



Modeling of Lightcurves from Reconnection-powered Very High-energy Flares from M87*

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Abstract

The black hole at the center of M87 is observed to flare regularly in the very high-energy (VHE) band, with photon energies $\gtrsim 100$ GeV. The rapid variability, which can be as short as 2 days in the VHE lightcurve, constrains some of the flares to originate close to the black hole. Magnetic reconnection is a promising candidate for explaining the flares, where the VHE emission comes from background soft photons that inverse Compton scatter off of high-energy electron–positron pairs in the reconnecting current sheet. In this work, we ray trace photons from a current sheet near the black hole event horizon during a flux eruption in a magnetically arrested state in a general relativistic magnetohydrodynamics simulation. We incorporate beaming of the Compton up-scattered photons, based on results from radiative kinetic simulations of relativistic reconnection. We then construct VHE lightcurves that account for the dynamics of the current sheet and lensing from general-relativistic effects. We find that most of the flux originates in the inner 5 gravitational radii, and beaming is essential to explain the observed flux from the strongest VHE flares. The ray traced lightcurves show features resulting from the changing volume of the reconnecting current sheet on timescales that can be consistent with observations. Furthermore, we find that the amount of beaming depends strongly on two effects: (i) the current sheet inclination with respect to the observer and (ii) the anisotropy in the direction of motion of the accelerated particles.

Unified Astronomy Thesaurus concepts: [Black holes \(162\)](#); [Gamma-ray observatories \(632\)](#); [High energy astrophysics \(739\)](#); [Magnetohydrodynamics \(1964\)](#)

1. Introduction

The elliptical galaxy Messier 87 (M87) is located at a distance of 16.8 Mpc from the Milky Way (J. P. Blakeslee et al. 2009). It hosts a supermassive black hole called M87*, with a mass of $6.5 \times 10^9 M_\odot$ (K. Gebhardt et al. 2011; Event Horizon Telescope Collaboration et al. 2019a), where M_\odot is a solar mass. M87* and a few other low-luminosity active galactic nuclei (AGNs) such as Sagittarius A* (Sgr A*), the supermassive black hole in our own Milky Way, show rapid variability, ranging from X-rays to, in the case of M87*, a few TeV γ -rays (A. Eckart et al. 2006; A. Abramowski et al. 2012). Multiple very high-energy (VHE) flares have been observed from M87* in 2005, 2008, 2010, and 2018 (F. Aharonian et al. 2006; J. Albert et al. 2008; V. A. Acciari et al. 2010; A. Abramowski et al. 2012; J. C. Algaba et al. 2024). These flares last for timescales as short as $\lesssim 2$ days, which is of the order of a few event horizon light-crossing times (about 8 hr for M87*, assuming that it is rapidly spinning), and have fractional variability (i.e., the ratio of the fluxes during the flare and quiescent state, respectively) $\Delta F/F \sim 2\text{--}40$ (J. C. Algaba et al. 2024). The observed flux from the VHE flares is between $\sim 10^{-13}\text{--}10^{-11}$ photons $\text{cm}^{-2} \text{s}^{-1}$ for energies in the range

350 GeV–10 TeV. The implied isotropic-equivalent luminosities are in the range of $10^{40}\text{--}10^{42}$ erg s^{-1} (F. Aharonian et al. 2006; J. C. Algaba et al. 2024)⁹. Furthermore, the correlated radio and X-ray emission from the M87* core in, e.g., the 2008 flare, points toward the near-horizon region as the origin of the flares, as opposed to a knot in the jet (V. A. Acciari et al. 2010; A. Abramowski et al. 2012), where the latter was X-ray quiet (A. Abramowski et al. 2012). This is further supported by X-ray flares being detected from the M87* core (Y.-L. Cheng et al. 2023). Several mechanisms have been proposed to power the VHE flares, including curvature radiation from pairs in charge-starved regions inside the jet, gaps (A. Levinson 2000; A. Levinson & B. Cerutti 2018; A. Y. Chen et al. 2018; B. Crinquand et al. 2020), or inverse-Compton (IC) up-scattering on magnetic reconnection-accelerated pairs from near the event horizon (B. Ripperda et al. 2020; A. Chashkina et al. 2021; B. Ripperda et al. 2022; H. Hakobyan et al. 2023b). Both mechanisms, which can potentially explain the energetics and variability of flares, require significant re-arrangement in the large-scale geometry and properties of the accretion flow during the flare. In the reconnection scenario, the formation of extended thin current sheets is required. In contrast, in the gap scenario, significant changes in the properties of the soft-photon field are needed (S. Kisaka et al. 2022).

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⁹ The estimate for the luminosity can vary by a factor of ~ 2 , depending on the cutoff energy at which the spectrum becomes steeper.

The plasma in the accretion disk around the black hole is nearly collisionless, with a luminosity of $L \sim 10^{-3} L_{\text{Edd}}$ in units of the Eddington luminosity. The Eddington luminosity is $L_{\text{Edd}} \equiv 4\pi G M m_p c / \sigma_T$, where G , M , m_p , c and σ_T are the gravitational constant, mass of black hole, mass of a proton, speed of light, and the Thompson cross section, respectively. The magnetic field strength of the black hole is estimated to be around 100 G. This is inferred by matching the submillimeter radio flux observed by the Event Horizon Telescope (EHT) to synchrotron radiation from an accretion disk with a plasma $\beta = 1$ and a $1/r$ dependence of the magnetic field (Event Horizon Telescope Collaboration et al. 2019b, 2024), where r is the distance from the black hole. Furthermore, this magnetic field strength agrees well with a jet powered by the Blandford–Znajek (BZ; R. D. Blandford & R. L. Znajek 1977) mechanism (B. Ripperda et al. 2022). Moreover, the radio and multi-wavelength observations by EHT (Event Horizon Telescope Collaboration et al. 2019a, 2019b, 2021; EHT Multi-Wavelength Science Working Group et al. 2021; Event Horizon Telescope Collaboration et al. 2023, 2024; J. C. Algaba et al. 2024), in particular of strong linear polarization, point toward the disk around the black hole being in a magnetically arrested state (G. S. Bisnovatyi-Kogan & A. A. Ruzmaikin 1974; R. Narayan et al. 2003; I. V. Igumenshchev 2008). In this scenario, the pressure of strong ordered magnetic fields eventually becomes comparable to the ram pressure of the accreting plasma. General-relativistic magnetohydrodynamics (GRMHD) simulations show that such disks exhibit quasiperiodic magnetic flux eruptions (A. Tchekhovskoy et al. 2011), forming a large-scale current sheet where the magnetic fields at the base of the jet then reconnect (B. Ripperda et al. 2022). The current sheet formed during these reconnection episodes is capable of accelerating electron–positron pairs to very high Lorentz factors due to the high magnetization expected in the base of the jet (H. Hakobyan et al. 2023b).

One of the challenges of the reconnection scenario is that the duration of the reconnection event, as observed in the GRMHD simulations (B. Ripperda et al. 2022; A. Galishnikova et al. 2023), is a factor of 10–100 longer than the duration of the observed high-energy flares (A. Abramowski et al. 2012). The reconnection duration can be shorter in global kinetic simulations of accreting collisionless plasma, which have a reconnection rate that is faster by a factor of few (A. Bransgrove et al. 2021; A. Galishnikova et al. 2023). While such kinetic simulations can account for particle acceleration in the presence of synchrotron and inverse-Compton cooling in a first-principles manner (see, e.g., G. R. Werner et al. 2019; L. Sironi & A. M. Beloborodov 2020; A. Chernoglazov et al. 2023; H. Hakobyan et al. 2023b, for local simulations), they cannot yet capture the long-term steady state of magnetically arrested flows and, thus, the three-dimensional global motion of the current sheet due to the computational expenses. Both of these effects can be very important in characterizing the lightcurves of high-energy flares. These effects can cause the radiation to get beamed in specific directions and potentially yield faster variability. For example, observations show that relativistic beaming near the black hole may be important in determining the rise and decay timescales of the flares (S. D. von Fellenberg et al. 2023).

In this work, we construct flare lightcurves by determining photon trajectories in global three-dimensional GRMHD data of a rapidly spinning black hole, capturing the near-horizon

reconnection layer (B. Ripperda et al. 2022). We use a novel Monte Carlo (MC) scheme based on existing ray tracing codes GRMONTY and κ MONTY (J. C. Dolence et al. 2009; J. Davelaar et al. 2023). We construct lightcurves relevant to the GeV–TeV band by tracing photons initialized close to the current sheet, with beaming prescriptions motivated by three-dimensional radiative particle-in-cell (PIC) simulations (A. Chernoglazov et al. 2023). These simulations self-consistently include strong synchrotron cooling in a highly magnetized pair plasma, in the regime appropriate for low-luminosity AGNs, such as Sgr A* and M87*. Our method of constructing the VHE lightcurves by introducing PIC-motivated beaming prescriptions into the GRMHD background can be applied to other relativistic astrophysical systems with large-scale current sheets (e.g., pulsar magnetospheres, B. Cerutti et al. 2016; neutron star collapse or merger remnants, S. Selvi et al. 2024; E. R. Most et al. 2024; or black hole coronae, M. T. P. Liska et al. 2022).

This paper is structured as follows. Section 2 contains the theory of VHE emission from the current sheet. Section 3 describes the current sheet identification and ray tracing methods we adopted to construct the lightcurves. Section 4 contains the key results from our analysis. Section 5 discusses our results in context of VHE observations from low-luminosity AGNs, and conclusions are presented in Section 6.

2. Reconnection-powered Flares

In the following section, we summarize the physics involved in the reconnection-powered VHE flare model. The process involves the following steps: (1) accretion of plasma onto the black hole, accompanied by increasing magnetic flux on the event horizon, and subsequent triggering of the large-scale magnetic reconnection; (2) acceleration of electron–positron pairs produced in the jet to large Lorentz factors inside the current sheet; and, (3) IC scattering of soft background photons by the energetic pairs to power VHE flares. We begin by listing the key physical parameters for M87* flares.

2.1. Physical Parameters

The inferred mass of the black hole and the local magnetic field strength from EHT are $M_{\text{BH}} = 6.5 \times 10^9 M_{\odot}$ and $B \sim 100$ G near the event horizon, respectively (in agreement with $B \sim 30$ G at 7 gravitational radii ($r_g = \frac{GM}{c^2}$) for a field linearly decaying with radius, as inferred by Event Horizon Telescope Collaboration et al. 2019a). The jet power is of the order of $L_{\text{jet}} \sim 10^{42} - 10^{44}$ erg s⁻¹ (M. A. Prieto et al. 2016). Assuming that the jet is launched by the BZ mechanism, the theoretical jet power estimated using the inferred 100 G magnetic fields matches the observed jet power. The 300 GHz (~ 1 meV photons) flux near the M87* horizon is ~ 1 Jy, from which one can estimate the soft-photon background energy density at 1 meV to be $U_{\text{soft}} \approx 0.01$ erg cm⁻³ (A. E. Broderick & A. Tchekhovskoy 2015; EHT Multi-Wavelength Science Working Group et al. 2021). This energy density is representative of the quiescent state of the accretion disk, and it can be a factor of a few lower during the magnetic flux eruption event when the accretion disk, the main source of the meV emission, is ejected from near the black hole (B. Ripperda et al. 2022; H. Jia et al. 2023). The accretion rate onto the black hole is $\sim 10^{-3} M_{\odot} \text{ yr}^{-1}$ (Event Horizon Telescope Collaboration et al. 2019a).

Two other important parameters affect the microphysics of particle acceleration: the radiation reaction-limited Lorentz factor and the plasma magnetization. The radiation reaction-limited Lorentz factor, γ_{rad} , is the Lorentz factor at which the radiative losses balance out the acceleration of pairs due to the electric field in the current sheet. Since the magnetic energy density vastly exceeds the energy density of the soft radiation field, $B^2/8\pi \gg U_{\text{soft}}$, radiation reaction is dominated by synchrotron losses. Additionally, the plasma magnetization, $\sigma_c = b^2/(4\pi\rho_{e\pm}c^2)$ is the ratio of twice the magnetic energy density in a frame comoving with the fluid ($b^2/4\pi = b^\mu b_\mu/4\pi$) to the rest mass energy of the pairs, where $\rho_{e\pm}$ is the mass density of pairs in the current sheet. Here, b^μ is the magnetic field 4-vector; refer to S. C. Noble et al. (2006) for its definition and relation to B (note that we use Greek indices to represent 4-vectors and Latin indices to represent 3-vectors throughout the paper). The characteristic energy gain of particles accelerated during reconnection is set by this magnetization, $\gamma \sim \sigma_c$. Note that most of the pair density in this scenario is produced locally, by collisions of high-energy synchrotron photons produced by reconnection-accelerated particles. We follow the estimates of H. Hakobyan et al. (2023b) for γ_{rad} and σ_c to be 4×10^6 and $\sim 10^7$, respectively. The value of σ_c depends on the plasma number density, which is assumed to be set by the pairs produced from the synchrotron radiation from the energized particles in the current sheet (H. Hakobyan et al. 2023b).

