

$H \rightarrow \tau^+\tau^-$ branching ratio study at $\sqrt{s} = 250$ GeV at the ILC with the ILD detector

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Abstract

We evaluated the measurement accuracy of the branching ratio of $H \rightarrow \tau^+\tau^-$ mode at $\sqrt{s} = 250$ GeV at the ILC with the ILD detector. We assumed the Higgs mass $M_H = 120$ GeV, branching ratio $\text{Br}(H \rightarrow \tau^+\tau^-) = 8.0$ %, beam polarization $P(e^-, e^+) = (-0.8, +0.3)$, and integrated luminosity $\int L dt = 250 \text{ fb}^{-1}$. We used the LOI samples as the Monte-Carlo samples. The evaluation was performed by the ILD full detector simulation. All Standard Model backgrounds were included in this study. We obtained the accuracy $\Delta(\sigma \cdot \text{Br})/(\sigma \cdot \text{Br}) = 3.5$ %. The scaled result to $M_H = 125$ GeV is calculated to be 4.2 %.

1 Introduction

A new Higgs-like particle was discovered by the ATLAS and the CMS experiments [1, 2]. One of the next important themes for particle physics is the investigation of that new particle, especially the mass generation mechanism.

One of the important properties of Higgs boson is its branching ratio. In the Standard Model (SM) of particle physics, the Yukawa coupling constant of matter fermions with the Higgs boson is proportional to the fermion mass. Besides, if there is new physics, the coupling constant may deviate from the SM prediction. Therefore, the branching ratio is a probe for new physics.

In this note, we focus on the branching ratio of $H \rightarrow \tau^+\tau^-$ mode. We estimate the measurement accuracy of the $H \rightarrow \tau^+\tau^-$ branching ratio at $\sqrt{s} = 250$ GeV with the ILD full detector simulation.

2 Signal and Background

The main Higgs production process at $\sqrt{s} = 250$ GeV is the Higgs-strahlung process ($e^+e^- \rightarrow ZH$). There are three types of signal depending on the decay of the Z boson, as shown in Figure 1. In this note, we concentrate on (A) $Z \rightarrow l^+l^-$ mode and (B) $Z \rightarrow q\bar{q}$ mode.

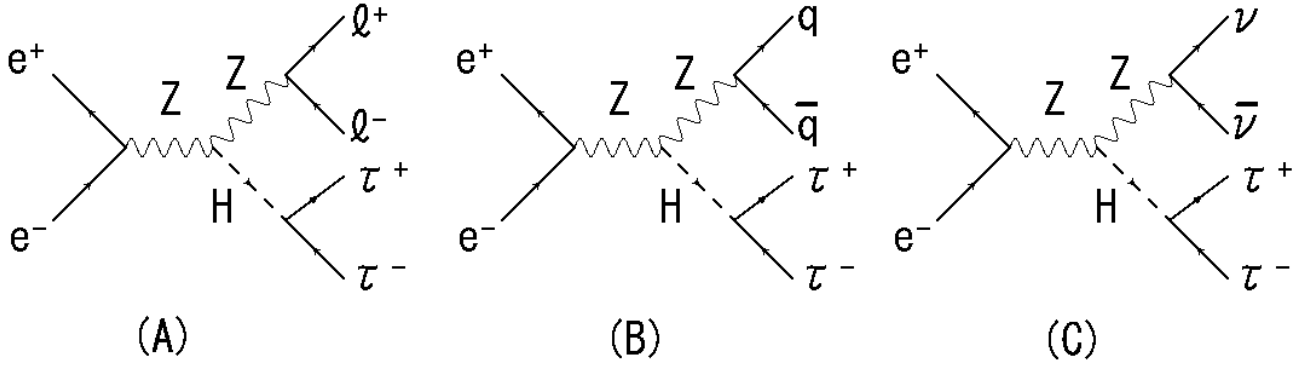


Figure 1: The diagrams of signal processes. (A): $Z \rightarrow l^+l^-$ mode, (B): $Z \rightarrow q\bar{q}$ mode, (C): $Z \rightarrow \nu\bar{\nu}$ mode.

The $Z \rightarrow \nu\bar{\nu}$ mode has been found to contribute negligibly to the overall precision which is dominated by the $Z \rightarrow q\bar{q}$ mode. However, at higher center-of-mass energies, the $e^+e^- \rightarrow \nu\bar{\nu}H$ mode is expected to contribute substantially due to the increase in the cross section of WW fusion process.

2.1 $Z \rightarrow l^+l^-$ mode

In this mode, we only considered $Z \rightarrow e^+e^-$ mode and $Z \rightarrow \mu^+\mu^-$ mode as the signal process. The signal cross section of this mode is 1.9 fb. The dominant background processes are the four leptons processes ($e^+e^- \rightarrow eeee$, $ee\mu\mu$, $ee\tau\tau$, $\mu\mu\mu\mu$, $\mu\mu\tau\tau$, and $\tau\tau\tau\tau$). An example diagram is shown in Figure 2-(A). Other background processes are $e^+e^- \rightarrow ZH$ reactions where the Higgs boson does not decay to tau pairs.

2.2 $Z \rightarrow q\bar{q}$ mode

The signal cross section of this mode is 19.8 fb. The possible background processes for this mode are $qqqq$, $qqll$, and $qq\nu\nu$, which come from $e^+e^- \rightarrow W^+W^-$ or $e^+e^- \rightarrow ZZ$ reactions. An example diagram is shown in Figure 2-(B). Other possible backgrounds are $e^+e^- \rightarrow ZH$ with $Z \rightarrow \tau^+\tau^-$ and $H \rightarrow q\bar{q}$. These processes have the same final state to the signal.

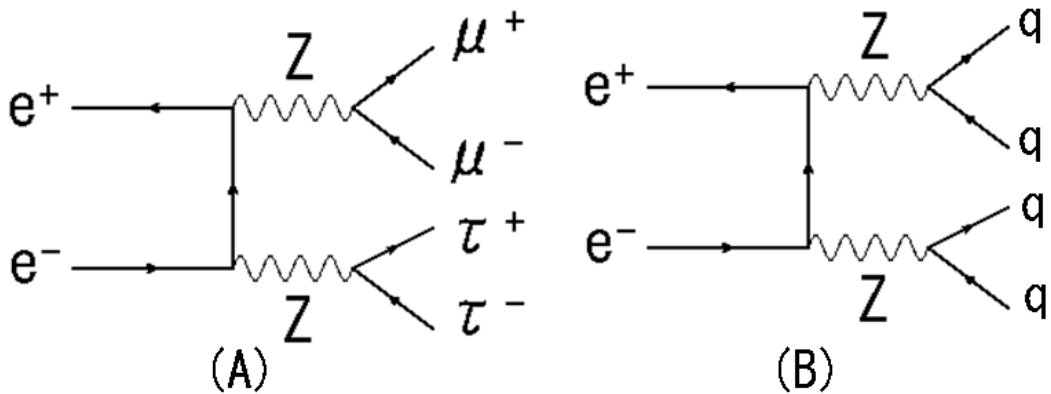


Figure 2: Example diagrams of possible background. (A): $\mu\mu\tau\tau$ background for $Z \rightarrow l^+l^-$ mode, (B): $qqqq$ background for $Z \rightarrow q\bar{q}$ mode.

