

# Experimental Integration of Quantum Key Distribution and Post-Quantum Cryptography in a Hybrid Quantum-Safe Cryptosystem

Lydia Garms, Taofiq K. Paraíso,\* Neil Hanley, Ayesha Khalid, Ciara Rafferty, James Grant, James Newman, Andrew J. Shields, Carlos Cid, and Maire O'Neill

Quantum key distribution (QKD) and post-quantum cryptography (PQC) are the two counter measures against cryptographic attacks via quantum computing. While QKD offers information theoretic security but limited authentication scalability, PQC facilitates scalable authentication in high density networks but is not information theoretic secure. Therefore, an ideal quantum-safe framework should efficiently leverage the complementarity of both techniques. However, despite growing efforts in integrating both, current realizations have focused on channel authentication, and a complete cryptosystem addressing both hybrid authentication and hybrid key exchange is yet to be demonstrated. Here, an authenticated hybrid key exchange protocol is introduced that incorporates PQC and QKD in a modular and information-theoretic secure architecture. The quantum-safe protocol is inherently resilient to catastrophic cryptographic failures and provides both forward and post-compromise security. As proof-of-concept implementation, the cryptosystem on a QKD hardware prototype is integrated, with the QKD processing, PQC key exchange and secret state masking via physical unclonable functions (PUFs) all running on a single field programmable gate array (FPGA). This work paves the way for the deployment of versatile and modular quantum-safe networks that exploit the complementarity of PQC and QKD.

parties involved in the key exchange. This shared secret can subsequently be used for fast, efficient symmetric encryption. Provided all bits in the key are unpredictable and the key is as long as the message, the Vernam cipher or one-time pad (OTP) can be used to ensure information theoretic security of the ciphertext. However, due to the practical cost of the OTP for long messages, our modern encryption schemes are instead based on computational hardness assumptions. Assuming that secure schemes for symmetric encryption and authenticated key exchange are used, the resulting ciphertext will also be secure.<sup>[1]</sup> In the symmetric setting, parties can authenticate a message with a message authentication code (MAC) that makes use of a pre-shared key. Only the other party holding the same pre-shared key can verify the MAC. In the asymmetric setting, a party can use a secret key to sign a message with a digital signature scheme and anyone with access to their public key can verify the signature. Existing asymmetric cryptographic primitives such as Rivest-Shamir-Adleman (RSA) and elliptic curve cryptography (ECC)

are used as building blocks to perform authenticated key exchanges.

As we move closer to the realization of large-scale, fault-tolerant quantum computers,<sup>[2–8]</sup> current cryptographic

## 1. Introduction

Authenticated key exchange allows two parties who have never met to agree on a shared secret, while verifying the identities of

L. Garms, C. Cid  
Information Security Group  
Royal Holloway  
University of London  
Egham TW20 0EX, UK

The ORCID identification number(s) for the author(s) of this article can be found under <https://doi.org/10.1002/qute.202300304>

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T. K. Paraíso, J. Newman, A. J. Shields  
Toshiba Europe Ltd.

Cambridge Research Laboratory  
Cambridge CB4 0GZ, UK

E-mail: [taofiq.paraíso@crl.toshiba.co.uk](mailto:taofiq.paraíso@crl.toshiba.co.uk)

N. Hanley, A. Khalid, C. Rafferty, J. Grant, M. O'Neill  
Centre for Secure Information Technologies (CSIT)  
Queen's University Belfast  
Belfast BT3 9DT, UK