Three-dimensional PIC simulations that account for radiative losses have shown how particle acceleration happens in both weak, $\gamma_{\text{rad}}/\sigma_c > 1$, and strong, $\gamma_{\text{rad}}/\sigma_c < 1$, cooling regimes (A. Chernoglazov et al. 2023). In the weak cooling regime, the highest-energy particles, $\gamma \sim \gamma_{\text{rad}}$ are accelerated by the reconnection-driven electric field while bouncing between the two converging upstreams (H. Zhang et al. 2021). In the strong cooling regime, however, the most energetic particles, $\gamma \sim \sigma_c$, preferentially move along the upstream magnetic field, escaping the synchrotron burnoff limit. When $\gamma_{\text{rad}} \sim \sigma_c$, the cooling is moderate, and the pairs' velocities at highest energies are almost isotropic. Following H. Hakobyan et al. (2023b), we generally expect $\gamma_{\text{rad}}/\sigma_c \lesssim 1$ for M87*, putting it into the moderate to strong cooling regime. In this paper, we construct lightcurves for both isotropic and along-the-upstream field beaming prescriptions to model both the moderate and strong cooling regimes. Additionally, an isotropic beaming prescription can be applicable if the magnetic field upstream of the current sheet is much less ordered on microscopic scales than what GRMHD simulations performed at macroscopic scales show. This situation can be realized if vigorous turbulence is excited during the current sheet formation.

2.2. VHE Flares: Energy Source

In order to produce TeV energy photons, electrons and positrons need to have energies of at least 1 TeV or Lorentz factors greater than $\gamma = E/(m_e c^2) \gtrsim 2 \times 10^6$, where E is their energy. The energy to accelerate the pairs during reconnection comes from the dissipation of the magnetic field energy, which is the free energy in the system. Accelerated pairs of ~ 1 TeV energies are cooled extremely quickly, $t_{\text{cool}} \sim 1\text{TeV}/P_{\text{sync}} \approx 0.1$ s, where $P_{\text{sync}} = (4/3)\sigma_T c \gamma^2 (B^2/8\pi)$ is the synchrotron power. The almost instantaneous nature of the synchrotron cooling allows us to not track accelerated particles through GRMHD scales but

instead postulate instantaneous ‘‘subgrid’’ emissivity (see Section 3.3).

The synchrotron radiation has a characteristic luminosity of $L_{\text{rec}} \approx 0.1 L_{\text{jet}}$, where L_{jet} is the M87* jet luminosity (H. Hakobyan et al. 2023b). The factor of 0.1 comes from the amount of magnetic flux that is reconnected, which energizes the pairs that then radiate away their energy via synchrotron emission. The VHE photons are produced by the up-scattering of the soft photons from the disk by particles accelerated in the current sheet. The ratio of synchrotron to inverse-Compton luminosity can be approximated as $L_{\text{rec}}/L_{\text{IC}} \sim (\langle \gamma^2 B_\perp^2 \rangle / 8\pi) / (\langle \gamma^2 \rangle U_{\text{soft}}) \sim (\gamma_{\text{rad}}/\sigma)^2 U_B / U_{\text{soft}} \sim 4 \times 10^2 (\gamma_{\text{rad}}/\sigma)_{0.1}^2 B_{100}^2 U_{\text{soft},0.01}$, where the subscripts represent the values by which the quantities are normalized. Here, $\langle \dots \rangle$ denotes an average over the particle distribution function, γ is the Lorentz factor of the particles, B_\perp is the effective perpendicular field that the particles experience, and U_B is the magnetic field energy density. Simulations of H. Hakobyan et al. (2023b) show that $\langle \gamma^2 B_\perp^2 \rangle / 8\pi \sim \gamma_{\text{rad}}^2 U_B$ and $\langle \gamma^2 \rangle \sim \sigma^2$. For a maximally spinning black hole, the jet luminosity can be estimated as $L_{\text{jet}} \sim c B_g^2 r_g^2 \sim 2 \times 10^{44} B_{100}^2 \text{erg s}^{-1}$. This yields a total IC luminosity of $\sim 6 \times 10^{40} \text{erg s}^{-1}$ (H. Hakobyan et al. 2023b). The isotropic-equivalent luminosity inferred from the strongest VHE flares of M87 can reach $10^{42} \text{erg s}^{-1}$ (A. Abramowski et al. 2012; J. C. Algaba et al. 2024), which requires some amount of beaming to be present in the reconnection-powered flare model.

Beaming effects will also be present in the synchrotron radiation emitted by energetic particles in the current sheet. In particular, simulations by A. Chernoglazov et al. (2023) show that the highest-energy particles in the reconnecting current sheet produce radiation in excess of the synchrotron burnoff limit, ~ 16 MeV, which is strongly beamed along the upstream magnetic field, i.e., in the same direction as the VHE IC emission that we consider in this paper.

2.3. VHE Flares: Angular Distribution of Power

While previous works have shown that IC emission by reconnection-accelerated particles is a plausible mechanism to get the correct VHE flux luminosity, they do not study the variability and angular distribution of the IC emission, which are important to understand the lightcurves and compare the model to observed data. Potential sources of variability and beaming include (a) local anisotropy in the distribution function of accelerated pairs (that is, accelerated particles preferentially moving along or perpendicular to the background magnetic field), (b) the changing volume and geometry of the current sheet, (c) the variation in the local IC emissivity throughout the current sheet, and (d) general-relativistic effects in the vicinity of the black hole.¹⁰

As discussed previously, VHE flares can potentially be powered by the IC emission of pairs accelerated in the current sheet. In the strong cooling regime, $\gamma_{\text{rad}}/\sigma_c < 1$, pairs that manage to exceed the synchrotron burnoff limit preferentially move along the upstream magnetic field, \hat{B}_{up} (A. Chernoglazov et al. 2023). Thus, the IC radiation powered by the energetic pairs can be highly beamed along the direction of the local upstream magnetic field. The global magnetic field direction

¹⁰ In addition to these effects, the faster flux decay rate in collisionless plasma, compared to the GRMHD approximation, may also contribute to faster variability due to the flux eruptions (A. Bransgrove et al. 2021; A. Galishnikova et al. 2023).

plays an important role in determining how much of the flare luminosity is received by a distant observer. The local beaming effects can be washed out if the magnetic field around the current sheet is randomly oriented. On the other hand, an ordered magnetic field will preserve some of the local beaming and make the overall IC flux anisotropic. The coherent near-horizon submillimeter polarization from M87* points toward ordered magnetic fields around the black hole, where this effect can be important (Event Horizon Telescope Collaboration et al. 2021). Moreover, the current sheet during the flux eruption itself is dynamic. The changing volume and geometry of the current sheet can, in principle, affect the flare luminosity. In particular, if the volume of the current sheet changes over time then it will also manifest as a variability in the lightcurve.

Finally, since in the reconnection scenario, the magnetic field energy at the jet base powers the flares, the local VHE emissivity scales as the local magnetic field energy density. While the exact radial profile of the magnetic field is unknown for M87*, the field strength should generally scale as $\sim 1/r$ for a preferentially toroidal field (B. Ripperda et al. 2020), and as $\sim 1/r^2$ for a poloidal field. Consequently, the VHE emissivity is expected to drop off with distance from the black hole, following the fluid-frame magnetic energy density, $b^\mu b_\mu \sim B^2 \Gamma^{-2}$, where Γ is the Lorentz factor of the plasma. Following these points, below we describe our procedure of constructing the VHE lightcurves from the GRMHD simulation using a subgrid model for the beaming of highest-energy particles, based on results of radiative PIC simulations (A. Chernoglazov et al. 2023; H. Hakobyan et al. 2023b).

3. Methods

We analyze a high-resolution GRMHD simulation of a spinning black hole (where the spin parameter $a = 0.9375$) with a geometrically thick accretion disk that reaches a magnetically arrested state, presented in B. Ripperda et al. (2022). The simulation is performed with the Graphics Processing Unit (GPU)-accelerated code HAMR (M. T. P. Liska et al. 2022). The simulation is performed in spherical Kerr–Schild (KS) coordinates (t, r, θ, ϕ) and has an (effective) resolution of $N_r \times N_\theta \times N_\phi = 5376 \times 2304 \times 2304$, and a radial domain of $r \in \{1.2, 2000\} r_g$. It is initialized with a large-scale poloidal (in the r – θ plane) magnetic field to ensure that the simulation reaches the MAD state. The strength of the initial magnetic field is normalized such that $2P_{\max}/(b^\mu b_\mu)_{\max} = 100$, where P is the gas pressure, and the “ $_{\max}$ ” values are the maximum values in the entire grid. The adiabatic index of the gas is $\hat{\gamma} = 13/9$, which lies between the adiabatic indices of relativistic and nonrelativistic gases, respectively. MHD simulations require lower bounds (floors) on fluid variables such as pressure and density. In the simulation, the density floor of the plasma in the jet is set such that the maximum value of the plasma magnetization in the domain is $\sigma_{c,\max} = 25$, using the magnetic field strength in the frame comoving with the fluid. The simulation is performed with a sufficiently high resolution so that the current sheet near the event horizon shows plasmoid formation, which indicates that the reconnection occurs in the fast asymptotic MHD regime. This observation is confirmed by the measured reconnection rate of $\sim 0.01c$ (B. Ripperda et al. 2022), where the reconnection rate is defined as the inflow velocity into the sheet, normalized by the Alfvén speed, $v_A = \sqrt{\sigma_c/(\sigma_c + 1)}c \sim c$ for $\sigma_c = 25$ in the jet.

The GRMHD outputs have a cadence of $5t_g$ where $t_g = r_g/c = GM/c^3$ in the KS coordinate time. The simulation shows three large-scale magnetic flux eruption events. Our analysis is done in the time interval 9050–9750 t_g , which brackets one of the eruption events or the flaring state. A large-scale current sheet forms during the flaring state, and the magnetic flux at the horizon rapidly drops (B. Ripperda et al. 2022).

The current sheet is confined within approximately $10r_g$, so we truncate our analysis domain within that radius. Similarly, the current sheet does not move more than 20° from the equator, so we also limit the analysis domain to $\theta \in (45^\circ, 135^\circ)$.

To construct the VHE lightcurves, we perform the following steps: (1) identify the current sheet—the location where pairs would be accelerated to large Lorentz factors, and the high-energy emission would be produced; (2) initialize the wavevectors of the photons in accordance with the local magnetic field geometry, and the different prescriptions for the amount of beaming of accelerated particles; and (3) ray trace photons to a large distance from the black hole following the method based on the ray tracing codes GRMONTY and Kmonty (J. C. Dolence et al. 2009; J. Davelaar et al. 2023). We now describe each of the steps in more detail.

3.1. Current Sheet Identification

The current sheet in the simulation is identified using a combination of the cold magnetization parameter, σ_c , and dimensionless fluid temperature, $T = P/\rho$ (i.e., in units of ion rest mass energy), thresholds. We expect a small magnetization parameter, σ_c , in the current sheet as well as a high sheet temperature proportional to the upstream magnetization (i.e., the temperature depends on σ_c in the upstream, and not on the small σ_c inside the current sheet), $T \propto \sigma_{c,\max} > 1$ (B. Ripperda et al. 2022). The value of σ_c is small inside the current sheet because $b^\mu b_\mu$ drops in the reconnection region and the density peaks in the current sheet compared to the magnetized upstream.¹¹ The fluid is heated up during reconnection as the (upstream) magnetic energy is converted into the thermal and kinetic energies of the plasma. The current sheet is more clearly captured using these two thresholds than directly computing the current density, which does not always uniquely identify reconnecting current sheets (see also Figure 8 of B. Ripperda et al. 2020).

Figure 1 shows the values of T and σ_c for three snapshots at different times in the simulation. The panels from left to right are taken before, during, and after a large-scale magnetic flux eruption, respectively. One can see the formation of a thin current sheet in the zoomed-in insets in the middle panels ($t = 9500r_g/c$), evident from the increase in fluid temperature and decrease in σ_c . The white dashed lines in the two figures are the locations where the fluid-frame magnetic field energy profile, b^2 , is computed and plotted in Figure 2. It is also clear that a combination of both parameters is necessary to pick out the current sheet. For instance, the middle panel of Figure 1 contains high-temperature zones that are clearly not located in the current sheet (e.g., hot fluid advected out of the reconnection zones). Similarly, the bulk of the disk has a low value of the magnetization, σ_c , and is not a part of the current sheet.

¹¹ Reconnection in the current sheet present during the magnetic flux eruption occurs in the zero-guide field regime; see B. Ripperda et al. (2022).

