GeV and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . (bottom) Bin-by-bin ratio of the data at 1.96 TeV and 900 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ .

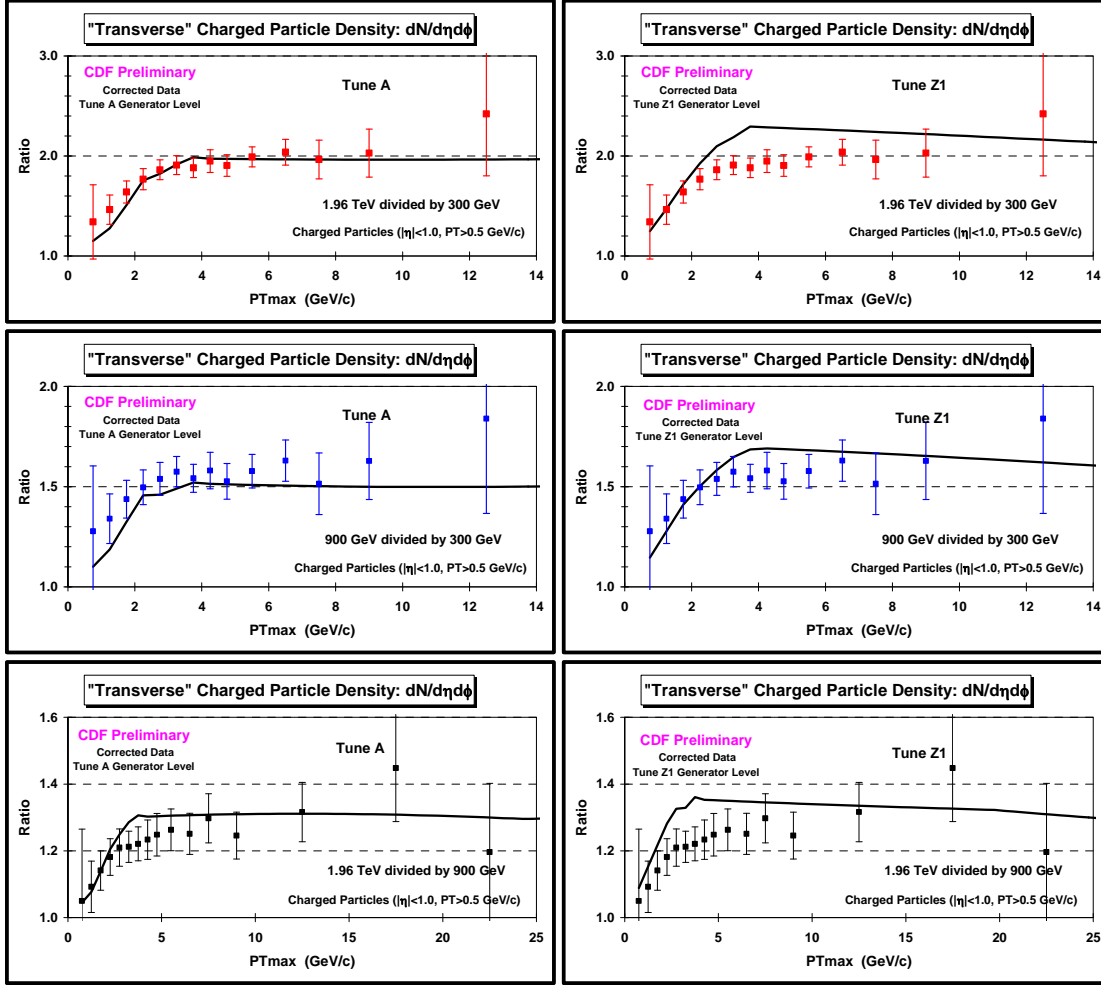


**Fig. 11.** Data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{max}$ , as a function of  $PT_{max}$ . The data are corrected to the particle level (with errors that include both the statistical error and the systematic uncertainty) and are compared with PHTYIA 6.2 Tune A (*top*), PYTHIA 6.2 Tune DW (*middle*), and PYTHIA 6.4 Tune Z1 (*bottom*) at the particle level (*i.e.* generator level).



**Fig. 12.** Data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , for  $5.0 < PT_{\text{max}} < 6.0$  GeV/c plotted versus the center-of-mass energy (on a log scale). The data are corrected to the particle level (with errors that include both the statistical error and the systematic uncertainty) and are compared with (*top*) PHTYIA 6.2 Tune A (solid curve) and Tune A scaled be a factor of 1.14 (dashed curve), (*middle*) PYTHIA 6.2 Tune DW (solid curve) and Tune DW scaled be a factor of 1.16 (dashed curve), and (*bottom*) PYTHIA 6.4 Tune Z1 (solid curve).