3 Simulation Conditions

We performed the detector simulation with Mokka [3], a Geant4-based [4] full simulation, with the ILD_00 detector model. TAUOLA [5] was used for the tau decay simulation. The ILD_00 detector model consists of vertex detector, time projection chamber, electromagnetic calorimeter (ECAL), hadronic calorimeter (HCAL), and yoke.

We used the signal and background samples which were generated in the context of the Letter of Intent [6]. The assumed center-of-mass energy is 250 GeV. The effects of beamstrahlung and initial state radiation are included. All Monte-Carlo sample information (process ID, process, polarization, cross section, number of events, and luminosity) are summarized in Tables 6 (page 9) and 7 (page 10). We assumed the Higgs mass $M_H = 120$ GeV, branching ratio $\text{Br}(H \rightarrow \tau^+\tau^-) = 8.0\%$ as assumed by PYTHIA [8], integrated luminosity $\int L dt = 250 \text{ fb}^{-1}$, and beam polarization $P(e^+, e^-) = (+0.3, -0.8)$. We also rescale the final result to the case of $M_H = 125$ GeV and the $H \rightarrow \tau^+\tau^-$ branching ratio which includes the NNLO corrections [9].

4 Event Reconstruction and Event Selection

4.1 $Z \rightarrow l^+l^-$ mode

In this mode, we take the strategy of reconstructing the Z boson first, followed by the reconstruction of the tau pairs from the Higgs decay.

We applied lepton identification at first for dividing $Z \rightarrow e^+e^-$ events and $Z \rightarrow \mu^+\mu^-$ events by using the information of energy deposit in the calorimeter (E_{ECAL} and E_{HCAL} , where E_{ECAL} is the energy deposit in ECAL, E_{HCAL} is the energy deposit in HCAL, respectively) and track momentum (P_{track}). Figures 3 - 6 are the plots of $E_{\text{ECAL}}/(E_{\text{ECAL}} + E_{\text{HCAL}})$ and $(E_{\text{ECAL}} + E_{\text{HCAL}})/P_{\text{track}}$.

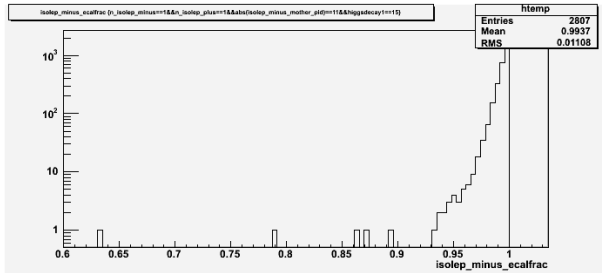


Figure 3: The plot of $E_{\text{ECAL}}/(E_{\text{ECAL}} + E_{\text{HCAL}})$ for the e in eeH samples.

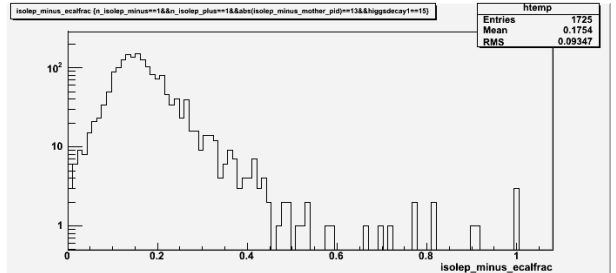


Figure 4: The plot of $E_{\text{ECAL}}/(E_{\text{ECAL}} + E_{\text{HCAL}})$ for the μ in $\mu\mu H$ samples.

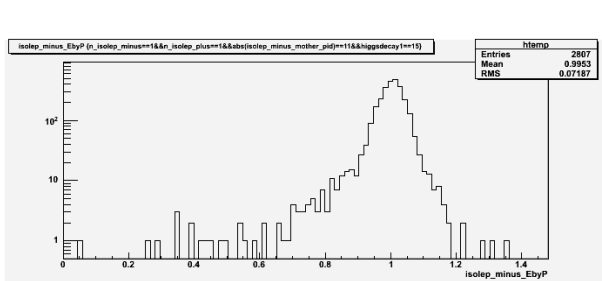


Figure 5: The plot of $(E_{\text{ECAL}} + E_{\text{HCAL}})/P_{\text{track}}$ for the e in eeH samples.

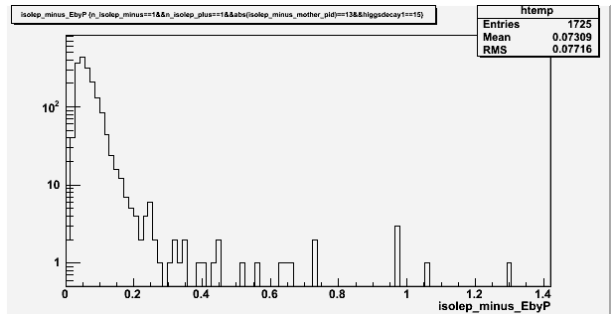


Figure 6: The plot of $(E_{\text{ECAL}} + E_{\text{HCAL}})/P_{\text{track}}$ for the μ in $\mu\mu H$ samples.

From these plots, we define the criteria for lepton identification. The criteria for electron identification (e -ID) are: $E_{\text{ECAL}}/(E_{\text{ECAL}} + E_{\text{HCAL}}) > 0.92$ and $(E_{\text{ECAL}} + E_{\text{HCAL}})/P_{\text{track}} > 0.5$. The criteria for muon identification (μ -ID) are: $E_{\text{ECAL}}/(E_{\text{ECAL}} + E_{\text{HCAL}}) < 0.6$ and $(E_{\text{ECAL}} + E_{\text{HCAL}})/P_{\text{track}} < 0.5$.

After the lepton identification, we applied selections to remove secondary leptons from tau decays. The strategy of this selection is to remove tracks which do not come from the interaction point (IP) by using the track energy E_{track} and impact parameter in the transverse direction d_0 and longitudinal direction z_0 with respect to the beam axis. Figures 7 - 12 show the $|d_0/\sigma(d_0)|$, $|z_0/\sigma(z_0)|$, and E_{track} plots which through the lepton identification. We defined the tau rejection cut for the objects through the e -ID: $|d_0/\sigma(d_0)| < 50$, $|z_0/\sigma(z_0)| < 5$, and $E_{\text{track}} > 10$ GeV, and for the objects through the μ -ID: $|d_0/\sigma(d_0)| < 3$, $|z_0/\sigma(z_0)| < 7$, and $E_{\text{track}} > 20$ GeV.