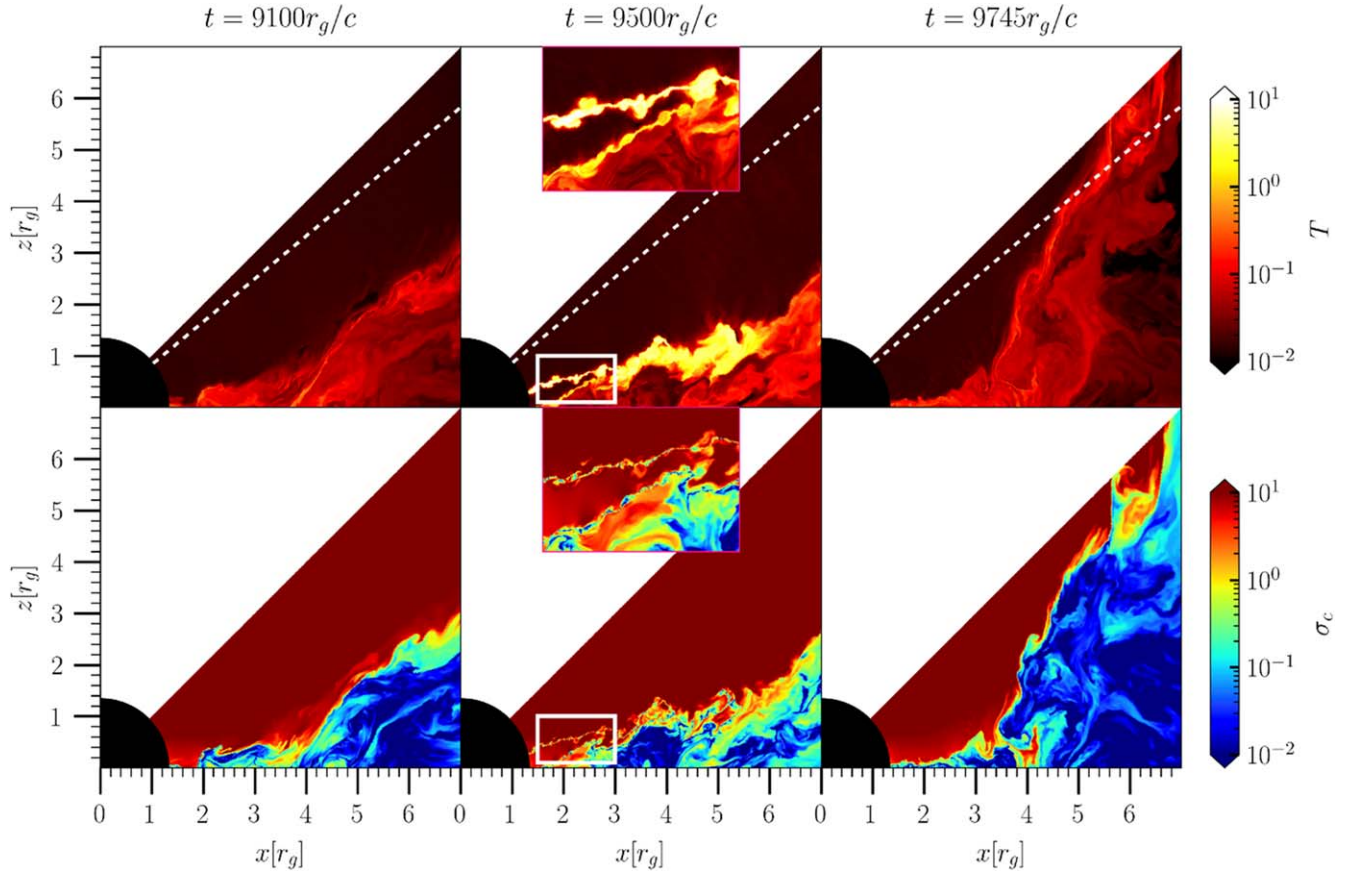


Figure 1. Poloidal slices of the dimensionless temperature, T , and magnetization, σ_c , taken during three snapshots in the simulation. The snapshots are taken before, during, and after a large-scale magnetic flux eruption, respectively. Fluid heats up to temperatures $T \sim \sigma_{\text{jet}}$ in the middle panel ($t = 9500 r_g/c$) as a result of magnetic reconnection. Likewise, σ_c is nearly zero where reconnection takes place because of vanishing magnetic fields and accumulation of matter in the current sheet. We use $T > 1$ and $\sigma_c < 0.01$ as our thresholds for current sheet identification. The insets in the middle panels show a zoomed-in view of the current sheet that undergoes reconnection. The plasma in the sheet is characterized by low magnetization, σ , and high temperature, T . We calculate the upstream magnetic field strength $b^2 = b^\mu b_\mu$ profiles in Figure 2, along the white dashed lines.

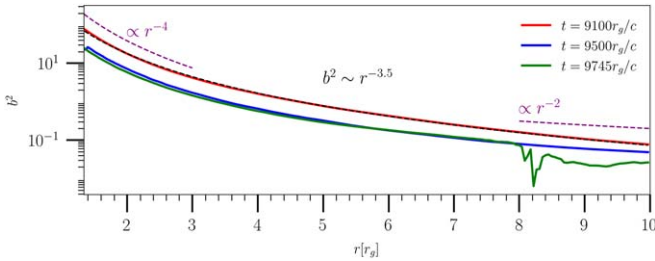


Figure 2. The radial profile of $b^2 = b^\mu b_\mu$, representing the fluid-frame magnetic field energy, taken along the white dashed lines in Figure 1. $b^2 \sim r^{-3.5}$ drops during the magnetic flux eruption, once the magnetic field lines start reconnecting. A similar drop in b^2 during a magnetic flux eruption is seen in Figure 14 of B. Ripperda et al. (2020). The approximate $r^{-3.5}$ scaling can be explained by the field being mainly radial, $b^2 \propto r^{-4}$, near the black hole, and increasingly toroidal, $b^2 \propto r^{-2}$, at larger distances.

There is no radial dependence of σ_c in the jet very close to the black hole, $\lesssim 10 r_g$, and $\sigma_{c,\text{jet}} \approx \sigma_{\text{max}}$ because of the imposed density floor. As a result, the plasma temperature in the reconnection layer is independent of the distance from the black hole as well, which motivates us to use a constant temperature threshold for the reconnection zone. The temperature in the disk-jet boundary during the magnetic flux eruption is $\gtrsim 1$, much higher than the temperature everywhere else in the disk. We take this threshold as a good indicator of localizing the plasma that passed through the reconnection

zone. Likewise, we adopt a constant σ_c threshold of $\sigma_c < 0.01$ to locate the regions of weak magnetic field, that is, in the current sheet. We test various choices of T and σ_c thresholds in Appendix A, and find that the above thresholds adequately capture the location of the current sheet. To summarize, we use constant thresholds of $T > 1$ and $\sigma_c < 0.01$ to identify the current sheet.

3.2. Photon Beaming and Upstream Identification

After identifying the current sheet, we need to find the direction of the upstream magnetic field, \hat{B}_{up} , along which the accelerated particles can be beamed. The VHE photons are beamed along the direction of motion of the high-energy particles that do the scattering. As a result, in a strongly cooled regime, $\gamma_{\text{rad}} \lesssim \sigma_c$, the IC photons are primarily emitted along the upstream magnetic field around the current sheet. The distribution of photon emission directions becomes more isotropic as σ_c approaches γ_{rad} (A. Chernoglazov et al. 2023). The results of PIC simulations directly apply to reconnection in a flat spacetime with no bulk flows in the upstream. However, there are global flows in the jet in the vicinity of the black hole, determined by the $\mathbf{E} \times \mathbf{B}$ drift resulting from the rotation of field lines, as well as possible bulk flows along the field lines. Because of these effects, we first identify the locally flat fluid rest frame in the upstream of the current sheet. We initialize the photon momenta in this frame according to the above

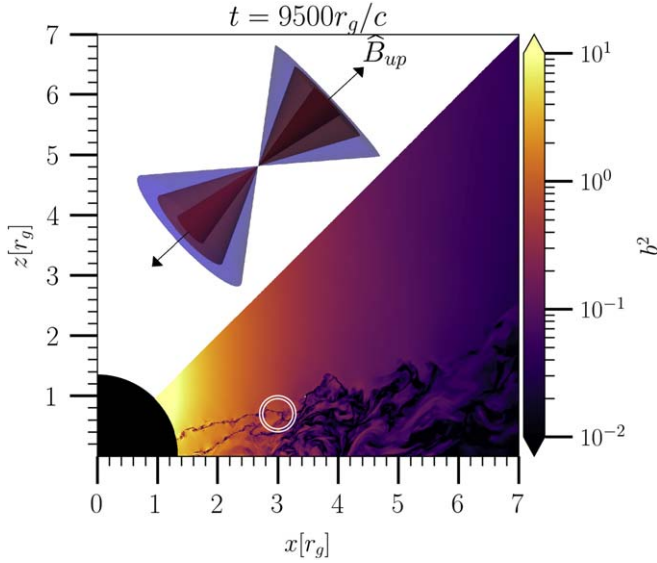


Figure 3. Polar slice of b^2 taken during the magnetic flux eruption. The current sheet is the region where b^2 falls as the magnetic field lines reconnect. In order to identify the upstream magnetic field, we take a small volume in the form of a thick spherical shell around each cell in the current sheet. The white shell plotted in the figure is representative of the volume we scan around every cell and pick the largest magnetic field scaled out by its radial dependence. Once the corresponding upstream magnetic field is identified for every point in the current sheet, the photons’ (superphotons’) wavevectors are sampled by using a Gaussian distribution centered around the upstream field. The cones in the top left represent different amounts of beaming, with smaller opening angles corresponding to stronger beaming.

prescriptions from PIC simulations, and boost back into the lab frame for ray tracing.¹²

The structure of turbulent three-dimensional magnetic field inside the identified current sheet does not allow to easily construct a vector along the upstream field. Instead, we consider a spherical shell around each cell in the previously identified current sheet. We then define the upstream field to be the magnetic field vector with the largest b^2 in the scanned volume, which is also above a threshold, $b^2 \geq 80r^{-3.5}$. The numerical pre-factor is chosen such that the selected values correspond to the true upstream field, and not local field compressions inside the current sheet. The radial dependence is chosen such that we are not biased in picking the magnetic field directions corresponding to cells closer to the black hole, where the field strength is highest. Note that b^2 in the upstream of the sheet approximately scales as $\sim r^{-3.5}$ (see the b^2 profile along the jet in Figure 2).

We find that the maximum value of b^2 computed within spherical shells saturates at a distance of $\approx 0.2r_g$ away from the current sheet. Therefore, we select the inner and outer radii of the scanned shells to be 0.25 and $0.3r_g$, respectively. A polar slice of the b^2 values is shown in Figure 3, taken during the flux eruption at $t = 9500 r_g/c$. We overplot a shell with inner and outer radii of 0.25 and $0.3r_g$, respectively (white rings), representative of the volume scanned to find the upstream field. We find that the choice of the outer radius of the spherical shell

¹² We verified that plasma in the upstream of the current sheet mainly moves according to the $\mathbf{E} \times \mathbf{B}$ drift, as expected for relativistic reconnection. Thus, in flat spacetime, our prescription in the case of strong synchrotron cooling is equivalent to boosting photons along $\hat{\mathbf{v}} = \hat{\mathbf{v}}_{\parallel} \mathbf{B}/B + \mathbf{E} \times \mathbf{B}/B^2$, where $\hat{\mathbf{v}}_{\parallel}$ is chosen such that $|\hat{\mathbf{v}}| = 1$. Such a prescription was used to model γ -ray lightcurves from pulsars (X.-N. Bai & A. Spitkovsky 2010) and is consistent with global PIC simulations of pulsar magnetospheres (B. Cerutti et al. 2016)

does not change the overall distribution of the identified upstream field as long as it is between 0.3 and $0.4r_g$. This convergence test is discussed in more detail in Appendix (B).

Once the direction of the upstream magnetic field is identified, b^{μ} is transformed to the fluid frame. This is done by constructing a tetrad basis, \hat{e}_{μ} , where the time axis, \hat{e}_t , is along the 4-velocity of the fluid in the upstream, and \hat{e}_x points along the identified upstream magnetic field. The \hat{e}_y and \hat{e}_z are constructed using the Gram–Schmidt orthonormalization, so the tetrad axes are orthonormal in metric $g_{\alpha\beta}$. The fluid-frame magnetic field is then obtained by projecting the lab frame magnetic field vector along the tetrad.

3.3. Photon Initialization and Geodesic Integration

We trace photons originating from the current sheet using an MC-based method following GRMONTY and Kmonty (J. C. Dolence et al. 2009; J. Davelaar et al. 2023). We initialize and ray trace packets of photons called “superphotons.” With the current sheet and the upstream magnetic field identified, we initialize $N_i(x_i^{\mu})$ superphotons with weights w_i and wavevectors $k_i^{\mu} = (k_i^0, \mathbf{k}_i)$ in every cell i inside the current sheet. Here, x_i^{μ} is the 4-position of cell i in KS coordinates. The superphotons are initialized in a frame that is comoving with the upstream fluid and is centered on the current sheet cell i . The x -axis is defined to be along the upstream magnetic field, $\hat{B}_{up,i}$, identified previously.

We use a random number generator (RNG) to sample $|k_{\perp,i}| = \sqrt{k_{y,i}^2 + k_{z,i}^2}$, the norm of the perpendicular component of the superphoton’s wavevector with respect to the upstream magnetic field, using a Gaussian probability distribution. The distribution has a mean of 0 and a standard deviation of $\Delta\chi$, which sets the opening angle of the photon beams coming out of the sheet. $\Delta\chi$ quantifies the amount of beaming: when it is small, \mathbf{k}_i is mostly along the local $\hat{B}_{up,i}$, as is expected in the case of strong cooling (accelerated pairs move along $\hat{B}_{up,i}$ and radiate in the same direction). Conversely, when $\Delta\chi$ is large, there is no correlation between \mathbf{k}_i and $\hat{B}_{up,i}$, representative of the case of weak cooling. Superphotons have $k^{\mu}k_{\mu} = 0$ and $|k| = 1$, implying $|k_{\perp}| \leq 1$. However, the RNG can occasionally sample unphysical wavevectors, with $|k_{\perp}| > 1$ ($\Rightarrow k^{\mu}k_{\mu} \neq 0$). When this happens, we resample $|k_{\perp}|$. To construct the full wavevector, we use uniform distributions to sample an azimuthal angle $\phi_i \in [0, 2\pi]$ and the sign of the $k_{\parallel,i}$, the wavevector component parallel to $\hat{B}_{up,i}$, $\text{sign}(k_{\parallel,i}) \in \{-1, 1\}$. The latter is done to ensure that superphotons can propagate both parallel and antiparallel to the upstream field. Finally, k^{μ} is initialized such that $k^0 > 0$ and $k^{\mu}k_{\mu} = 0$. We do not consider the energy distribution of the photons, since all of the \vec{k}_i ’s have a unit norm. This is because the IC emission mechanism is treated using a prescription for beaming in post-processing, and no information about the distribution function of emitting pairs that produce the IC radiation is specified, or required. The different cones correspond to different values of $\Delta\chi$, namely $\Delta\chi \in \{1^{\circ}, 10^{\circ}, 45^{\circ}\}$, going from strongly to weakly beamed photons along the magnetic field, respectively. We also include a model with no subgrid beaming, where k_x , k_y , and k_z are all sampled from a uniform distribution.