C. Cid  
Simula UiB  
Bergen 5006, Norway

C. Cid  
Okinawa Institute of Science and Technology Graduate University  
Okinawa 904-0495, Japan

standards are under threat. Quantum algorithms such as Shor's algorithm<sup>[9]</sup> and Grover's search algorithm<sup>[10]</sup> have the potential to completely break the widely used asymmetric RSA and ECC algorithms, while halving the security strength of symmetric-key algorithms such as Advanced Encryption Standard (AES). To date, only two different cryptographic approaches are deemed quantum-safe, i.e., immune to attacks by quantum computers. First, a physical approach, quantum key distribution (QKD), which produces information theoretic secure (ITS) symmetric encryption keys between two remote parties Alice and Bob, where the source of security is underpinned by the communication of quantum light signals.<sup>[11]</sup> QKD has reached a number of breakthroughs toward global intercontinental deployment, including high secret key generation rates,<sup>[12–15]</sup> long-distance quantum communications,<sup>[16–22]</sup> photonic integration,<sup>[23–27]</sup> and terrestrial and satellite-based network deployment.<sup>[28,29]</sup> Second, an algorithmic approach, post-quantum cryptography (PQC), which deploys new asymmetric protocols that can run on classical computers but are believed to be secure against known quantum computing attacks. In 2016, the National Institute of Standards and Technology (NIST) initiated a PQC competition to standardize quantum resistant algorithms (QRAs) for key exchange mechanisms (KEMs) and digital signature algorithms (DSAs).<sup>[30]</sup> The winning algorithms were announced in July 2022, with standardization to follow in 2024.<sup>[31]</sup>

Hybrid cryptography combines multiple cryptographic primitives to allow security to be based on a wide range of hard problems, helping to mitigate against unknown possible attacks. The security of a hybrid cryptosystem holds as long as one of the primitives is secure, thus reinforcing security over longer term. Historically, the term hybrid referred to a combination of symmetric and asymmetric algorithms.<sup>[32]</sup> In the context of PQC migration, the use of hybrid schemes combining classical and post-quantum public-key algorithms is already advocated, as they can guarantee inter-operability during the transition phase.<sup>[33–35]</sup> Further hybrid schemes combining the advantages of both QKD and PQC would greatly benefit our communication security. A natural first step in this direction is to enhance the scalability of QKD authentication using post-quantum (PQ) digital signatures.<sup>[36,37]</sup> Going beyond this step and completely merging QKD and PQC in a hybrid cryptosystem would further exploit the full potential of quantum-safe primitives and add considerable gain in terms of security: the encryption keys will remain secure even in the event of a catastrophic failure of one of the primitives caused by advances in quantum computing, or unforeseen attacks on less well established PQ algorithms.<sup>[38]</sup>

In this work, we present and demonstrate experimentally a hybrid quantum-safe cryptosystem capable of ITS authentication and key exchange. We incorporate QKD with a post-quantum DSA (PQ-DSA), a post-quantum KEM (PQ-KEM), their classical counterparts, an ITS MAC (IMAC) and a key derivation function (KDF). In addition, we provide an extra layer of hardware security by making use of a PUF for masking the secret state and tying it to the physical hardware device. The full protocol is implemented on a commercial QKD prototype where the PQ-KEM and PUF primitives are all executed by the same FPGA that executes the QKD functions. Our results constitute a new paradigm for hybrid quantum-safe cryptography, providing pathways toward information theoretic secure cryptosystems and their seamless

deployment in existing quantum communication infrastructures for ultimate resilience against quantum computing threats.

## 2. Results

### 2.1. Protocol Description

A hybrid cryptosystem combines cryptographic material from different protocols to ensure that the resulting protocol is secure provided at least one of these building blocks remains secure. Our protocol is based on the proposal by Dowling, Hansen and Patterson,<sup>[39]</sup> who provided the first security framework for a hybrid authenticated key exchange (HAKE) protocol combining QKD and PQC and proved the protocol secure in this model. While the original protocol did not include PQ-DSA and did not provide a complete ITS implementation, we propose a modular protocol, Muckle++, that incorporates both PQ-DSA and advanced cryptographic building blocks to support broader functionality, and which can easily be replaced to meet application requirements of efficiency and security.