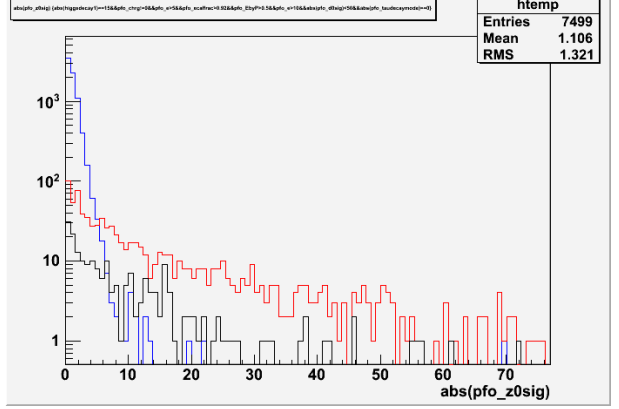
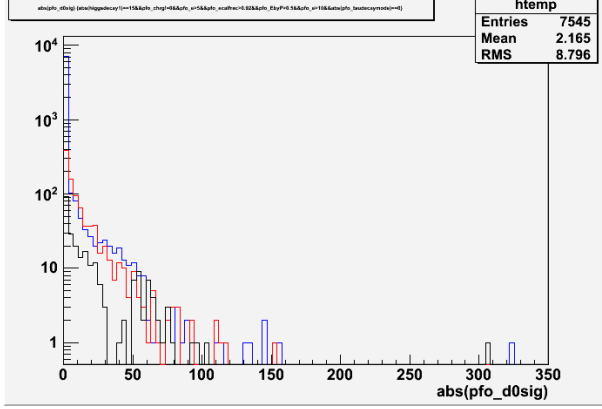


Figure 7: The plot of $|d_0/\sigma(d_0)|$ of e of eeH process. Blue, red, and black histograms show the e from $Z \rightarrow e^+e^-$, the e from $\tau \rightarrow e\nu\nu$, and the hadrons from τ decay, respectively. Figure 8: The plot of $|z_0/\sigma(z_0)|$ of e of eeH process. Blue, red, and black histograms show the e from $Z \rightarrow e^+e^-$, the e from $\tau \rightarrow e\nu\nu$, and the hadrons from τ decay, respectively.

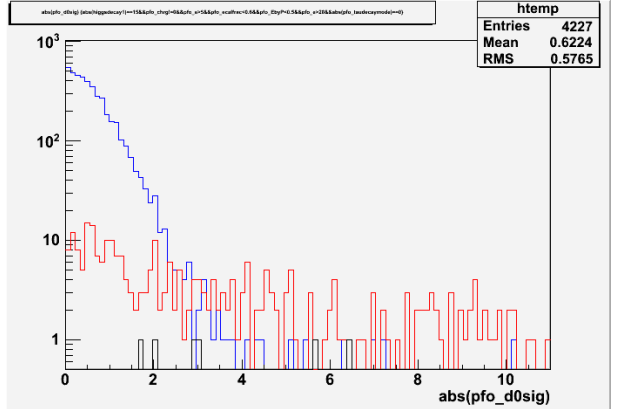
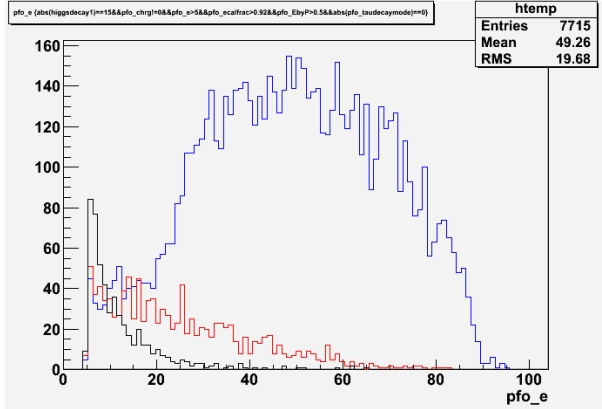


Figure 9: The plot of E_{track} of e of eeH process. Blue, red, and black histograms show the e from $Z \rightarrow e^+e^-$, the e from $\tau \rightarrow e\nu\nu$, and the hadrons from τ decay, respectively. Figure 10: The plot of $|d_0/\sigma(d_0)|$ of μ of $\mu\mu H$ process. Blue, red, and black histograms show the μ from $Z \rightarrow \mu^+\mu^-$, the μ from $\tau \rightarrow \mu\nu\nu$, and the hadrons from τ decay, respectively.

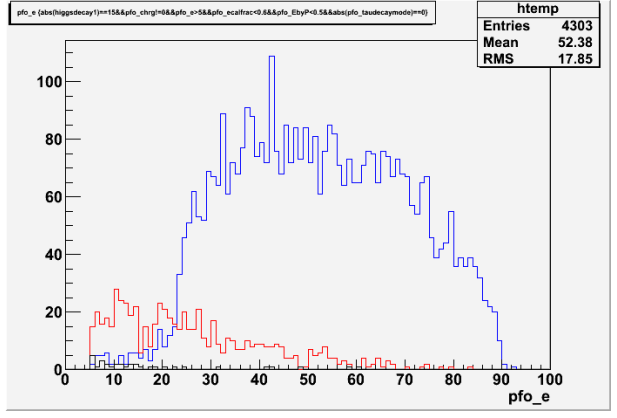
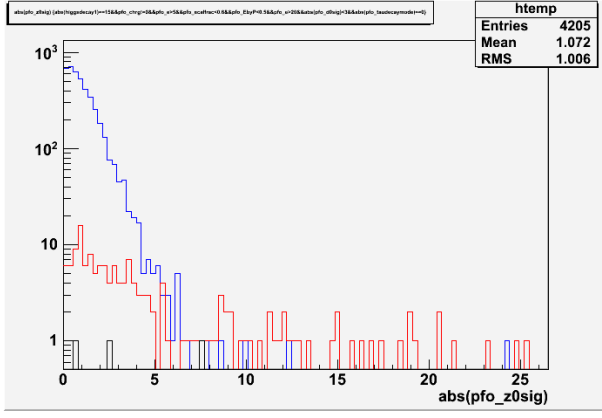


Figure 11: The plot of $|z_0/\sigma(z_0)|$ of μ of $\mu\mu H$ process. Blue, red, and black histograms show the μ from $Z \rightarrow \mu^+\mu^-$, the μ from $\tau \rightarrow \mu\nu\nu$, and the hadrons from τ decay, respectively. Figure 12: The plot of E_{track} of μ of $\mu\mu H$ process. Blue, red, and black histograms show the μ from $Z \rightarrow \mu^+\mu^-$, the μ from $\tau \rightarrow \mu\nu\nu$, and the hadrons from τ decay, respectively.

We applied the energy recovery procedure to correct for bremsstrahlung and final state radiation. In order to reconstruct the original Z boson, we have to use both the charged particles and the radiated photons. To achieve this, we defined the cone as shown in Figure 13. The four-momenta of the neutral particles in the cone were combined with that of the lepton candidate. We defined the half-opening angle of the cone with $\cos\theta_{\text{cone}} = 0.999$ and applied the recovery procedure to the lepton candidates. The results are shown in Figures 14 and 15.

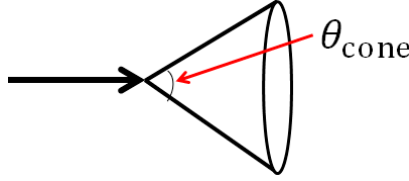


Figure 13: The definition of the cone. Black arrow shows the lepton candidate. θ_{cone} is the angle of the cone.