The number of photons emitted in each cell, N_i , is proportional to the volume element as well as the local IC emissivity, i.e., $N_i \propto j(x_i^{\mu}) d^3 x_i^{\mu} \sqrt{|1 - g(x_i^{\mu})|}$, where $g(x_i^{\mu})$ is the

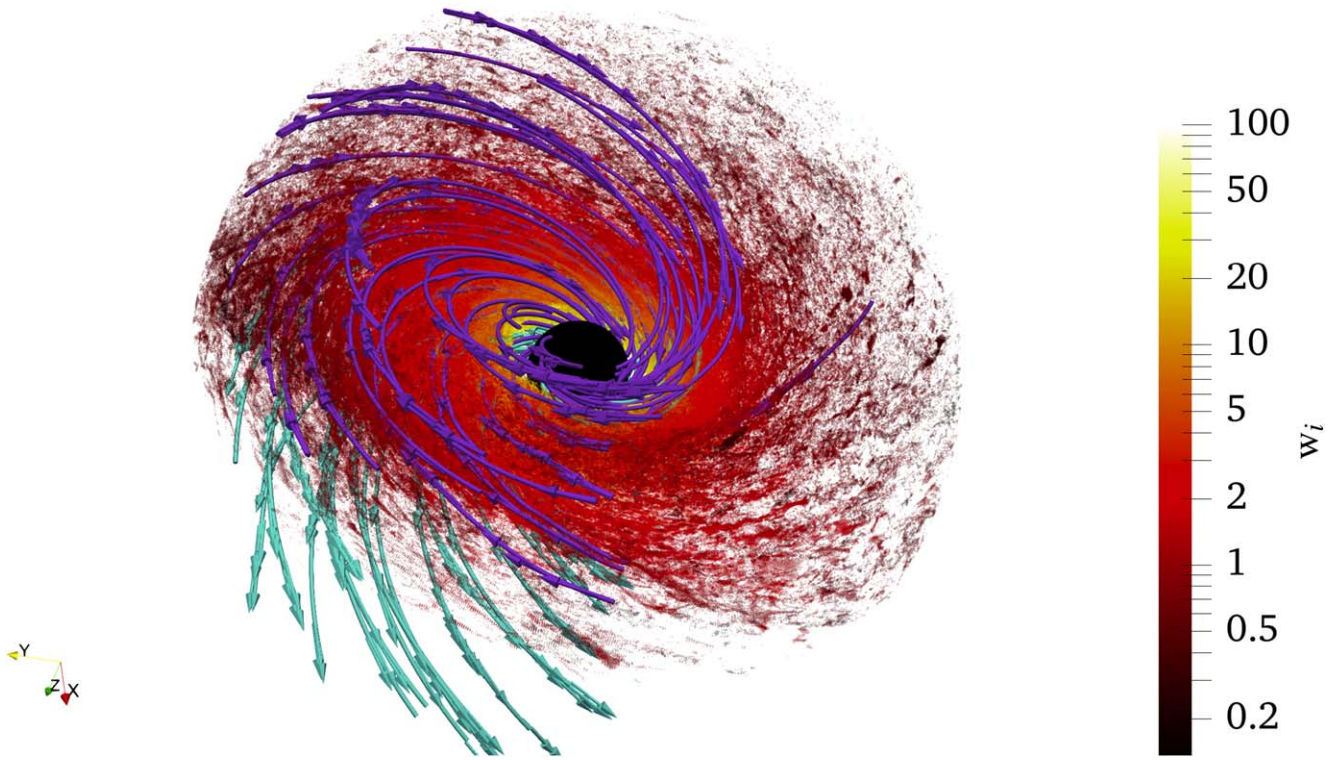


Figure 4. The location of the VHE emission production, combined over all of the simulation snapshots analyzed in this paper. The color represents the superphoton weights w_i . The emission region lies in the equatorial plane of the simulation at smaller distances but gets progressively misaligned from it farther from the black hole. The magnetic field lines are overplotted as purple (pointing radially inward) and cyan (pointing outward) lines, taken from one of the simulation snapshots during the magnetic flux eruption.

determinant of the metric. The coordinates used in the simulation have constant $d^3 x_i^{\mu}$ and therefore $N_i \propto j(x_i^{\mu}) \sqrt{|-g(x_i^{\mu})|}$.

Further, $j(x_i^{\mu})$ is the IC emissivity of the VHE photons, which we set to be proportional to $b^2(x_i^{\mu})$. This choice is motivated by the fact that the average energy density of the accelerated leptons in the current sheet is proportional to the upstream magnetic field energy density. In practice, N_i can have very large values for different cells in the grid, making ray tracing more computationally expensive. To circumvent this issue, we define a quantity $c_i = \sqrt{|-g(x_i^{\mu})|} / \min(\sqrt{|-g(x^{\mu})|})_{\forall i}$ and set $N_i = c_i^{1/2}$ and $w_i = b^2(x_i^{\mu}) c_i^{1/2}$. This ensures that at least one photon is produced in every cell that belongs to the current sheet. The superphoton weight, w_i , depends on the upstream magnetic field strength and the determinant of the metric at the position of emission. We obtain identical results using $N_i = 1 \times c_i^{1/2}$, $5 \times c_i^{1/2}$ and $10 \times c_i^{1/2}$ (i.e., ray tracing at least 1, 5, and 10 superphotons per current sheet cell, respectively), as shown in the Appendix C.

The N_i wavevectors from every current sheet cell are then transformed back to the lab frame. We use the standard Runge–Kutta 4 (RK4) integrator to integrate the geodesics in modified (i.e., logarithmic in radius) KS coordinates. We use adaptive time stepping described in J. C. Dolence et al. (2009) with an initial step size of $10^{-4} t_g$. A small step size is required because most of the emission originates very close to the black hole, where general-relativistic effects are important and smaller steps are required to maintain accuracy. The convergence of our ray tracing scheme is discussed in Appendix C. Numerical integration ends when the geodesics cross the event horizon or attain a coordinate radius $r > 10^4 r_g$. The lightcurves are constructed from binning the superphotons that reach the outer

boundary, weighted by w_i . We analyze the total data of 140 simulation outputs, spanning $t \in (9000t_g, 9750t_g)$, which capture a magnetic flux eruption that occurs during the interval $(9300t_g, 9600t_g)$.

4. Results

4.1. Emission Zone

The identified locations of VHE photon production, combined over all of the analyzed simulation snapshots, are shown in Figure 4. The magnetic field streamlines are overplotted, which are taken from a snapshot during the state of magnetic eruption at $t = 9500 r_g/c$. The purple and cyan field lines represent field lines that point radially inward and outward, respectively.¹³ The colors represent the superphoton weights $w_i \propto b^2(x_i^{\mu}) \sqrt{|-g(x_i^{\mu})|}$.¹⁴ The superphotons originating close to the black hole have larger weight because of the radial dependence of b^2 (see Figure 2). Reconnection and, thus, photon emission, happens along the jet base. Unlike in two-

¹³ In the rest frame of the upstream plasma moving nearly radially, the wavevectors of superphotons are aligned along the upstream magnetic field in the strongly beamed models.

¹⁴ This prescription assumes that the amount of the dissipated power scales with the magnetic field energy density that is calculated in the upstream fluid frame. This assumption is not universally valid, as reconnection at high σ leads to significant changes to fluid velocity inside the current sheet where reconnection occurs. For example, it has been shown that the velocity component along the upstream field does not lead to a change in the reconnection rate as long as it is significantly lower than the Alfvén speed (H. Hakobyan et al. 2023a). In the case considered here, however, the Lorentz factors in the upstream are mild, $\Gamma \lesssim \text{few}$, so this correction is not significant. We defer issues related to the dependence of reconnection rate on upstream fluid velocity to a future dedicated study.

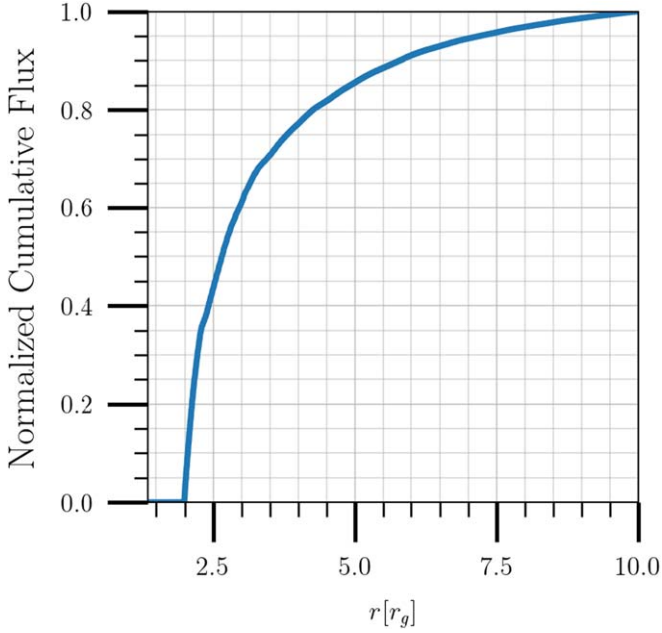


Figure 5. The normalized cumulative distribution of the total luminosity from the current sheet as a function of the radial coordinate measured in r_g . The radial dependence of luminosity is identical for all of the beaming models. About 80% of the total flux originates within $5r_g$ from the black hole. This is because of the strong radial dependence of the VHE emissivity ($\propto b^2 \sim r^{-3.5}$).

dimensional simulations (B. Ripperda et al. 2020), the current sheet is no longer located dominantly in the equatorial plane for flux eruptions in three dimensions. For strongly beamed models that are particularly sensitive to the geometry of the magnetic field in the emission region, this fact highlights the importance of capturing fully three-dimensional dynamics of the eruption for VHE lightcurve modeling.

We plot the cumulative VHE flux as a function of distance from the black hole in Figure 5. The cumulative flux at position \mathbf{r} is obtained by computing the normalized sum of weights of all of the superphotons at $10^4 r_g$, which have an initial KS coordinate of $r \leq \mathbf{r}$. We find that there are almost no superphotons in the inner $\approx 2r_g$ that contribute to the flux that makes it to the outer boundary. About 80% of the flux comes from $r \lesssim 5r_g$ of the black hole. This fact stems from the larger magnetic field energy density available to power the IC emission. The cumulative VHE flux as a function of radius is very similar for all of the beaming models (i.e., cumulative fluxes constructed for different values of $\Delta\chi$), and here we only show the isotropic case.

Figure 6 shows the two-dimensional histograms of the initial and final (computed at $10^4 r_g$) θ coordinates of the superphotons, for the very strong, $\Delta\chi = 1^\circ$, and no-beaming models, respectively. Their initial and final values are given by θ_i and θ_f , respectively. Most of the calculated flux originates from the vicinity of the equatorial plane, $\theta_i \in \{80^\circ, 120^\circ\}$. In the case of very strong beaming, the outgoing photons stay in the equatorial plane, and therefore the spread in θ_f is small. On the other hand, in the model with uniform beaming, the flux is more uniformly distributed over all latitudes. There is also a tight correlation between the initial and final arrival latitudes of superphotons such that $\theta_f = 180^\circ - \theta_i$. This is clearly evident in the strong beaming model, where most of the superphotons are initialized close to the equatorial plane and along the magnetic field lines. Therefore, they move in the r -direction toward or

away from the black hole. This trend is also visible in the no-beaming model, although to a lesser extent. This correlation can be understood as follows. In addition to the energy, norm of the wavevector, and angular momentum, the geodesics also have an additional conserved quantity called the Carter’s constant. In Boyer–Lindquist (BL) coordinates $(t_{\text{BL}}, r_{\text{BL}}, \theta_{\text{BL}}, \phi_{\text{BL}})$, this quantity can be written as $\mathcal{C} = k_{\theta_{\text{BL}}}^2 + \cos^2 \theta_{\text{BL}} (k_{t_{\text{BL}}}^2 a^2 - k_{\phi_{\text{BL}}}^2 / \sin^2 \theta_{\text{BL}})$, where \mathcal{C} is the Carter’s constant, and $|k_{t_{\text{BL}}}|$ and $k_{\phi_{\text{BL}}}$ are the conserved energy and angular momentum, respectively. The initial wavevectors of the superphotons have a negligible $k^{\theta_{\text{BL}}} = k^\theta$ component because they follow the upstream magnetic field distribution, which is radially dominated (note that $k^{\theta_{\text{BL}}}$ is equivalent in both the coordinate systems because $\theta_{\text{BL}} = \theta$); see Appendix B. Then $k_\theta \propto k^\theta$ vanishes in BL coordinates, and therefore the superphotons initially are at a turning point in θ . The outer boundary is also a turning point in θ since the superphotons propagate radially outward at infinity and $k^\theta \rightarrow 0$. The second turning point is located at $\theta_f = \pi - \theta_i$, which can be verified by substitution into the equation for the Carter’s constant.