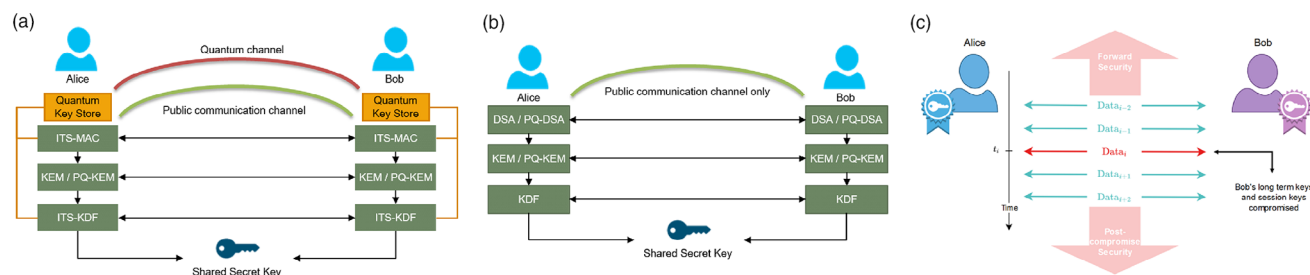
The security of a cryptographic protocol is strongly linked to its authentication mechanism. QKD nodes are conventionally authenticated using pair-wise pre-shared keys. While this approach is suitable for a small number of nodes, it may not easily scale to high-density networks, which could even include links without quantum capable hardware, such as very long distance links or wireless links. We therefore propose the flexibility of authenticating with or without pre-shared keys and provide security proofs in both cases. This modular feature is illustrated in **Figure 1a,b**. In the absence of pre-shared keys, the protocol makes use of a classical and a PQ digital signature scheme. As authentication must now rely on long-term asymmetric secrets, information theoretic security is not achievable in this setting, though the protocol remains computationally quantum-safe. When we can assume that nodes in the network have established pre-shared keys, our protocol can authenticate with a MAC combined with pre-shared key material. In this optimal instantiation, our protocol is provably ITS for both authentication and key exchange and does not rely on computational hardness assumptions. In **Notes S2 and S3** (Supporting Information), we provide detailed security proofs for both settings within an updated HAKE security framework.

In both cases, the HAKE architecture further guarantees noteworthy security features illustrated in **Figure 1c**:

1. The key exchange protocol remains secure, provided at least any one of three ingredients: QKD, classical key exchange and quantum resistant key exchange, remains secure.
2. The secret state allows for *post-compromise security*;<sup>[40]</sup> that is, security can be recovered in the event of session keys being leaked.
3. *Forward security* is guaranteed, ensuring that a security breach will not affect the security of previous keys.

**Figure 2** gives a flow diagram of the protocol. The process is summarized as follows:

- (i) *Session initialization*. Before the first communication session, the initiator Alice and responder Bob are set up with identifiers, a pre-shared key (or alternatively long-term



**Figure 1.** Protocol security features. a) Optimal instantiation: in the presence of QKD hardware, quantum key material is combined to an ITS MAC and to the KDF to achieve an ITS cryptosystem. b) In the absence of QKD hardware, e.g. wireless links, authentication is done using hybrid DSA and keys are constructed using a standard KDF. The protocol is quantum-safe but not ITS. c) Forward and post-compromise security. At time  $t_i$  the security of Bob's long term keys and session key is compromised by an attacker. Forward secrecy ensures that messages exchanged at earlier times remain protected. Post-compromise security ensures that future messages remain protected.

classical and post-quantum public keys and their own secret keys), the secret state *SecState* (initially set to 0) and a counter *ctr* (initially set to 0). In subsequent communication sessions the secret state and counter are retained from the previous session.