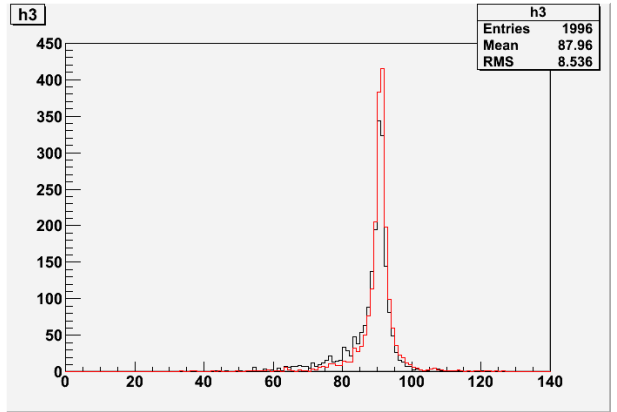
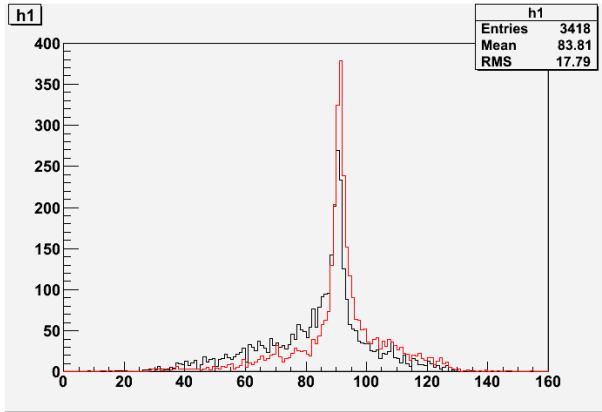


Figure 14: The results of recovery for $Z \rightarrow e^+e^-$ mode. The horizontal axis shows the $\mu^+\mu^-$ mode. The horizontal axis shows the M_Z . Black and red histograms show the results of without recovery and with recovery ($\cos\theta_{\text{cone}} = 0.999$), respectively. Figure 15: The results of recovery for $Z \rightarrow \mu^+\mu^-$ mode. The horizontal axis shows the $\mu^+\mu^-$ mode. The horizontal axis shows the M_Z . Black and red histograms show the results of without recovery and with recovery ($\cos\theta_{\text{cone}} = 0.999$), respectively.

After that, we applied the tau finder to the remaining objects to reconstruct tau leptons. First of all, the objects which already used at Z boson reconstruction were rejected from tau reconstruction analysis. Then we search the highest energy track from the remaining objects, and combine the neighboring particles (which satisfies the angle with respect to the highest energy track less than 1.0 radian) with the combined mass less than 2 GeV. We regarded the combined object as a tau candidate. Then repeat these processes until there are no charged particles.

After finishing the event reconstruction, we applied the cuts for selecting signal, rejecting background. Before optimizing the cuts, we applied the preselection as follows for $Z \rightarrow e^+e^-$ mode: number of e^+ and $e^- = 1$, number of τ^+ and $\tau^- = 1$, and for $Z \rightarrow \mu^+\mu^-$ mode: number of μ^+ and $\mu^- = 1$, number of τ^+ and $\tau^- = 1$.

We applied the following cuts for $Z \rightarrow e^+e^-$ mode: number of tracks ≤ 8 , $115 \text{ GeV} < E_{\text{vis}} < 230 \text{ GeV}$, $|\cos \theta_{\text{miss}}| < 0.99$, $81 \text{ GeV} < M_Z < 113 \text{ GeV}$, $\cos \theta_{e^-} < 0.92$, $\cos \theta_{e^+} > -0.92$, $E_{e^-} < 90 \text{ GeV}$, $E_{e^+} < 90 \text{ GeV}$, $\cos \theta_{\tau^+\tau^-} < -0.45$, $\cos \theta_{\tau^-} < 0.92$, $\cos \theta_{\tau^+} > -0.92$, and $116 \text{ GeV} < M_{\text{recoil}} < 142 \text{ GeV}$, where E_{vis} is the visible energy, θ_{miss} is the missing momentum angle with respect to beam axis, $\theta_{e^-(e^+)}$ is the $e^-(e^+)$ angle with respect to beam axis, $E_{e^-(e^+)}$ is the $e^-(e^+)$ energy, $\theta_{\tau^+\tau^-}$ is the angle between τ^+ and τ^- , $\theta_{\tau^-(\tau^+)}$ is the $\tau^-(\tau^+)$ angle with respect to beam axis, and M_{recoil} is the recoil mass, respectively. The histograms of all cut variables are shown in Figures 17 - 28 (page 11 - 12). Table 1 shows the cut statistics of this mode. After the cuts, the $Z \rightarrow e^+e^-$ signal events of 108.9 and background events of 76.0 remained. The statistical significance was calculated to be $S/\sqrt{S+B} = 108.9/\sqrt{108.9+76.0} = 8.0\sigma$.

We applied the following cuts for $Z \rightarrow \mu^+\mu^-$ mode: number of tracks ≤ 8 , $115 \text{ GeV} < E_{\text{vis}} < 235 \text{ GeV}$, $|\cos \theta_{\text{miss}}| < 0.98$, $72 \text{ GeV} < M_Z < 107 \text{ GeV}$, $E_{e^-} < 90 \text{ GeV}$, $E_{e^+} < 90 \text{ GeV}$, $\cos \theta_{\tau^+\tau^-} < -0.5$, and $118 \text{ GeV} < M_{\text{recoil}} < 143 \text{ GeV}$. The histograms of all cut variables are shown in Figures 29 - 36 (page 13 - 14). Table 2 shows the cut statistics of this mode. For the $Z \rightarrow \mu^+\mu^-$ mode case, 131.2 signal events and 91.2 background events were remained. The significance was $S/\sqrt{S+B} = 131.2/\sqrt{131.2+91.2} = 8.8\sigma$.

Table 1: The cut statistics of $Z \rightarrow e^+e^-$ mode.

	eeH $H \rightarrow \tau\tau$	$\mu\mu H$ $H \rightarrow \tau\tau$	$\tau\tau H$ $H \rightarrow \tau\tau$	ZH with no τ	$ee\tau\tau$	other 4 leptons	other SM bkg	signi.
No cut	228.3	211.1	214.6	7325	2.388×10^5	5.238×10^5	1.492×10^{10}	0.0019
preselection	171.3	0.155	1.532	47.05	1.338×10^4	3.215×10^4	1.023×10^7	0.053
# of tracks	169.4	0.155	1.532	41.56	1.316×10^4	3.205×10^4	1.009×10^7	0.053
E_{vis}	162.3	0.155	0.912	38.36	1.068×10^4	1.039×10^4	4.761×10^6	0.074
$\cos \theta_{\text{miss}}$	160.6	0.155	0.912	38.03	8719	1906	5.155×10^5	0.22
M_Z	148.0	0	0.017	29.09	2408	501.2	1.299×10^4	1.2
$\cos \theta_{e^-(e^+)}$	133.9	0	0.009	25.40	1067	101.5	729.7	3.0
$E_{e^-(e^+)}$	133.0	0	0.009	24.93	690.3	78.70	629.7	3.4
$\cos \theta_{\tau^+\tau^-}$	130.8	0	0	3.536	254.9	30.70	155.4	5.5
$\cos \theta_{\tau^-(\tau^+)}$	123.4	0	0	3.074	212.1	9.161	3.817	6.6
M_{recoil}	108.9	0	0	2.474	72.35	1.134	0.034	8.0

Table 2: The cut statistics of $Z \rightarrow \mu^+\mu^-$ mode.