4.2. Flare Lightcurves

We plot the lightcurves for models with different beaming in Figure 7. The superphoton wavevectors are integrated out to $10^4 r_g$, and their coordinates are stored. The lightcurves are constructed by creating a histogram of the superphotons’ time coordinates once they reach the outer boundary, weighted by the photon weight, w_i . Each color represents the total flux at different inclination ranges with respect to the spin-axis of the black hole in the simulation. The inclination ranges are chosen such that an equal amount of solid angle is contained in every curve.

Further, it is necessary for the superphoton flux requires to be normalized so that the generated lightcurves can be compared to the VHE observations. To do so, we equate the median flux over all solid angles to a fiducial luminosity of $10^{40} \text{ erg s}^{-1}$; see Section 2.2. Then, the flux at time t going into a solid angle $\Delta\Omega = 2\pi \int_{\theta_i}^{\theta_f} \sin \theta d\theta$ is given by:

$$F(t, \theta = \theta_i) = 10^{40} \cdot \frac{\int_{\theta_i}^{\theta_f} \Delta N(t, \theta_i) \sin \theta d\theta}{\overline{\Delta N} \Delta\Omega d_{\text{M87}}^2} \text{ erg s}^{-1} \text{ cm}^{-2}, \quad (1)$$

where $\Delta N(t, \theta)$ are the number of (weighted) superphotons received between times t and $t + t_g$, and angles θ_i and θ_f , and $L_0 = 10^{40} \text{ erg s}^{-1}$ is the fiducial IC luminosity (Section 2.2). Here, θ_f is computed so that an equal amount of solid angle, taken to be $\Delta\Omega \equiv 2\pi \times (\pi/180)$, is contained for all lightcurves, so that $\theta_f = \arccos(\cos \theta_i - \frac{\Delta\Omega}{2\pi})$. In all of the constructed lightcurves, θ_f differs from θ_i by $< 1^\circ$. The normalization constant is given by $\overline{\Delta N}$, which is the median value of $\int_0^\pi \Delta N(t, \theta_i) \sin \theta d\theta$ in time.

Since our ray tracing does not keep track of the superphoton energies, we need to relate the superphoton count to the VHE flux.¹⁵ Therefore, we adopt a photon power-law index of 2.2

¹⁵ Note that we construct the lightcurves using an optical depth of $\tau = 0$; i.e., there is no attenuation in the signal during propagation. Estimates for the VHE photon optical depth for M87* vary in the literature. $\tau \lesssim 1$ is expected for energies less than a TeV (A. E. Broderick & A. Tchekhovskoy 2015; H. E. S. S. Collaboration et al. 2024)

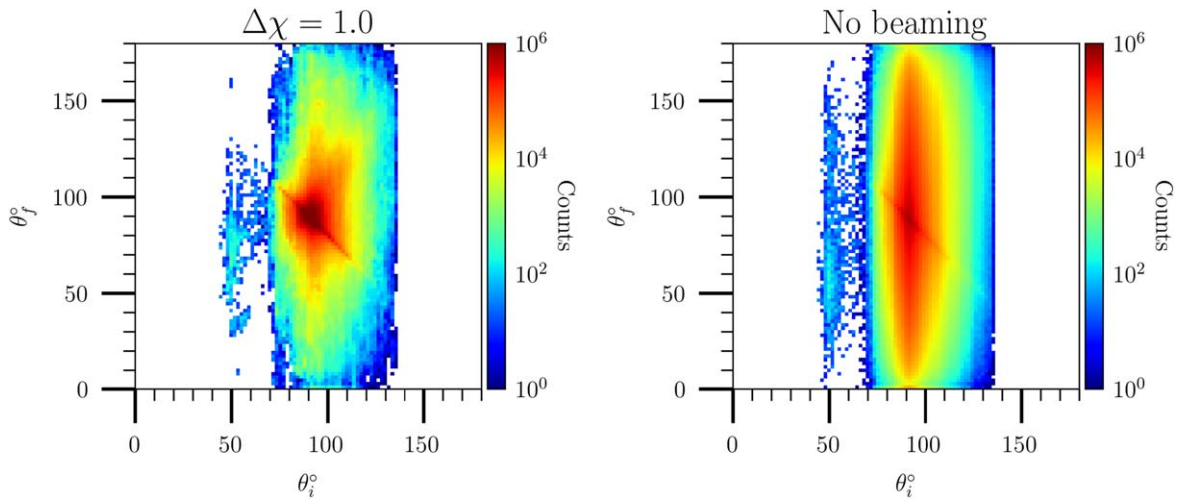


Figure 6. Two-dimensional histograms for the initial and final θ coordinates of superphotons in the lightcurves computed for strong and no-beaming cases. Most of the initial emission is concentrated in a small range of angles, namely $80^\circ < \theta_i < 120^\circ$ for both cases. In the strong beaming case ($\Delta\chi = 1^\circ$), the superphotons stay close to the equatorial plane even at large distances. On the contrary, superphotons propagate more uniformly when there is no strong beaming assumed, which is as expected. This is because in the vicinity of the black hole, the upstream magnetic field points in the $\hat{e}_r - \hat{e}_\phi$ direction, where \hat{e}_r and \hat{e}_ϕ are unit vectors along the r - and ϕ -directions, respectively. Therefore, the emission is beamed along the same direction. See the text in Section 4.1 for the tight correlation between θ_i and θ_f .

starting from 350 GeV (E. Aliu et al. 2012). The average superphoton energy for such a distribution is about $2\text{TeV} \approx 3.2$ erg. The flux is then converted into counts $\text{s}^{-1} \text{cm}^{-2}$ using this value. The fiducial luminosity, L_0 , further scales with the assumed strength of the magnetic field near the black hole, properties of the soft-photon field, and distribution of accelerated particles (see Section 2.2).

The maximum flux from the beamed lightcurves gets as large as $\sim 10^{-11}$ photons $\text{cm}^{-2} \text{s}^{-1}$, which is suppressed by a factor of 10 for the no-beaming lightcurves. The VHE flux is largest at the equator ($\theta_i = 90^\circ$) for all of the lightcurves, which results from two different beaming effects at play. Most of the VHE flux comes from the inner part of the current sheet, which lies roughly in the equatorial plane of the simulation. In this region, the upstream magnetic field lines, and therefore the wavevectors of superphotons in the strong beaming model, are oriented in the radial direction. Because of this fact, most of the flux ends up along the equatorial plane. A high-altitude observer will only see the emission if the upstream magnetic field points out of the equatorial plane. Consequently, the emission drops by 2 orders of magnitude at higher latitudes in the lightcurves with $\Delta\chi = 1^\circ$ and 10° . The lightcurves at these high latitudes also show a faster timescale variation of less than a day, although the overall flux is highly suppressed.

Additionally, there is an increased flux along the equatorial plane, even in the case of no beaming. This is a result of the mildly relativistic bulk plasma motion in the radial direction close to the black hole. Figure 8 shows the radial 3-velocity and the Lorentz factor of the plasma during the magnetic flux eruption. The increased equatorial flux by a factor of a few can be explained by the bulk motion of the plasma. The beaming in this case is proportional to $\Gamma_{\text{upstream}}^2 \lesssim 4$ and not as strong of an effect as the assumed beaming.

In order to compare the lightcurves with the observations, we plot the strong beaming case, $\Delta\chi = 1^\circ$, and isotropic models, on a linear scale in Figure 9. Assuming a threshold of $10^{-11} \text{cm}^{-2} \text{s}^{-1}$ (e.g., the threshold flux for the very strong VHE flares in A. Abramowski et al. 2012), the flux from the lightcurve with strong beaming would not appear as a very energetic VHE flare at higher latitudes. However, when there is

no beaming, the flux at high latitudes is only suppressed by a moderate factor of $\sim 2-3$.

While the entire flux eruption, indicating the period in which a flare could be powered in the simulation, lasts for $\sim 400r_g/c$ (120 days), there is a much faster variability present in all of the lightcurves, on timescales of $\sim 20r_g/c$ (15 days). This variability closely resembles the changing 4-volume of the current sheet over time, which traces the total amount of the dissipated power. It is important to check how the volume of the identified sheet changes when it is identified using different (T, σ_c) thresholds. We plot the normalized 4-volumes of the current sheet identified using different (T, σ_c) thresholds in Figure 10 as a function of time.¹⁶ It is computed as $V_{\text{sheet}} = \sum_i \sqrt{-g_i}$, where V_{sheet} is the Four-dimensional volume, and the summation is done over all of the cells in the sheet (note that the measure $\Delta^4 x^\mu$ is constant for each cell and is not included in the 4-volume calculation). The volume is normalized by its maximum value during the flux eruption. We conclude that our results are not very sensitive to the choice of T and σ_c : for any threshold, the volume changes on a $\sim 20r_g/c$ timescale, which gets imprinted in the lightcurve.

From the current sheet identification, we find that there is always a small amount of persistent magnetic reconnection near the event horizon before the onset of the flux eruption. We take this as a measure of the quiescent flux in our lightcurves. Taking the sudden increase in the flux at $t = 9350r_g/c$ to be the start of the flare (which is consistent with the rapid increase in the 4-volume of the current sheet at $t = 9300r_g/c$), Figure 9 shows a factor of 5–10 increase in flux during the flare in the model without strong beaming.

5. Discussion

5.1. Key Results

We constructed VHE lightcurves of M87* by post-processing a GRMHD simulation of an accretion disk in a

¹⁶ Note that we use the 4-volume instead of the 3-volume to also account for the change in flux from gravitational time dilation.

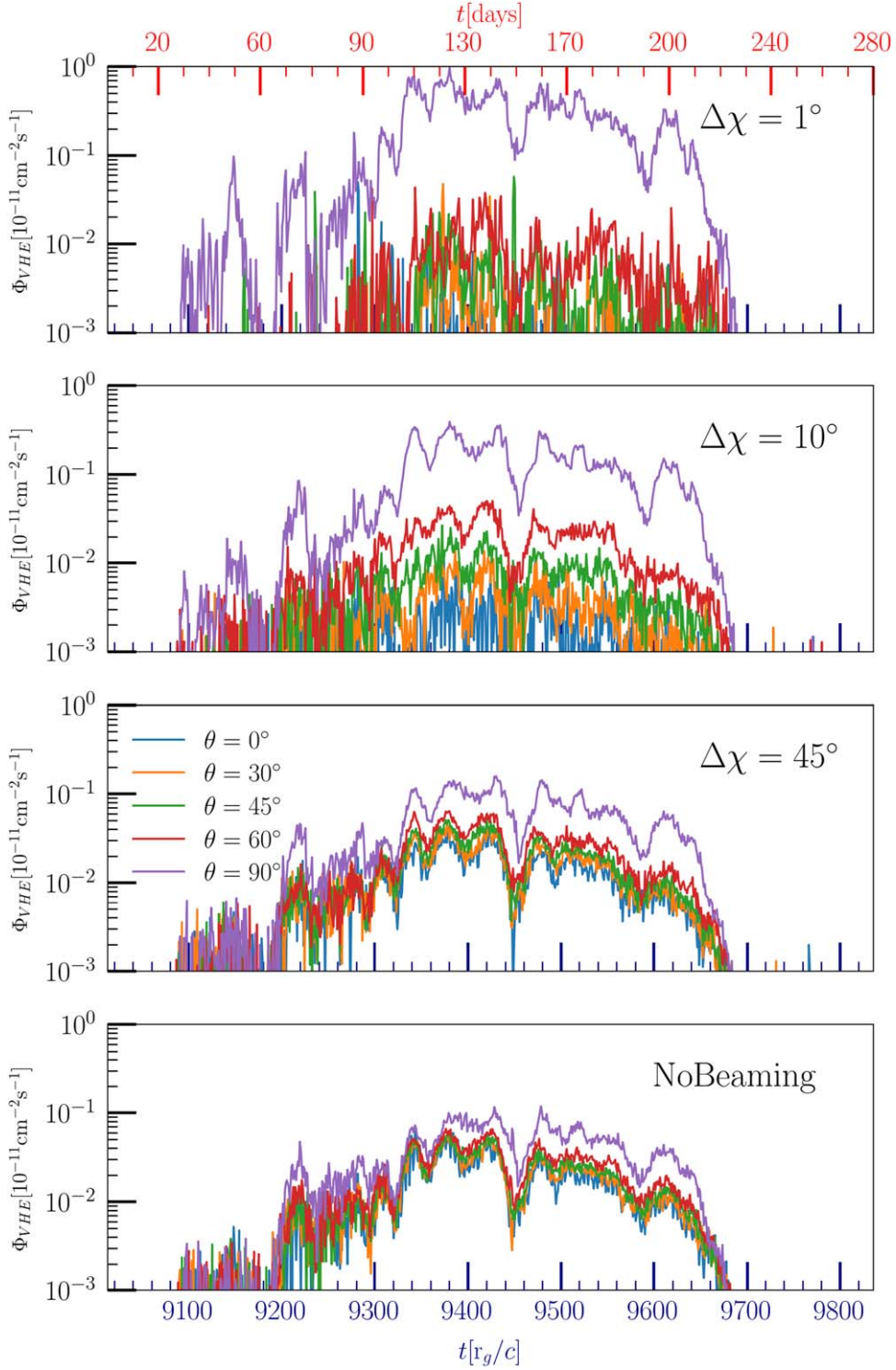


Figure 7. Lightcurves for different photon beaming models obtained from binning the Kerr–Schild (KS) coordinate times of the superphotons at $10^4 r_g$. $\Delta\chi$ is a measure of the beaming strength, with a smaller $\Delta\chi$ corresponding to superphotons aligned to the upstream magnetic field. The colors in each plot represent solid angles at different inclinations over which the flux is received. In the extreme beaming case $\Delta\chi = 1^\circ$, most of the received emission arrives in the equatorial plane of the simulation. There is approximately a factor of 100 suppression in the luminosity at higher latitudes. This fraction changes once $\Delta\chi$ gets larger, that is, there is less beaming. In the other extreme case where there is no beaming, there is only a factor of a few difference in received flux near the equator and at higher latitudes. The superphoton count is first normalized by re-scaling all of the lightcurves by the median flux in the no-beaming model. This flux is then equated to the corresponding flux arising from a flare with luminosity of $\sim 10^{40} \text{ erg s}^{-1}$ at a distance of 16 Mpc. The photon count is obtained by dividing the flux by a characteristic photon energy of 2 TeV to compare with VHE observations in A. Abramowski et al. (2012).

magnetically arrested state. Based on prescriptions from self-consistent kinetic simulations of a strongly cooled reconnecting pair plasma, we initialized and ray traced photons from a

reconnecting current sheet. We showed that the lightcurves depend on both the global dynamics and the microphysical prescriptions for the particle acceleration.