- (ii) **Public Key Generation.** The initiator generates the public/private key pairs using both the classical KEM and the PQ-KEM. The quantum key material generated from a QKD protocol is interpreted as a shared array of random bits that both parties can access. A first message,  $m_0$ , is then formed to send the classical and PQ public keys ( $lcpk_A, lqpk_A$ ) to the responder along with a header containing the type of KEM primitives used and an identifier of the party sending the message.
- (iii) **Message authentication.** Authentication is needed before sending the message. If a pre-shared key is available, the message is authenticated with an IMAC tag ( $\tau_0 / \tau_1$ ), where the secret key ( $mkey_A / mkey_B$ ) combines the pre-shared keys of both parties, and the secret state saved from the previous session. Otherwise, a MAC tag is generated conventionally and both the message and MAC tag are signed with both a classical and a PQ signatures ( $\sigma_0 / \sigma_1$  and  $\sigma'_0 / \sigma'_1$ ) using the long-term keys.
- (iv) **Key exchange.** Upon reception of the first message, tag and signatures, the responder verifies the tag against the message and if successful proceeds to the key encapsulation steps. The encapsulated keys are sent in a second message  $m_1$ , authenticated with the same procedure as  $m_0$ . After verification of the second message and key decapsulation, the classical and PQ KEMs are completed and the link is authenticated for the generation of quantum key material (QKM) using a QKD protocol.
- (v) **Key derivation.** The resulting session keys  $sk_A, sk_B$  are derived from the messages sent, the symmetric keys generated by the classical and post-quantum KEM, QKM, as well as the secret state to ensure post-compromise security. The QKM can be interpreted as a shared array of quantum random bits that both parties can access. These elements are successively input to a PRF.
- (vi) **Secret state.** Finally, the output of the final PRF is split into the secret session keys of both users, as well as the secret state for the next session.

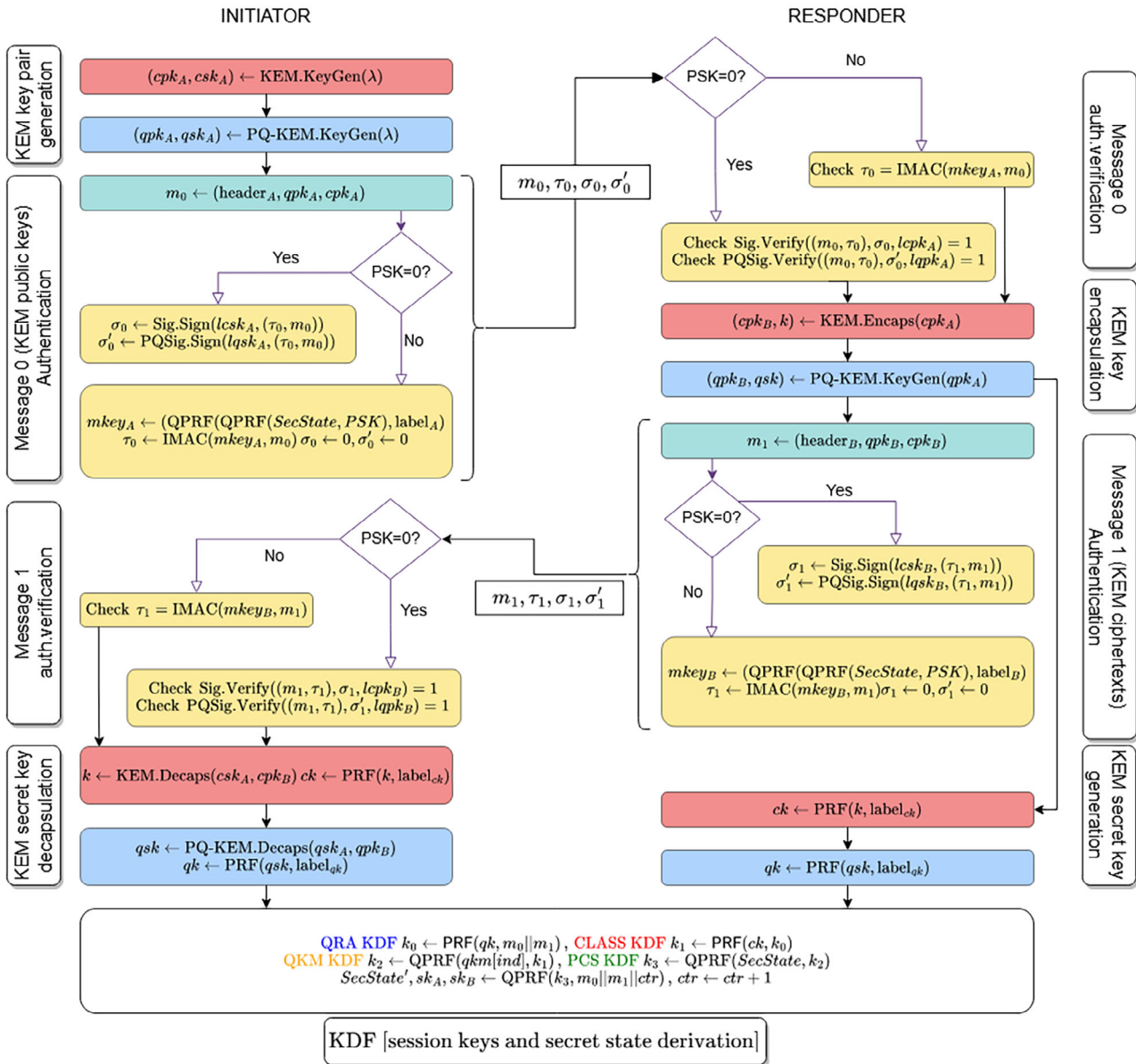
## 2.2. Selected Cryptographic Primitives