	$\mu\mu H$ $H \rightarrow \tau\tau$	eeH $H \rightarrow \tau\tau$	$\tau\tau H$ $H \rightarrow \tau\tau$	ZH with no τ	$\mu\mu\tau\tau$	other 4 leptons	other SM bkg	signi.
No cut	211.1	228.3	214.6	7325	3513	7.591×10^6	1.492×10^{10}	0.0017
preselection	168.5	0	0.155	43.01	1698	7546	7732	1.3
# of tracks	167.4	0	0.155	39.65	1684	7537	7400	1.3
E_{vis}	162.9	0	0.155	37.40	1586	2285	3713	1.9
$\cos \theta_{\text{miss}}$	158.6	0	0.155	36.51	1386	227.5	55.48	3.7
M_Z	153.2	0	0	32.84	1038	55.28	42.54	4.2
$E_{e^-(e^+)}$	153.2	0	0	32.70	738.6	42.41	36.72	4.8
$\cos \theta_{\tau^+\tau^-}$	146.3	0	0	3.638	259.4	20.19	0.756	7.1
M_{recoil}	131.2	0	0	2.875	82.36	5.311	0.301	8.8

4.2 $Z \rightarrow q\bar{q}$ mode

In this mode, the tau pairs are reconstructed first, followed by the di-jet reconstruction of the Z decay.

At first in this mode, we applied the tau finder to all objects to reconstruct tau leptons. In this analysis, we search the highest energy track and combine the neighboring particles, which satisfy $\cos\theta_{\text{cone}} > 0.98$, with the combined mass less than 2 GeV. We regarded the combined object as a tau candidate. Then we applied the selection cuts as following: $E_{\text{tau candidate}} > 3$ GeV, $E_{\text{cone}} < 0.1E_{\text{tau candidate}}$ with $\cos\theta_{\text{cone}} = 0.9$, and rejecting 3-prong with neutral particles events. These selection cuts were tuned for minimizing misidentification of part of quark jets as tau jets. The survived tau candidate regarded as a tau jet. After the selection cuts, we applied the charge recovery to obtain better efficiency. The charged particles in tau jet which have the energy less than 2 GeV are detached one by one from smallest energy from the tau jet until satisfying the conditions as following: the charge of tau jet is $+1$ or -1 , and the number of track(s) in tau jet is 1 or 3. The tau jet after detaching is rejected if it does not satisfy the above conditions. After the selection cuts and detaching, we repeat the above processes until there are no charged particles which have the energy greater than 2 GeV.

After the tau reconstruction, we applied the collinear approximation [10] to reconstruct $M_{\tau^+\tau^-}$. In this approximation, we assumed that the visible decay products of tau and the neutrino(s) from tau is collinear, and the contribution of missing transverse momentum is only comes from the neutrino(s) of tau decay. The invariant mass of the tau pair with the collinear approximation shown in Figure 16.

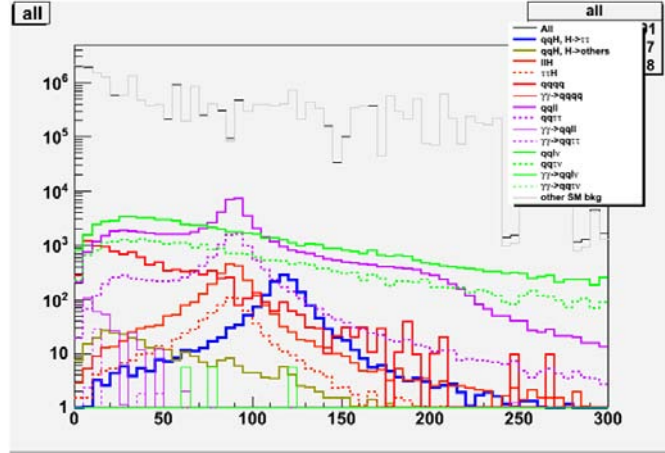


Figure 16: The plot of M_{colapp} in the unit of GeV, the invariant mass of di-tau with collinear approximation. Blue histogram shows the signal process $ZH \rightarrow qq\tau\tau$.

After that, we applied the Durham jet clustering method [11] with two jets for the remaining objects for the reconstruction of the Z boson.

After the tau and Z reconstruction, we applied the cuts to select signal process. Before optimizing cuts, we applied the preselection as follows: number of quark jets = 2, number of τ^+ and $\tau^- = 1$, number of tracks in $\tau \leq 3$, and the events which have the tracks in both $\tau = 3$ were rejected (double 3-prong cut). We applied the following cuts to reject the background: $9 \leq$ number of tracks < 50 , $110 \text{ GeV} < E_{\text{vis}} < 235 \text{ GeV}$, $|\cos\theta_{\text{miss}}| < 0.98$, $77 \text{ GeV} < M_Z < 135 \text{ GeV}$, $80 \text{ GeV} < E_Z < 135 \text{ GeV}$, $\cos\theta_{\tau^+\tau^-} < -0.5$, $\log_{10}|d_0/\sigma(d_0)|(\tau^+) + \log_{10}|d_0/\sigma(d_0)|(\tau^-) > -0.7$, $\log_{10}|z_0/\sigma(z_0)|(\tau^+) + \log_{10}|z_0/\sigma(z_0)|(\tau^-) > -0.1$, $M_{\tau^+\tau^-} < 115 \text{ GeV}$, $E_{\tau^+\tau^-} < 125 \text{ GeV}$, $100 \text{ GeV} < M_{\text{colapp}} < 170 \text{ GeV}$, $100 \text{ GeV} < E_{\text{colapp}} < 280 \text{ GeV}$, and $112 \text{ GeV} < M_{\text{recoil}} < 160 \text{ GeV}$, where $M_{\tau^+\tau^-}$ and $E_{\tau^+\tau^-}$ is the invariant mass and energy without using collinear approximation, M_{colapp} and E_{colapp} is the invariant mass and energy with collinear approximation, respec-

tively. The histograms of all cut variables are shown in Figures 37 - 49 (page 14 - 16). Table 3 shows the cut statistics of this mode. After the cuts, the signal events and background events were remained 1026 and 554.4. The statistical significance of $Z \rightarrow q\bar{q}$ mode is calculated to be $S/\sqrt{S+B} = 1026/\sqrt{1026+554.4} = 25.8\sigma$.