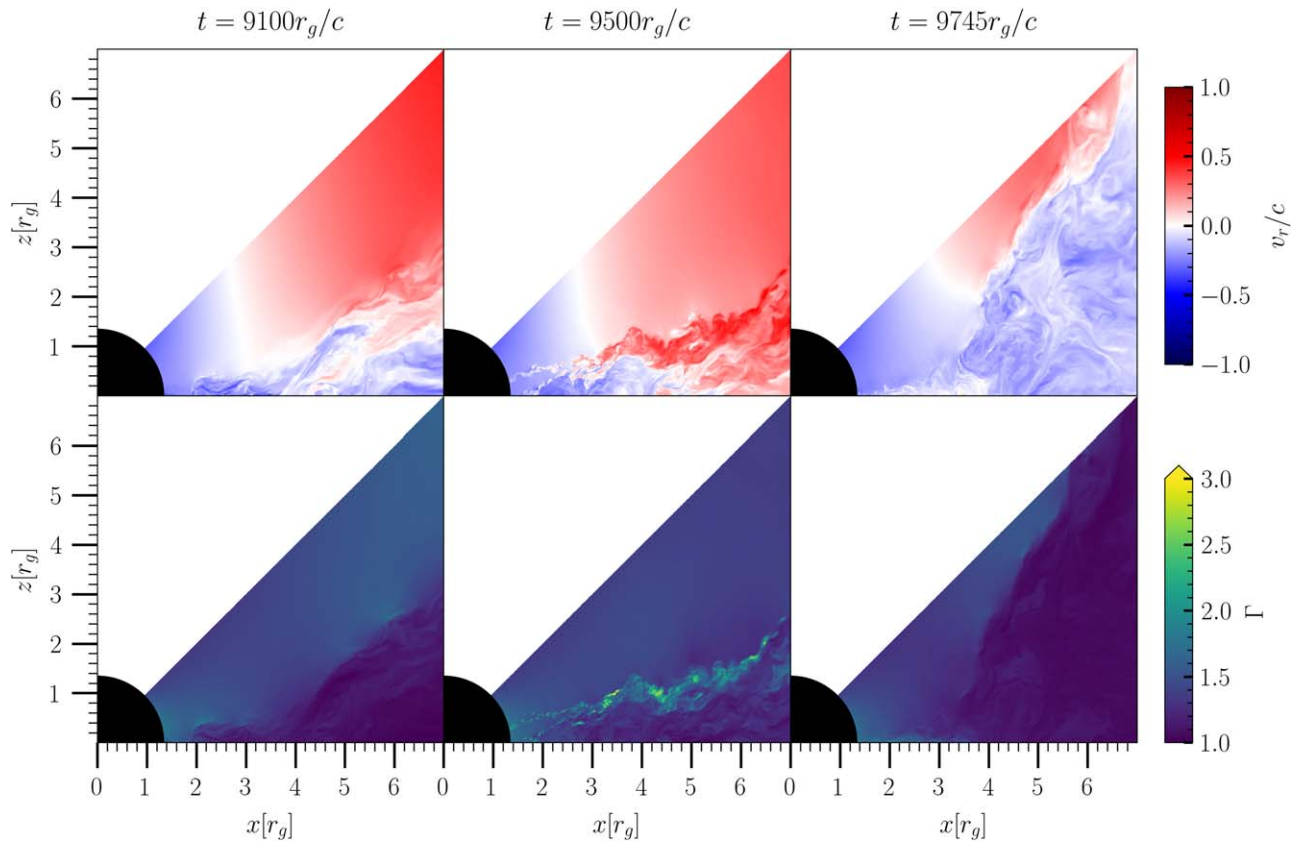


Figure 8. The radial velocity and the Lorentz factor of plasma near the current sheet. Relativistic beaming from the bulk motion of the plasma is another effect that can beam the IC flux in the equatorial plane. The Lorentz factor of plasma near the equatorial plane is $\Gamma \lesssim 2$, which moves radially outward during the flux eruption. As a result, there is an equatorial beaming in the lightcurve that is $\propto \Gamma^2 \lesssim 4$, even if no beaming is assumed.

The lightcurves generically show a long-term variability during which the flux rises by over a factor of 10. This timescale is as long as the duration of the magnetic flux eruption in the simulation, which is about $400r_g/c$, or about 130 days for M87*. The variability is modulated by faster “subflares” that last for $\sim 40r_g/c$, or a little over 10 days. The fractional flux changes by a factor of 2–5 in the subflares, which occur about 10 times during the flux eruption. The duration of the subflares correlates with the timescale of the changing volume of the current sheet, which is set by the dynamics of the current sheet.

Beaming and variations in the current sheet extent can boost the observed flux in the lightcurves of strongly beamed models, $\Delta\chi = 1^\circ$, compared to the no-beaming lightcurves. This can account for the observed flux of $\sim 10^{-11}$ photons $\text{cm}^{-2} \text{s}^{-1}$ in the most energetic flares, even if the median flare luminosity is of the order $\sim 10^{40}$ erg s^{-1} . The necessity of beaming in the reconnection model motivates conducting detailed investigations of the relative orientation of the current sheet and the black hole magnetic spin-axis in different accretion models.

Note that the GRMHD simulation shows multiple smaller-scale flux eruptions, resulting in short-lived and shorter current sheets, which we have not ray traced here. We focus on the largest flux eruptions, producing the flares with the longest time-duration.

5.2. Comparison with Observations

For all of our models, most of the flux in the lightcurves originates from the inner $5r_g$, where the current sheet

dominantly lies in the equatorial plane. Consequently, the flux in the lightcurves of strongly beamed models is highly concentrated in the equatorial plane because the upstream magnetic fields are ordered in the toroidal direction. For a nearly jet-aligned observing angle expected in M87*, we conclude that our simulations are not providing enough variability in the current sheet orientation to explain the observed flares in the strong beaming model, which corresponds to the very strong cooling. However, the subflares observed in models with moderate degree of beaming can be potentially reconciled with the data. The VHE flares from M87* show flux variations that are as short as 2 days. The subflares can get close to these short timescales and have $\Delta F/F \sim 2-5$, similar to the fractional flux variations of the observed flares.

If we consider the observed M87* VHE flares to represent the subflares within a longer flaring episode, we predict that the submillimeter and VHE lightcurves should vary on different timescales. The ejection of the accretion disk during the flux eruption can produce a characteristic submillimeter dimming of the 230 GHz flux on the same timescale as the flux eruption (H. Jia et al. 2023). While the baseline VHE flux should increase during this longer timescale, it can still vary much more quickly because of the shorter duration of the subflares, which is tracing the evolution of the current sheet during the flare. Long-term multiwavelength monitoring of M87* can provide more insight into the relation of the submillimeter and VHE emission properties during flux eruptions.

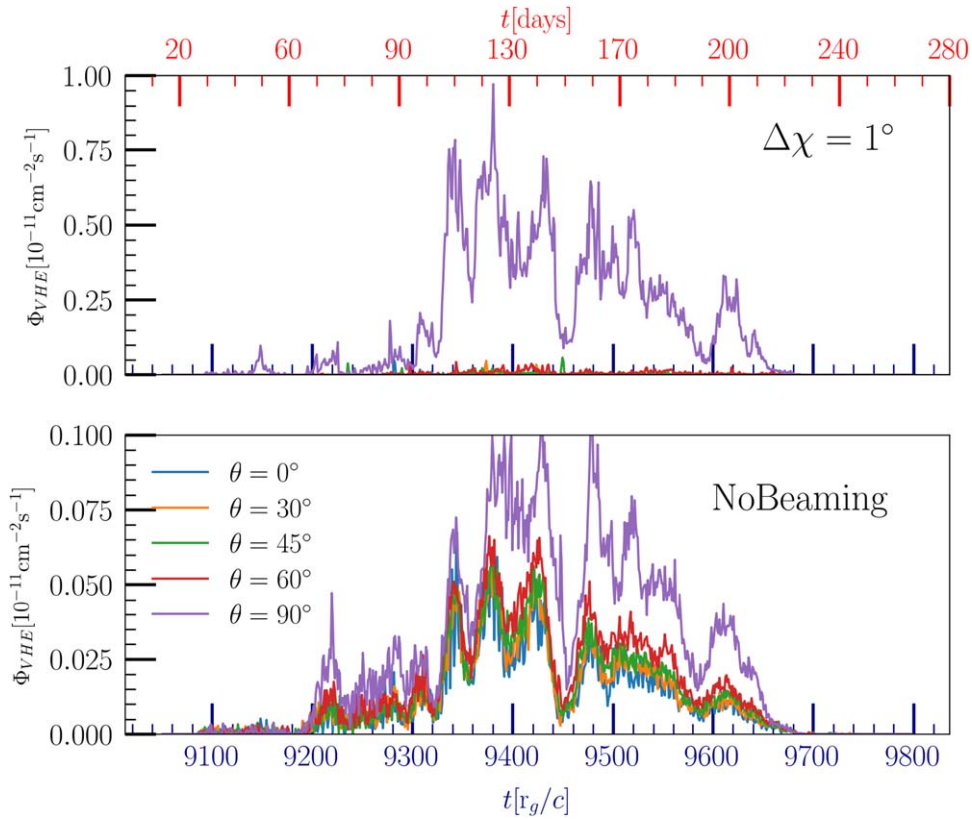


Figure 9. Same lightcurves as in Figure 7 but plotted on a linear scale on the y-axis to better compare with the observations. The superphoton counts are converted to a photon number flux using the same procedure as in Figure 7. Although the entire flare lightcurve lasts for over 100 days, shorter-timescale features are still visible, resulting from the changing 4-volume of the current sheet.

5.3. Caveats

While our methods of constructing VHE lightcurves are motivated by self-consistent kinetic simulations, they contain several constraining assumptions that can be addressed in future work.

The plasma around M87* is collisionless, and first-principles modeling of reconnection dynamics requires fully kinetic simulations. In particular, axisymmetric GRPIC simulations showed that the timescale of magnetic flux eruptions can be shorter as a result of larger rate of magnetic reconnection in kinetic simulations (A. Galishnikova et al. 2023). This may well apply to the timescales for the variations in the current sheet volume in three-dimensional kinetic simulations, which we identified as one of the important sources of the VHE lightcurve variability during the eruption. This is particularly relevant because the shortest timescales in our ray traced lightcurves are still a factor of few longer compared to those observed in VHE flares.

A related source of uncertainty is connected with the geometry of flux eruptions. In particular, it remains to be seen whether more tilted current sheet geometries can be obtained in more realistic accretion setups that do not start with much-simplified rotating plasma tori (e.g., for tilted disks, C. J. White et al. 2019; K. Chatterjee et al. 2023; or in accretion flows with less ordered angular momentum, S. M. Ressler et al. 2023; A. Galishnikova et al. 2025). If more inclined current sheets can be realized, models with strong beaming could produce enough variability while still producing enough flux for nearly face-on viewing angles.

To construct the lightcurves, we assumed the same level of the beaming of IC radiation throughout the current sheet, using order-of-magnitude estimates for γ_{rad} and σ_c . Plasma magnetization, σ_c , is particularly uncertain because it is supposed to be set by the self-consistent regulation of pair density produced by high-energy synchrotron photons emitted by accelerated particles, and the global inflow-outflow effects. Local and global radiative kinetic simulations that can capture these effects are important to produce more reliable estimates of σ_c . Because of these uncertainties, we constructed lightcurves for both the strong cooling, $\sigma_c > \gamma_{\text{rad}}$ (strong beaming), and weak cooling, $\sigma_c \sim \gamma_{\text{rad}}$ (no beaming), regimes. For similar reasons, we do not attempt to construct energy-dependent lightcurves with different levels of beaming.

VHE observations of M87* constrain its optical depth $\tau \leq 0.2$ for $E \leq 10$ TeV (H. E. S. S. Collaboration et al. 2024). Therefore, our ray tracing does not include the effects of γ -ray attenuation, i.e., we assume $\tau = 0$). This assumption remains to be verified theoretically. In particular, the nominal γ - γ pair-production optical depth can be estimated to be ~ 1 for 1 TeV photons (H. Hakobyan et al. 2023b), assuming a quiescent soft-photon radiation field observed from M87* (A. E. Broderick & A. Tchekhovskoy 2015). This indicates that pair-production attenuation can be nonnegligible. However, the submillimeter flux from the inner accretion zone can be suppressed during the magnetic flux eruption (H. Jia et al. 2023), so that more detailed calculations are needed.