**Table 1** summarizes the concrete instantiation of each cryptographic building block in our protocol. A detailed introduction to the different primitives is provided in Note S1 (Supporting Information). For the PQ-KEM, CRYSTALS Kyber,<sup>[41]</sup> on the NIST standardization track<sup>[31]</sup> was selected, while for the PQ digital signature, FALCON,<sup>[42]</sup> which is also on the standardization track, was selected. Both are lattice-based schemes, with FALCON the most compact of the selected NIST digital signature candidates. Lattice-based cryptographic schemes have been widely studied, and in general have computation speeds similar to, if not faster than, their classical equivalents. However, this is offset by the fact that their keys and ciphertexts can be significantly larger. The quantum key material is generated via a T12 protocol.<sup>[43]</sup> To instantiate the QPRF, a keyed-hash MAC (HMAC)-based KDF (HKDF)<sup>[44]</sup> was modified by xor-ing quantum key material to the PRF output.

For the IMAC, the Poly1305-AES MAC<sup>[45]</sup> construction was combined with QKM to ensure ITS assuming the security of the quantum key distribution holds. In Note S4 (Supporting Information) this scheme is detailed in full, alongside with proofs that the construction remains computationally secure if the security of the QKD is broken, and proof that ITS is achieved if the QKD remains secure.

## 2.3. System Architecture and Hardware Implementation

The cryptosystem was deployed on a high-speed commercial-grade QKD system prototype<sup>[13]</sup> consisting of two units, a quantum transmitter and a quantum receiver, configured to exchange quantum secure keys using the T12 protocol.<sup>[43]</sup> These are state-of-the-art systems able to generate QKD keys at rates of a few Mb/s, enabling the generation of a large store of pre-shared quantum key material between distant parties in a very short time. The overall architecture of the hybrid cryptosystem is shown in **Figure 3**. Each unit contains the discrete optics required to prepare or measure time-bin-encoded weak coherent pulses, the corresponding control electronics, an FPGA acting as the central QKD processor, and a server for the public channel communication.



**Figure 2.** Simplified flow diagram of the Muckle++ protocol. Hybrid classical/post-quantum asymmetric key exchange and authentication is used in conjunction with QKD to derive session keys and secret state. In the presence of pre-shared keys (PSKs), authentication is provided by an IMAC construction. Otherwise, hybrid classical and PQ digital signatures are used to sign the messages. The final key derivation step combines the different key materials by successively inputting the PQ key, the classical key, the QKD key, as well as the secret state for post-compromise security (PCS), in a series of PRFs. In the absence of QKD hardware, a standard PRF replaces the QPRF.