Table 3: The cut statistics of $Z \rightarrow q\bar{q}$ mode.

	qqH $H \rightarrow \tau\tau$	ZH with no τ	lH	$\tau\tau H$	$qqqq$	$qqll$	$qq\tau\tau$	$qq\nu\nu$	$qq\tau\nu$	other SM bkg	signi.
No cut	4233	4.829×10^4	5377	2596	4.038×10^6	3.563×10^5	4.169×10^4	2.788×10^6	1.326×10^6	1.494×10^{10}	0.035
preselection	1647	578.8	2761	765.4	1.230×10^4	6.378×10^4	1.161×10^4	1.249×10^5	4.948×10^4	2.570×10^7	0.32
# of tracks	1644	549.8	2680	765.4	1.230×10^4	6.059×10^4	1.146×10^4	1.214×10^5	4.806×10^4	5.190×10^5	1.9
E_{vis}	1607	492.3	1015	744.2	4443	2.106×10^4	1.107×10^4	1.192×10^5	4.693×10^4	2.383×10^5	2.4
$\cos\theta_{\text{miss}}$	1572	474.7	860.5	725.1	2127	8315	1.021×10^4	1.171×10^5	4.415×10^4	5939	3.6
M_Z	1440	376.1	791.3	682.8	778.6	4987	8674	8189	3288	997.3	8.3
E_Z	1429	352.0	782.7	528.7	505.0	4797	7857	7703	3061	609.9	8.6
$\cos\theta_{\tau^+\tau^-}$	1386	46.28	442.2	255.6	191.4	1468	2001	2831	1154	475.6	13.7
$d_{0\text{sig}}$	1338	30.29	235.1	244.3	131.4	854.9	1928	1786	1044	248.1	15.1
$z_{0\text{sig}}$	1287	19.54	105.0	234.7	81.77	408.2	1845	909.9	883.4	244.6	16.6
$M_{\tau^+\tau^-}$	1286	19.39	103.2	234.7	72.05	349.1	1837	883.5	883.4	243.9	16.7
$E_{\tau^+\tau^-}$	1282	19.39	103.0	234.7	72.05	324.7	1836	873.2	883.4	243.9	16.7
M_{colapp}	1065	3.074	18.76	47.94	10.28	72.83	616.9	150.8	137.0	0.746	23.1
E_{colapp}	1062	2.454	18.01	46.72	10.28	71.27	612.1	93.05	93.52	0.454	23.7
M_{recoil}	1026	2.144	14.54	21.24	9.938	57.07	366.3	39.64	43.31	0.161	25.8

5 Summary

We evaluated the measurement accuracy of the branching ratio of the $H \rightarrow \tau^+\tau^-$ mode at $\sqrt{s} = 250$ GeV at the ILC with ILD_00 detector model. We assumed $M_H = 120$ GeV, $\text{Br}(H \rightarrow \tau^+\tau^-) = 8.0\%$, $\int L dt = 250 \text{ fb}^{-1}$, and the polarization $P(e^+, e^-) = (+0.3, -0.8)$. The obtained values were summarized in Table 4.

Table 4: The analysis results of $\sqrt{s} = 250$ GeV.

mode	$Z \rightarrow e^+e^-$	$Z \rightarrow \mu^+\mu^-$	$Z \rightarrow q\bar{q}$
significance	8.0σ	8.8σ	25.8σ

From these results, the combined significance was calculated to be $\sqrt{8.0^2 + 8.8^2 + 25.8^2} = 28.4\sigma$. Therefore, the measurement accuracy $\Delta(\sigma \cdot \text{Br})/(\sigma \cdot \text{Br})$ was calculated to be $\Delta(\sigma \cdot \text{Br})/(\sigma \cdot \text{Br}) = 1/28.4 = 3.5\%$.

The results are extrapolated to the case of $M_H = 125$ GeV by scaling the signal yields by the $e^+e^- \rightarrow ZH$ cross section and the branching ratio $\text{Br}(H \rightarrow \tau^+\tau^-) \rightarrow 6.32\%$ [9]. We assumed that the selection efficiencies the same. The results are summarized in Table 5.

Table 5: The results of the extrapolation to $M_H = 125$ GeV.

$Z \rightarrow e^+e^-$	$Z \rightarrow \mu^+\mu^-$	$Z \rightarrow q\bar{q}$	Combined	$\frac{\Delta(\sigma \cdot \text{Br})}{\sigma \cdot \text{Br}}$
6.8σ	7.4σ	21.9σ	24.1σ	4.2 %

A Monte-Carlo Samples

Table 6: Monte-Carlo information which used in this analysis. From the left line, the process ID, process, beam polarization (ep for positrons, em for electrons), cross section in the unit of fb, number of Monte-Carlo events, integrated luminosity in the unit of fb⁻¹, are shown. This list continues to Table 7.