**Fig. 13.** (top) Bin-by-bin ratio of the data at 1.96 TeV and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$  compared with PYTHIA 6.2 Tune A (left) and with PYTHIA 6.4 Tune Z1 (right). (middle) Bin-by-bin ratio of the data at 900 GeV and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$  compared with PYTHIA 6.2 Tune A (left) and with PYTHIA 6.4 Tune Z1 (right). (bottom) Bin-by-bin ratio of the data at 1.96 TeV and 900 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$  compared with PYTHIA 6.2 Tune A (left) and with PYTHIA 6.4 Tune Z1 (right).

## IV. Results: “Transverse” Charged Particle Density

Figures 8 and 9 show the corrected data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$ . The data are corrected to the particle level with errors that include both the statistical error and the systematic uncertainty. Fig. 9 also shows the percentage total error for the data at the three energies. It also shows the data at 1.96 TeV, 900 GeV, and 300 GeV on the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , for  $5.0 < PT_{\text{max}} < 6.0$  GeV/c plotted versus the center-of-mass energy (on a log scale). Fig. 10 shows the bin-by-bin ratio of the data at 1.96 TeV and 300 GeV, the data at 900 GeV and 300 GeV, and the data at 1.96 TeV and 900 GeV for the “transverse” charged particle density as defined by the leading charged particle,  $PT_{\text{max}}$ , as a function of  $PT_{\text{max}}$ .

Figures 11, 12, and 13 compare the data on the “transverse” charged particle density with the PYTHIA 6.2 Tune A and Tune DW and the PYTHIA 6.4 Tune Z1. Tune A does a nice job on the energy dependence but is low by about 14% at each energy. Tune DW does a very poor job in describing the 300 GeV data and hence does not fit the energy dependence. Tune Z1 fits very well the LHC data [6,7] and also does a fairly good job with the CDF data presented here.

## V. Summary & Conclusions

The data presented here together with the LHC data allows for a precise study of the energy dependence of the UE. None of the QCD Monte-Carlo models fit all the data perfectly yet, however, the data presented here will result in new and improved tunes. There is much remaining to do. Soon we will update this note with the other observables in Table 1. In addition, to compare with LHC UE studies we will include all the observables for both the range  $p_T > 0.5$  GeV/c and  $|\eta| < 1.0$  and the range  $p_T > 0.5$  GeV/c and  $|\eta| < 0.8$ . This is fun!

## ACKNOWLEDGMENTS

I want to thank Mary Convery, Ray Culbertson, Craig Group, and Jonathan Lewis for their help with the datasets.

## References

- [1] *Charged Jet Evolution and the Underlying Event in Proton-Antiproton Collisions at 1.8 TeV*, The CDF Collaboration, Phys. Rev. **D65**, 092002, (2002).
- [2] *Studying the Underlying Event in Drell-Yan and High Transverse Momentum Jet Production at the Tevatron*, The CDF Collaboration, Phys. Rev. **D82**, 034001 (2010), arXiv:1003.3146.
- [3] T. Sjöstrand, Phys. Lett. **157B**, 321 (1985); M. Bengtsson, T. Sjöstrand, and M. van Zijl, Z. Phys. **C32**, 67 (1986); T. Sjöstrand and M. van Zijl, Phys. Rev. **D36**, 2019 (1987). T. Sjöstrand, P. Eden, C. Friberg, L. Lonnblad, G. Miu, S. Mrenna and E. Norrbin, Computer Physics Commun. **135**, 238 (2001).
- [4] *CDF Run 2 Monte-Carlo Tunes*, R. Field, Tevatron-for-LHC: Report of the QCD Working Group, arXiv:hep-ph/0610012, FERMILAB-Conf-06-359, October 1, 2006.
- [5] P. Skands, *The Perugia Tunes*, 2009. arXiv:0905.3418.
- [6] *Min-Bias and the Underlying Event at the LHC*, R. Field, arXiv:1110.5530, proceedings of the 51<sup>st</sup> Cracow School of Theoretical Physics: *The Soft Side of the LHC*, Zakopane, June 11 - 19, 2011, Acta Physica Polonica **B42**, 2631 (2011).
- [7] *Early LHC Underlying Event Data - Findings and Surprises*, R. Field, arXiv:1010.3558, proceedings of the Hadron Collider Physics Symposium (HCP2010), August 23-27, 2010.
- [8] For example see, *Underlying Event Measurements in pp Collisions at 0.9 and 7 TeV with the ALICE experiment at the LHC*, The ALICE Collaboration, arXiv:1112.2082v2, December 2011.
- [9] *Using MAX/MIN Transverse Regions to Study the Underlying Event in Run 2 at the Tevatron*, Alberto Cruz, Rick Field, and Craig Group, CDF/ANAL/CDF/CDFR/7703.
- [10] *CDF-QCD Data for Theorists Part 1 Leading Jet Events*, Rick Field and Craig Group, CDF/ANAL/CDF/CDFR/9087.
- [11] *Using Drell-Yan to Probe the Underlying Event in Run 2 at CDF*, Deepak Kar and Rick Field, CDF/ANAL/CDF/CDFR/9242.