The FPGAs are used to control the optical hardware and for the sifting procedure, where the preparation and measurement bases are compared to only retain events where Alice and Bob selected matching bases. The resulting sifted keys are transferred from the FPGAs to the servers for the classical post-processing of the key. The first post-processing step is the error correction of the sifted keys, which is based on a low density parity check algorithm. From the error correction and sifting results, the quantum bit error rate and the photon statistics for the different intensity states (signal, decoy and vacuum) can be evaluated.<sup>[43]</sup> These parameters are essential to estimate and bound the single photon

contribution to the key information and to perform the second post-processing step, i.e., privacy amplification.

To incorporate the HAKE on the QKD system, we implemented the main routine of the protocol as a c++ code executed on the server and featuring a hardware abstraction layer (HAL) providing access to the cryptographic components running in hardware built on a FPGA connected via Ethernet. We developed custom FPGA cores to execute the CRYSTALS Kyber PQ-KEM algorithm and the PUF functions for secret state masking alongside core QKD functions such as key sifting and photon statistics evaluation. The classical KEM, the DSA, the MAC and the



**Table 1.** Algorithms/protocols and parameters used to instantiate the cryptographic building blocks in the Muckle++ cryptosystem.

Building Blocks (see Note S1, Supporting Information)	Algorithm/Protocol	Parameters
KEM	Ephemeral elliptic curve Diffie-Hellman key exchange <sup>[47]</sup>	Curve25519 <sup>[46]</sup>
PQ-KEM	CRYSTALS Kyber <sup>[41]</sup>	$k = 3$
PRF	HKDF <sup>[44]</sup>	256-bit keys
QPRF	HKDF xored with quantum key material	256-bit keys
IMAC (see Note S4, Supporting Information)	Poly1305-AES <sup>[45]</sup> combined with quantum key material	256-bit AES keys
DSA	Elliptic curve digital signature algorithm (ECDSA) <sup>[48]</sup>	Elliptic curve NIST P-256 and SHA-256 hash function
PQ-DSA	FALCON <sup>[42]</sup>	$(n = 512, q = 12289)$
QKD	T12 <sup>[43]</sup>	1-Mbit keys, $\epsilon < 10^{-10}$

QPRF are performed on the server. A common daemon enables the communication between the main software and the different hardware cores.