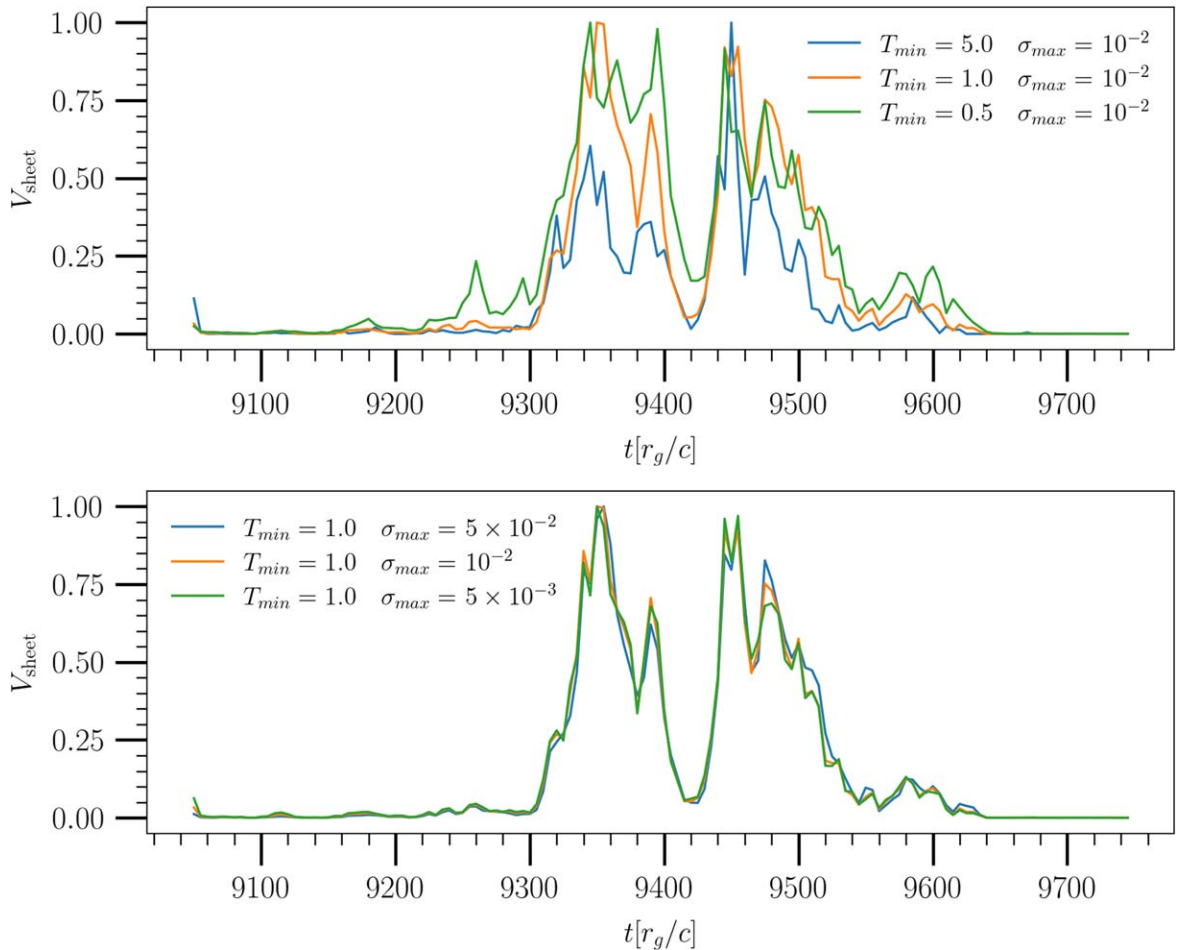


Figure 10. The re-scaled volumes of the current sheets identified using different (T, σ_c) thresholds as a function of the KS coordinate time. We separately vary the T and the σ_c thresholds to identify the current sheets and calculate the 4-volumes. The respective volumes are computed by summing up $dV_i = \sqrt{-g_i} d^4x$ of the current sheet, where dV_i is the four-dimensional volume of the current sheet cell i . They are normalized by dividing by the maximum volume attained during the flux eruption. Results from different T thresholds are shown in the left panel and for different σ_c thresholds in the right panel. Orange curves represent the default $T = 1$ and $\sigma_c = 10^{-2}$ thresholds used in the analysis in this paper. There are some differences in the relative change in 4-volumes while varying the temperature, but these differences occur on similar timescales. Varying σ_c produces very similar results. The 4-volumes all show shorter-timescale features that are related to the global, nonlinear dynamics of the system. These variations are imprinted on the VHE lightcurves in Figure 9.

6. Conclusions

Current sheet formation is ubiquitous in many astrophysical systems containing black holes and neutron stars. These are the sites of particle energization and production of the high-energy emission. However, first-principles modeling of the high-energy lightcurves from these systems can be challenging because of the large separation of scales between the Larmor radii of the accelerated particles and the system size. In this work, we describe a general method, which is applicable whenever the cooling length of high-energy emitting particles is short, such that they do not need to be traced through the global scales. We use the results from local kinetic simulations that describe the beaming of accelerated particles, combined with GRMHD simulations that capture the global dynamics, and in particular the geometry of the current sheet and upstream magnetic field. This procedure can be similarly applied to other astrophysical systems with different values of plasma magnetization, σ_c , and radiative cooling, γ_{rad} , parameters; different levels of beaming can be modeled based on the ratio of the two parameters.

The production of VHE emission from low-luminosity AGNs is not well understood. We explore the combined role of kinetic (beaming of accelerated particles) and global (current sheet

dynamics), including general-relativistic (photon orbits), effects on the VHE lightcurves by ray tracing GRMHD simulations of a rapidly spinning black hole undergoing large-scale magnetic flux eruptions. We find: (a) most of the emission originates from very close ($r \lesssim 5r_g$) to the black hole; (b) the duration of the observed flare is roughly equivalent to the time span of the magnetic flux eruption; (c) there are multiple subflares within the main flare that occur as a result of the changing volume of the current sheet, and this result is insensitive to the numerical procedure of the current sheet identification; and (d) there can be over a factor of 50 suppression of outgoing flux away from the equatorial plane in all of the lightcurves because of the IC beaming. Future VHE flare observations in multiple energy bands could better inform us about the parameters of the flaring plasma around the black hole M87*.

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Appendix A Thresholds for Current Sheet Identification

It is important to check how sensitive the identified current sheet, and therefore, the lightcurves are to the T and σ_c thresholds. To that end, we vary both thresholds, identify the corresponding current sheet, and plot the results in Figure 11. The minimum (dimensionless) temperature thresholds are taken from $\{0.5, 1, 5\}$ and the maximum σ_c thresholds from $\{5 \times 10^{-3}, 10^{-2}, 5 \times 10^{-2}\}$. The $T=1$ and $\sigma_c = 10^{-2}$ thresholds are used in the rest of the paper. The process is repeated for all of the simulation outputs, and the coordinates of the current sheet cells are combined and binned into the x - y coordinates. x , y , and z represent the cartesian KS coordinates that can be obtained from the standard transformation of spherical into Cartesian coordinates.

The binned data are weighted by $r^{-3.5}$ to account for the emissivity that is proportional to the strength of the upstream magnetic field in the fluid frame (see Section 3.3). The outer extent of the current sheet reduces for the $T=5$ threshold. However, in all of the cases, the current sheet structure in the inner $5r_g$ is very similar, where most of the emission originates in the lightcurves. We therefore conclude that $(T, \sigma_c) = (1, 10^{-2})$ are reasonable choices of thresholds to use for the current sheet identification.

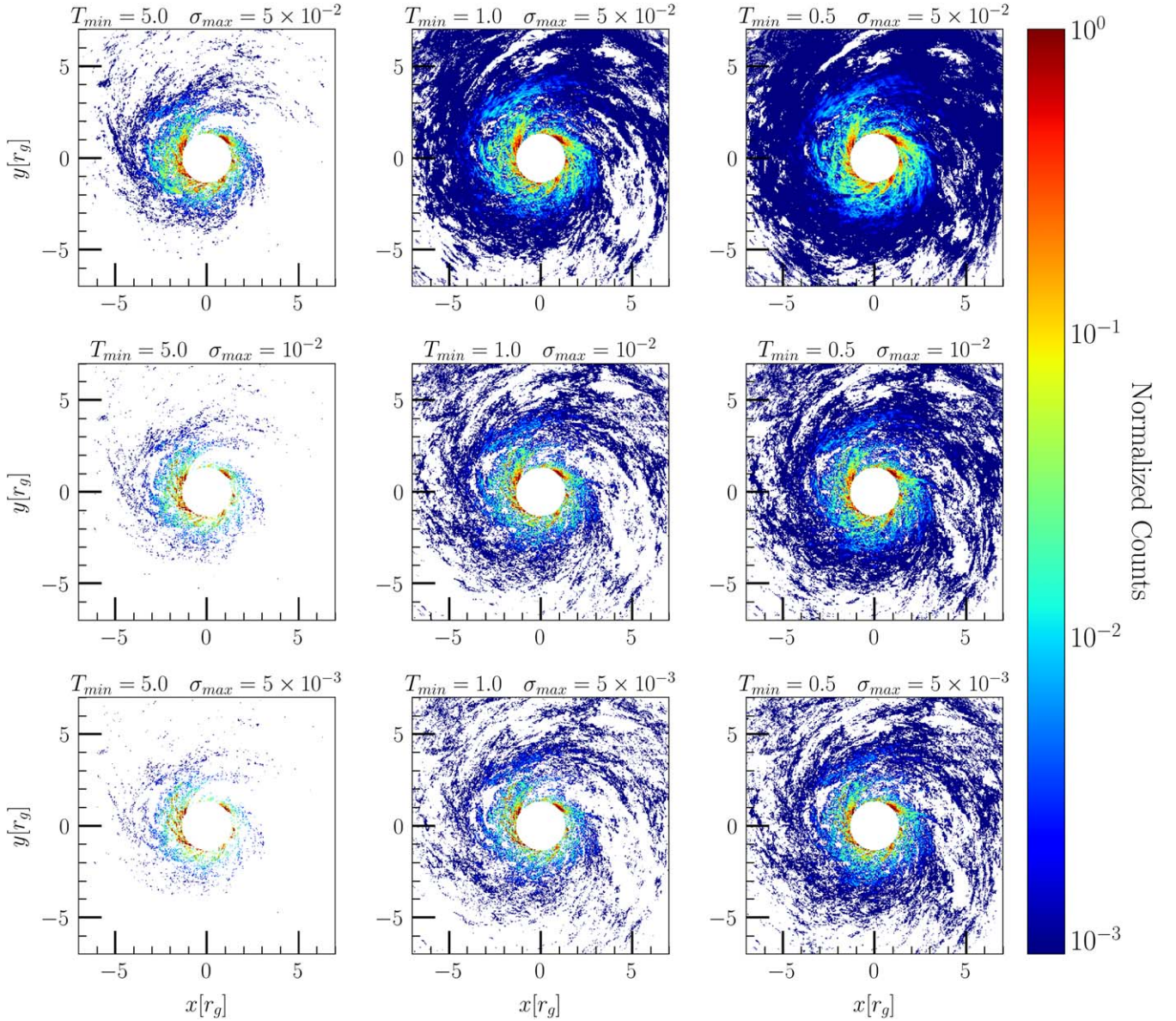


Figure 11. The location of the current sheet, identified using various (T, σ_c) thresholds. We plot the binned location of the current sheet zones after projecting them on the equatorial plane in Cartesian KS coordinates, weighted by $r^{-3.5} \propto b^2$. The weighting is proportional to the fluid-frame magnetic energy density that is proportional to the IC emissivity. The location of the current sheet close to the black hole ($r \lesssim 5r_g$) is similar for all of the thresholds, where most of the flux originates in our lightcurves.

Appendix B Selection of the Upstream Magnetic Field

The initial wavevectors of the geodesics depend on the upstream magnetic field when the effect of beaming is included in the model. We pick the upstream magnetic field vector by scanning a small spherical shell around every cell in the current sheet and then picking the magnetic field vector in the cube with the largest fluid-frame magnitude. Because the reconnecting field is less ordered than the upstream field, we set the inner radius of the shell to be $0.25 r_g$ to not pick any magnetic field

vector within the current sheet and vary the outer radius of the shell. Here, we compare the distributions of the selected upstream magnetic field using different values of the outer shell radii and show that the distribution of the identified upstream field does not depend strongly upon the choice of the outer radius. Figure 12 is a plot of two-dimensional histograms of the components of the upstream field as a function of r using different outer radii for the shells. The blue ($R_{\text{out}} = 0.4r_g$), red ($R_{\text{out}} = 0.35r_g$), and orange ($R_{\text{out}} = 0.3r_g$) distributions are similar, demonstrating that the selected upstream is independent of the size of the shell.