21564 aa_bb ep+0,0em+0,0 960,971 95 0,099899	23594 aa_e2e3dd ep+0,0em+0,0 0,073276 10 136,47	21664 ae1_e1e1e1 ep-1,0em+0,0 7275,46 7275 0,999937
21565 aa_bb ep+0,0em+0,0 5218,47 521 0,0998377	23595 aa_e2e3dd ep+0,0em+0,0 0,096363 10 103,143	21665 ae1_e1e1e1 ep-1,0em+0,0 44860,5 44060 0,982156
21566 aa_bb ep+0,0em+0,0 5205,84 520 0,0998878	23596 aa_e2e3dd ep+0,0em+0,0 0,097375 10 102,696	21666 ae1_e1e1e1 ep+1,0em+0,0 7327,35 7327 0,999952
21567 aa_bb ep+0,0em+0,0 4768,41 476 0,0998236	23597 aa_e2e3dd ep+0,0em+0,0 0,019565 10 511,117	21667 ae1_e1e1e1 ep+1,0em+0,0 44910,9 44910 0,999998
21560 aa_cc ep+0,0em+0,0 25826,9 2582 0,0999733	23581 aa_e2e3e3e3 ep+0,0em+0,0 2,98239 10 3,35302	21668 ae1_e1e2e2 ep-1,0em+0,0 7859,36 7859 0,999954
21561 aa_cc ep+0,0em+0,0 158487 15848 0,0999956	23581 aa_e2e3e3e3 ep+0,0em+0,0 5,81718 10 1,71905	21669 ae1_e1e2e2 ep+1,0em+0,0 53497,7 52297 0,977556
21562 aa_cc ep+0,0em+0,0 158287 15828 0,0999956	23582 aa_e2e3e3e3 ep+0,0em+0,0 5,83263 10 1,71449	21670 ae1_e1e2e2 ep+1,0em+0,0 7874,12 6874 0,872986
21563 aa_cc ep+0,0em+0,0 208135 20813 0,0999976	23583 aa_e2e3e3e3 ep+0,0em+0,0 2,0741 10 4,82137	21671 ae1_e1e2e2 ep+1,0em+0,0 53695,4 52695 0,981369
23532 aa_ccbb ep+0,0em+0,0 0,010556 10 947,329	23588 aa_e2e3ss ep+0,0em+0,0 0,073357 10 136,32	21672 ae1_e1e3e3 ep-1,0em+0,0 13442,9 13442 0,999933
23533 aa_ccbb ep+0,0em+0,0 0,004464 10 2240,14	23589 aa_e2e3ss ep+0,0em+0,0 0,03712 10 102,965	21673 ae1_e1e3e3 ep+1,0em+0,0 96101,5 94701 0,985427
23534 aa_ccbb ep+0,0em+0,0 0,004538 10 2203,61	23590 aa_e2e3ss ep+0,0em+0,0 0,037361 10 102,965	21674 ae1_e1e3e3 ep+1,0em+0,0 13483 13283 0,985187
23432 aa_cccc ep+0,0em+0,0 0,038923 10 256,918	23591 aa_e2e3ss ep+0,0em+0,0 0,019638 10 509,217	21675 ae1_e1e3e3 ep+1,0em+0,0 96257,6 94057 0,977138
23433 aa_cccc ep+0,0em+0,0 0,012718 10 786,287	23312 aa_n1e1du ep+0,0em+0,0 0,225273 10 44,3906	21648 ae1_e1n2n2 ep-1,0em+0,0 33,3463 33 0,989615
23434 aa_cccc ep+0,0em+0,0 0,01308 10 764,526	23300 aa_n1e1e1n1 ep+0,0em+0,0 0,076337 10 130,998	21649 ae1_e1n2n2 ep-1,0em+0,0 14,4871 14 0,966377
23528 aa_ccdd ep+0,0em+0,0 0,008955 10 1116,69	23304 aa_n1e1e2n2 ep+0,0em+0,0 0,073443 10 136,16	21650 ae1_e1n2n2 ep+1,0em+0,0 52,0695 52 0,998665
23529 aa_ccdd ep+0,0em+0,0 0,002019 10 4952,95	23308 aa_n1e1e3n3 ep+0,0em+0,0 0,073757 10 135,58	21651 ae1_e1n2n2 ep+1,0em+0,0 22,6358 22 0,971912
23530 aa_ccdd ep+0,0em+0,0 0,002071 10 4828,59	23316 aa_n1e1sc ep+0,0em+0,0 0,225277 10 44,3898	21652 ae1_e1n3n3 ep-1,0em+0,0 33,3836 33 0,988509
23516 aa_cce1e1 ep+0,0em+0,0 0,475002 10 21,0525	23436 aa_n1n1e2e2 ep+0,0em+0,0 0,003527 10 2835,27	21653 ae1_e1n3n3 ep-1,0em+0,0 14,5035 14 0,965284
23517 aa_cce1e1 ep+0,0em+0,0 0,574236 10 17,4144	23440 aa_n1n1e3e3 ep+0,0em+0,0 0,003793 10 2636,44	21654 ae1_e1n3n3 ep+1,0em+0,0 52,1148 52 0,997797
23518 aa_cce1e1 ep+0,0em+0,0 0,578967 10 17,2395	23400 aa_n1n1uu ep+0,0em+0,0 0,002035 10 4914	21655 ae1_e1n3n3 ep+1,0em+0,0 22,6013 22 0,973395
23519 aa_cce1e1 ep+0,0em+0,0 0,095892 10 104,116	23332 aa_n2e2du ep+0,0em+0,0 0,225253 10 44,3945	21680 ae1_e1ss ep-1,0em+0,0 263,497 263 0,980414
23520 aa_cce2e2 ep+0,0em+0,0 0,473337 10 21,0989	23320 aa_n2e2e1n1 ep+0,0em+0,0 0,073442 10 136,162	21681 ae1_e1ss ep-1,0em+0,0 1205,28 1205 0,999768
23521 aa_cce2e2 ep+0,0em+0,0 0,578749 10 17,2787	23324 aa_n2e2e2n2 ep+0,0em+0,0 0,076285 10 131,087	21682 ae1_e1ss ep+1,0em+0,0 304,802 304 0,997369
23522 aa_cce2e2 ep+0,0em+0,0 0,581645 10 17,1926	23328 aa_n2e3e3n3 ep+0,0em+0,0 0,073621 10 135,831	21683 ae1_e1ss ep+1,0em+0,0 1203,83 1203 0,999311
23523 aa_cce2e2 ep+0,0em+0,0 0,095404 10 104,817	23412 aa_n2n2cc ep+0,0em+0,0 0,002028 10 4930,97	21656 ae1_e1uu ep-1,0em+0,0 2630,42 2630 0,999984
23524 aa_cce3e3 ep+0,0em+0,0 0,089322 10 12,356	23456 aa_n2n2e1e1 ep+0,0em+0,0 0,003538 10 2826,46	21657 ae1_e1uu ep+1,0em+0,0 14117,2 14117 0,999986
23525 aa_cce3e3 ep+0,0em+0,0 0,17006 10 9,34527	23460 aa_n2n2e3e3 ep+0,0em+0,0 0,003797 10 2633,66	21658 ae1_e1uu ep+1,0em+0,0 2696,52 2696 0,999807
23526 aa_cce3e3 ep+0,0em+0,0 0,107435 10 9,30795	23352 aa_n3e3du ep+0,0em+0,0 0,22566 10 44,3145	21659 ae1_e1uu ep+1,0em+0,0 14189,1 14189 0,999993
23527 aa_cce3e3 ep+0,0em+0,0 0,198611 10 50,3497	23340 aa_n3e3e1n1 ep+0,0em+0,0 0,073677 10 135,728	21189 bb ep+1,0em-1,0 47956,1 95600 0,96567
23332 aa_cdsu ep+0,0em+0,0 0,844164 10 15,524	23344 aa_n3e3e2n2 ep+0,0em+0,0 0,073519 10 136,019	21190 bb ep+1,0em-1,0 27566 99800 3,5204
23333 aa_cdsu ep+0,0em+0,0 0,001171 10 8539,71	23348 aa_n3e3e3n3 ep+0,0em+0,0 0,077072 10 129,749	21185 cc ep+1,0em-1,0 44745,7 95600 2,22591
23334 aa_cdsu ep+0,0em+0,0 0,001492 10 6747,64	23356 aa_n3e3sc ep+0,0em+0,0 0,225636 10 44,3192	21186 cc ep+1,0em+1,0 28600 2,24338