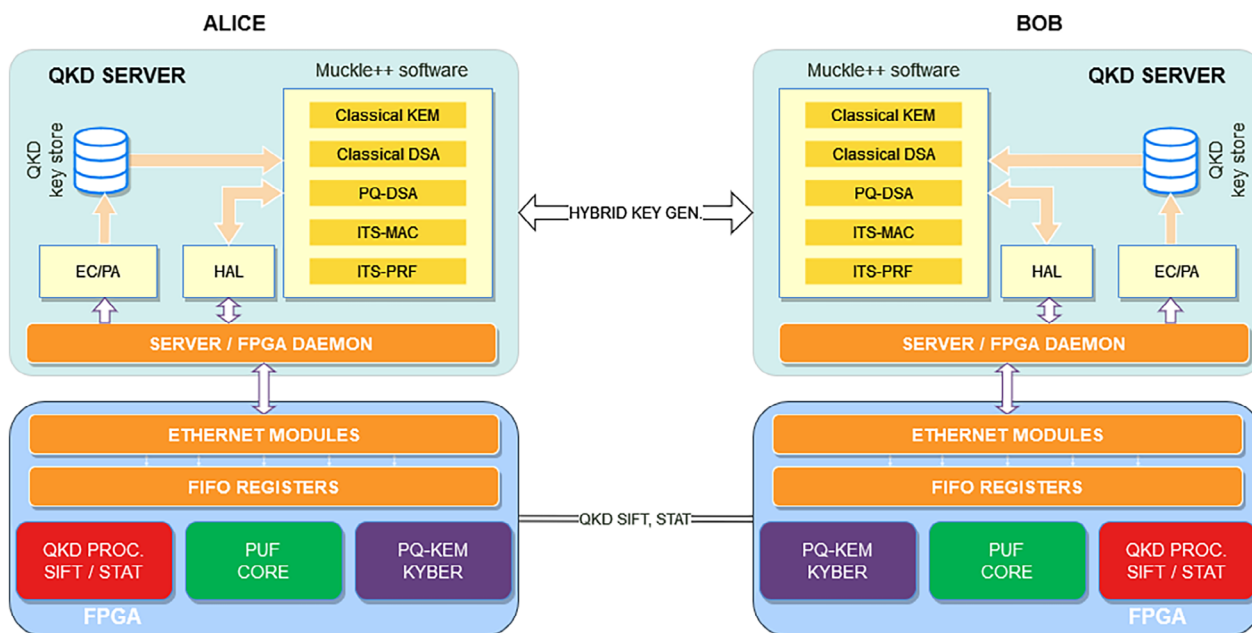
## 2.4. Platform Authentication

FPGA-based PUFs are used for authentication of the physical FPGA devices, providing an additional layer of security. Prior to storing the Muckle++ secret state in memory after a key exchange, it is first masked by the PUF response. This PUF response is based on the unique manufacturing variations of the physical hardware device itself, and can be viewed as an intrinsic digital fingerprint of the device. Therefore, in order to subsequently unmask the secret state to generate the next session key, the code must be run on physically the same hardware device in order to generate the required PUF response. This ensures that the underlying FPGA, where the QKD processing occurs, has not

been modified, providing additional protection for the generated keys and binding the exact FPGA device to the server. A symmetric encryption scheme is used to mask the state, with the specific instantiation being AES<sup>[49]</sup> in Galois/counter mode (GCM) with a 256-bit key derived from the PUF response. The PUF is a modified version of that proposed in Ref. [50], with a majority vote of 3 and a  $[23, 12, 7]_2$  binary Golay code used for error correction. Both the majority vote and the algorithm are performed in hardware and abstracted away from the Muckle++ software.

## 2.5. Performance and Hybrid Key Generation

Following Figure 3, the software implementing the Muckle++ protocol was run on a pair of commercial servers connected via Ethernet to FPGAs. The FPGAs contained intellectual property (IP) cores for QKD processing, Kyber encapsulation and decapsulation and PUF operations. The resource requirements for the



**Figure 3.** System architecture. The cryptosystem is deployed on a commercial QKD system prototype. The main software runs on the QKD servers where the classical primitives, the PQ-DSA, the MACs, and PRFs are executed alongwith the QKD error correction and privacy amplification. A hardware implementation of the PQ-KEM and the PUF was designed to execute them on the same FPGA that performs the core QKD functions.



chosen in this work to instantiate the PQ-KEM and PQ-DSA, respectfully, among future standard quantum resistant algorithms. A standardization process on their implementation has now started and will be completed within the next 2 years.

**Related Works:** After completion of this manuscript, we became aware of a related work ref. [51] that also aims at extending the work by Dowling et al. [39] although without the emphasis on information theoretic security as it is devised in the current work.

## Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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## Conflict of Interest

The authors declare no conflict of interest.

## Author Contributions

L.G. and C.C. developed the software and derived the security analysis. N.H., A.K., C.R., and J.G. developed the FPGA hardware acceleration firmware including the puf engine. J.G. and J.N. developed the hardware interface layer between the software and the QKD FPGA with input from N.H. and T.P.. T.P. deployed the project on the QKD system with input from L.G., N.H., J.G., and J.N. and ran the experiment. L.G., T.P., N.H., and A.K. wrote the manuscript with comments from the other authors. A.J.S., C.C., and M.O.N. supervised the project.

## Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

## Keywords

hybrid authenticated cryptosystem, information theoretic security, post-quantum cryptography, quantum cryptography, quantum key distribution

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