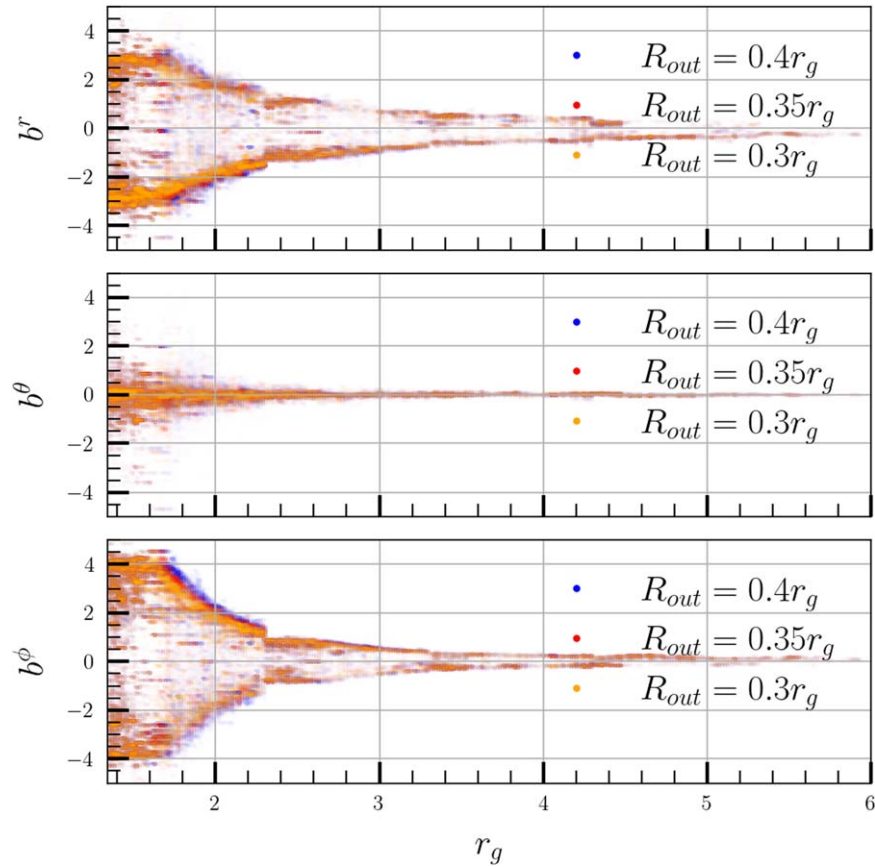


Figure 12. Shows two-dimensional histograms of the upstream magnetic field components with respect to the radial coordinate r . The panels from top to bottom show b^r , b^θ , and b^ϕ of the upstream field, respectively, and the colors represent various outer shell radii used to pick out the upstream magnetic field. Each color represents a different value of the outer radius of the spherical shell. Evidently, the upstream field distribution does not change much even after using larger radii for the spherical shells. Note that b^r , b^θ , and b^ϕ do not all have the same units.

Appendix C Convergence of Ray Tracing

There are various methods to test the accuracy and convergence of ray tracing method to compute the lightcurves. One can check whether the constants of motion (norm of the wavevector, energy, angular momentum, and Carter’s constant) are conserved along a select few geodesics. However, this does not necessarily guarantee convergence of the entire lightcurve. There may also be the issue of under-sampling, i.e., a very small number of superphotons make it to certain bins where the lightcurve is being computed. The lightcurve must also be numerically converged such that changing the step size of the integrator does not change the result. Here, we test our lightcurves using all of the above-mentioned metrics.

We integrate an ensemble of 60,000 superphotons randomly initialized to lie in the current sheet with a wavevector constructed as described in Section 3. We use an RK4 integrator for the geodesic integration with adaptive time

stepping taken from J. C. Dolence et al. (2009). We perform a scan over various initial time steps and measure the relative change in the norm, energy, angular momentum, and Carter’s constant evaluated at the initial (in the current sheet) and final (at $10^4 r_g$) positions of the superphotons. The superphotons have an initial wavevector norm $k^\mu k_\mu = 0$, and therefore we take the final value of $|k^\mu k_\mu|$ as the change in norm. The energy and angular momentum are calculated as $E = g_{\alpha t} k^\alpha$ and $L = g_{\alpha\phi} k^\alpha$, respectively, and we report $|(E_f - E_i)/(E_i + \epsilon)|$ and $|(L_f - L_i)/(L_i + \epsilon)|$, where $\epsilon = 10^{-20}$. Finally, we also compute the relative change in the Carter’s constant for the superphotons, which requires a coordinate transformation to BL coordinates. As is evident from Figure 13, the norm and the relative change in angular momentum are conserved to 1 part in 10^{-13} , the energy to roughly 1 part in 10^{-14} and the Carter’s constant to 1 part in 10^{-6} . The relatively large difference in the latter is partly due to errors in the coordinate transformation involving a nonlinear root find.

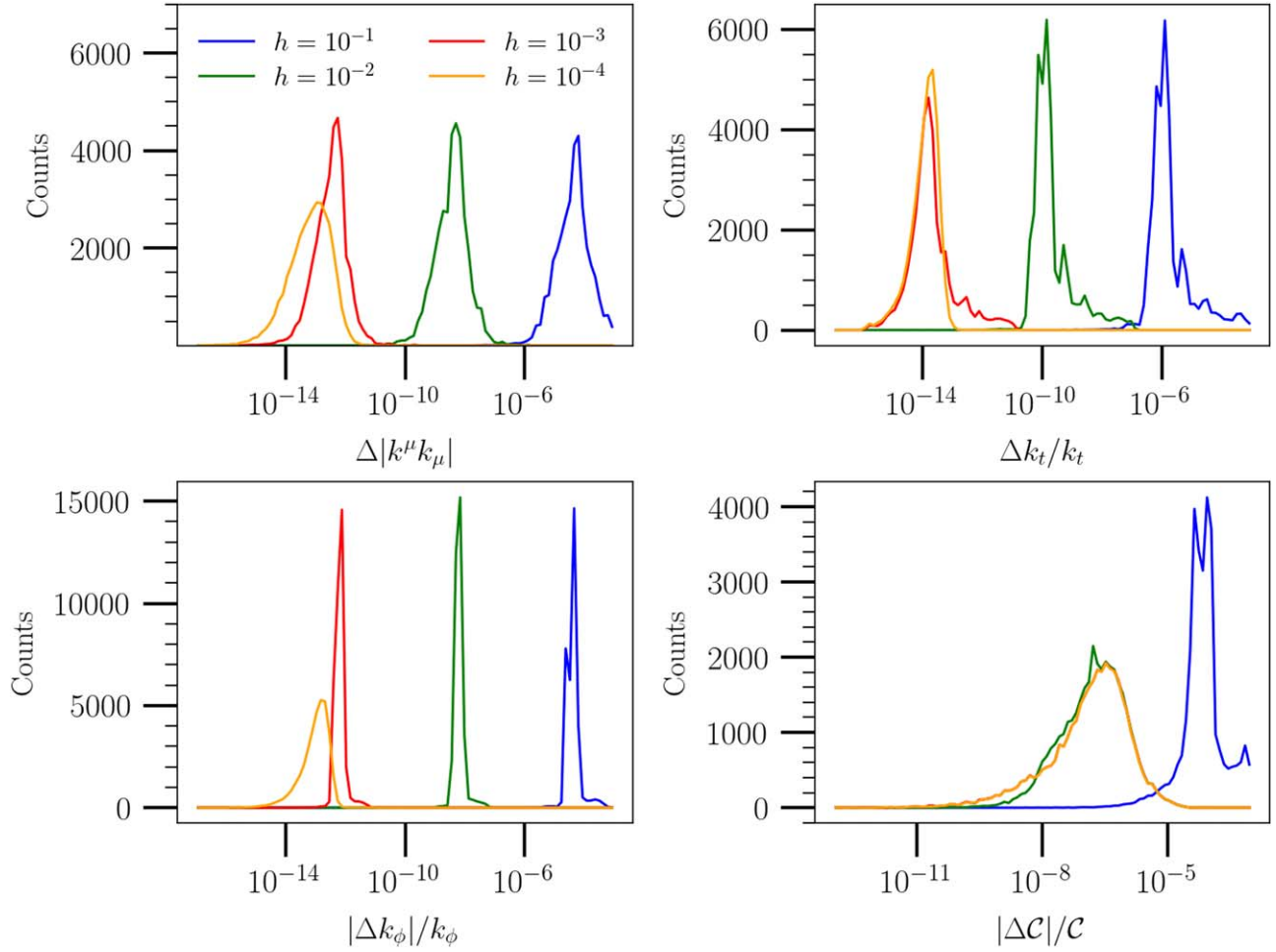


Figure 13. The relative error in the norm, energy, angular momentum, and Carter's constant of the 60,000 superphotons between the start and end of the numerical integration.

The numerical convergence of the arrival times of the superphotons is tested next. We once again integrate 60,000 randomly selected geodesics using initial step sizes of 10^{-1} , 10^{-2} , 10^{-3} , 10^{-4} , and $10^{-5} t_g$ with an RK4 integrator and adaptive time stepping. We construct the lightcurve by binning the t coordinates of the superphotons once they reach $10^4 r_g$. The generated lightcurves are shown in

Figure 14. The distributions converge to $\Delta t \lesssim 1 r_g/c$ for $h = 10^{-4}$ and $10^{-5} t_g$, despite the relatively small uncertainties in the constants of motion even at larger step sizes. This is because the steps are taken in $\log r$, and convergence in t is desired. Therefore, we use an initial step size of $h = 10^{-4}$ for our geodesic integration presented in this paper.

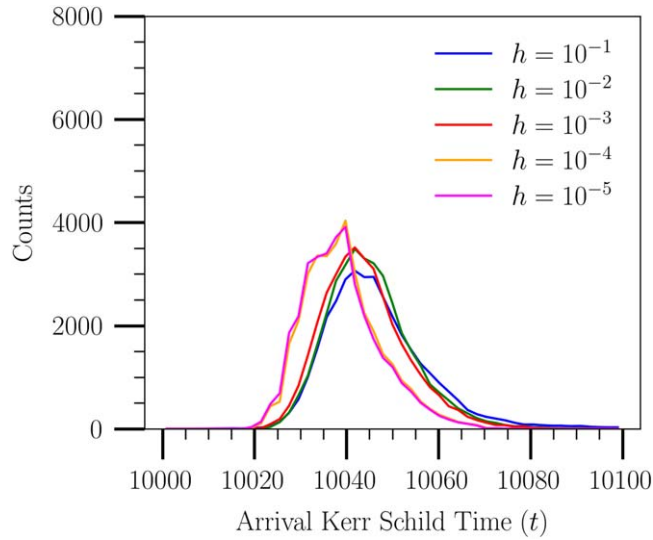


Figure 14. Convergence test by integrating the geodesics from a single simulation snapshot using different initial step sizes. This is done by binning the t coordinate of superphotons that reach $10^4 r_g$. We see acceptable convergence for an initial step size of $h \leq 10^{-4} t_g$, which is what we use for our geodesic integration presented in this paper.

Finally, we test the lightcurve convergence by sampling a different number of superphotons per point. That is, we initialize geodesics such that $N_i = c_i^{1/2}$, $5c_i^{1/2}$ and $10c_i^{1/2}$ such that each point in the current sheet has at least 1, 5, and 10 superphotons

initialized, respectively. As seen in Figure 15, the t , arrival t , θ , and ϕ coordinate distributions of the weighted superphotons are almost identical. We, therefore, use $N_i = c_i^{1/2}$ (i.e., at least 1 superphoton per point) for our ray traced lightcurves.

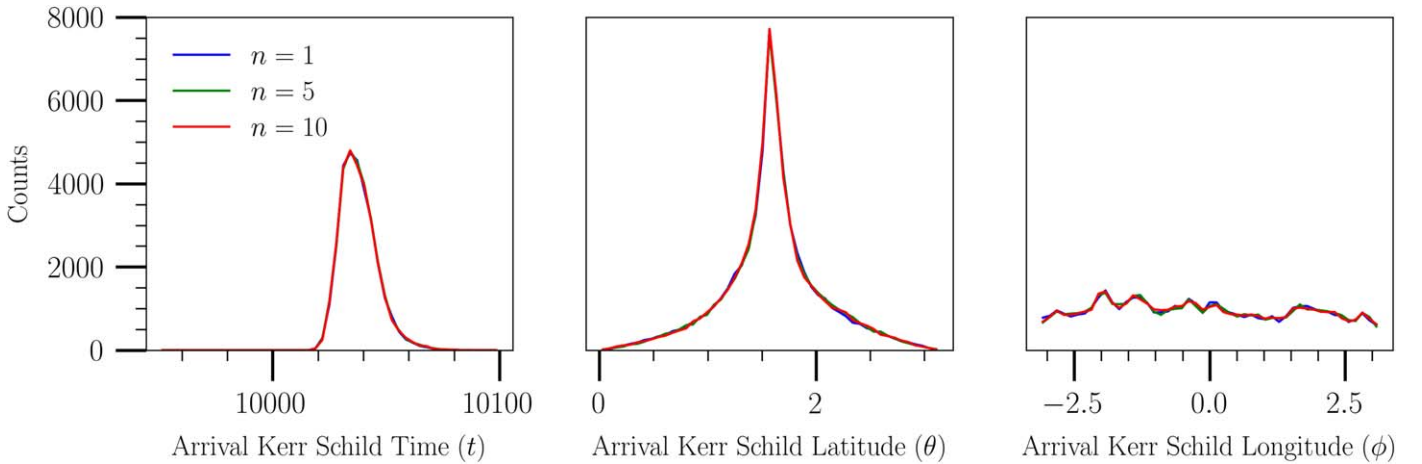






Figure 15. We test the convergence of the lightcurve by using a different number of minimum superphotons from each point in the current sheet. Here, we test the convergence in the t , θ , and ϕ coordinates by launching at least 1, 5, or 10 superphotons per cell in the current sheet. The coordinates of superphotons are binned once they cross $10^4 r_g$ after being weighted by the process described in Section 3.3. The final coordinate distributions for $N = 1, 5,$ and 10 lie on top of each other, indicating that superphotons are adequately sampled.

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