23380 aa_cse1n1 ep+0,0em+0,0 0,225189 10 44,4071	23420 aa_n3n3cc ep+0,0em+0,0 0,002032 10 4921,26	21449 ccb ep+1,0em-1,0 123,789 99000 739,748
23384 aa_cse2n2 ep+0,0em+0,0 0,225196 10 44,4058	23476 aa_n3n3e1e1 ep+0,0em+0,0 0,003529 10 2833,66	21450 ccb ep+1,0em+1,0 56,6712 55671 982,351
23388 aa_cse3n3 ep+0,0em+0,0 0,225468 10 44,3522	23480 aa_n3n3e2e2 ep+0,0em+0,0 0,003535 10 2828,85	21349 cccc ep+1,0em-1,0 54,3735 53774 988,974
23396 aa_cssc ep+0,0em+0,0 0,850312 10 15,3772	23416 aa_n3n3uu ep+0,0em+0,0 0,002035 10 4914	21350 cccc ep+1,0em+1,0 26,3297 26330 1000,01
23397 aa_cssc ep+0,0em+0,0 0,002852 10 3506,31	21556 aa_ss ep+0,0em+0,0 1612,02 161 0,0998747	24477 cccbb ep+1,0em-1,0 0,003422 10000 2,92227e+06
23398 aa_cssc ep+0,0em+0,0 0,003221 10 3104,63	21557 aa_ss ep+0,0em+0,0 9919,95 992 0,100001	24478 cccbb ep+1,0em+1,0 0,001756 10000 5,69476e+06
21552 aa_dd ep+0,0em+0,0 1611,35 161 0,0999162	21598 aa_ss ep+0,0em+0,0 9874,29 987 0,0999566	21445 codd ep+1,0em-1,0 120,779 100000 827,958
21553 aa_dd ep+0,0em+0,0 9902,35 990 0,0999763	21599 aa_ss ep+0,0em+0,0 13010,8 1301 0,0999939	21446 codd ep+1,0em+1,0 55,1663 54566 989,118
21554 aa_dd ep+0,0em+0,0 9913,25 991 0,0999672	23372 aa_uddu ep+0,0em+0,0 0,550353 10 15,3763	24773 coddbb ep+1,0em-1,0 0,004519 10000 2,21288e+06
21555 aa_dd ep+0,0em+0,0 12993,6 1299 0,0999723	23373 aa_uddu ep+0,0em+0,0 0,00265 10 3490,4	24774 coddbb ep+1,0em+1,0 0,002267 10000 4,4112e+06
21536 aa_e1e1 ep+0,0em+0,0 75476,4 7547 0,0998928	23374 aa_uddu ep+0,0em+0,0 0,003197 10 3127,93	21432 cce1e1 ep+1,0em-1,0 448,721 96400 214,833
21537 aa_e1e1 ep+0,0em+0,0 551033 107786 0,195607	23360 aa_ude1n1 ep+0,0em+0,0 0,225336 10 44,3782	21433 cce1e1 ep+1,0em+1,0 506,805 98000 135,368
21539 aa_e1e1 ep+0,0em+0,0 1,42431e+06 137431 0,0964895	23364 aa_ude2n2 ep+0,0em+0,0 0,225701 10 44,3064	21434 cce1e1 ep+1,0em+1,0 464,393 96800 206,449
23556 aa_e1e1bb ep+0,0em+0,0 0,031025 10 322,321	23368 aa_ude3n3 ep+0,0em+0,0 0,225594 10 44,3274	21435 cce1e1 ep+1,0em+1,0 448,339 99200 221,251
23557 aa_e1e1bb ep+0,0em+0,0 0,002870 10 348,371	23376 aa_udsc ep+0,0em+0,0 0,643852 10 15,5315	21437 cce2e2 ep+1,0em-1,0 53,1534 52935 996,229
23558 aa_e1e1bb ep+0,0em+0,0 0,002884 10 346,741	23377 aa_udsc ep+0,0em+0,0 0,001171 10 8539,71	21438 cce2e2 ep+1,0em+1,0 29,3345 29335 1000,02
23559 aa_e1e1bb ep+0,0em+0,0 0,004257 10 2349,07	23378 aa_udsc ep+0,0em+0,0 0,001484 10 6738,54	21441 cce3e3 ep+1,0em-1,0 52,7484 52548 996,201
23549 aa_e1e1dd ep+0,0em+0,0 0,050209 10 199,167	21548 aa_uu ep+0,0em+0,0 25709,9 2570 0,0999615	21442 cce3e3 ep+1,0em+1,0 29,1511 29151 999,997
23550 aa_e1e1dd ep+0,0em+0,0 0,050399 10 198,417	21549 aa_uu ep+0,0em+0,0 158254 21658 0,200045	20609 cch ep+1,0em-1,0 59,231 59321 1000,01
23551 aa_e1e1dd ep+0,0em+0,0 0,008768 10 1140,51	21581 aa_uu ep+0,0em+0,0 208230 20823 0,1	20610 cch ep+1,0em+1,0 37,8798 37880 1000,01
23536 aa_e1e1e1 ep+0,0em+0,0 0,652331 10 15,0982	23512 aa_uubb ep+0,0em+0,0 0,010578 10 945,358	21309 csdu ep+1,0em-1,0 59,3544 59534 993,319
23537 aa_e1e1e1 ep+0,0em+0,0 0,371629 10 10,232	23513 aa_uubb ep+0,0em+0,0 0,004456 10 2244,17	21310 csdu ep+1,0em+1,0 2465,5 32400 37,4688
23538 aa_e1e1e1 ep+0,0em+0,0 0,050928 10 199,889	23514 aa_uubb ep+0,0em+0,0 0,004531 10 2207,02	21298 cse1n1 ep+1,0em-1,0 20,9278 11528 550,846
23539 aa_e1e1e1 ep+0,0em+0,0 0,235859 10 42,2194	23429 aa_uucc ep+0,0em+0,0 0,073277 10 127,751	21299 cse1n1 ep+1,0em+1,0 86,2613 80061 928,122
23540 aa_e1e2e2 ep+0,0em+0,0 1,68665 10 5,92891	23513 aa_uucc ep+0,0em+0,0 0,027362 10 365,47	21301 cse2n2 ep+1,0em-1,0 2268,39 100000 44,0841
23541 aa_e1e2e2 ep+0,0em+0,0 0,371425 20 6,51158	23430 aa_uucc ep+0,0em+0,0 0,027931 10 358,025	21302 cse2n2 ep+1,0em+1,0 20,8866 20887 1000,02
23543 aa_e1e2e2 ep+0,0em+0,0 0,371522 10 10,2931	23496 aa_uue1e1 ep+0,0em+0,0 0,476112 10 21,0035	21305 cse3n3 ep+1,0em-1,0 2266,29 100000 44,125
23544 aa_e1e2e3 ep+0,0em+0,0 0,314724 30 3,17739	23498 aa_uue1e1 ep+0,0em+0,0 0,58118 10 17,2064	21306 cse3n3 ep+1,0em+1,0 20,8669 20867 1000,01
23545 aa_e1e2e3 ep+0,0em+0,0 0,6 49529 10 1,53958	23499 aa_uue1e1 ep+0,0em+0,0 0,095015 10 105,247	21313 cssc ep+1,0em-1,0 6638,5 99900 15,0335
23546 aa_e1e2e3 ep+0,0em+0,0 0,6 52147 10 1,5334	23500 aa_uue2e2 ep+0,0em+0,0 0,474597 10 21,0705	21314 cssc ep+1,0em+1,0 112,648 79200 703,075
23547 aa_e1e2e3 ep+0,0em+0,0 2,55979 10 3,90657	23502 aa_uue2e2 ep+0,0em+0,0 0,576787 10 17,5374	21181 dd ep+1,0em-1,0 48065,6 100000 2,08049
23552 aa_e1e1ss ep+0,0em+0,0 0,444906 10 222,887	23503 aa_uue2e2 ep+0,0em+0,0 0,095267 10 104,968	21182 dd ep+1,0em+1,0 28936,9 99200 3,55319
23553 aa_e1e1ss ep+0,0em+0,0 0,050928 10 199,889	23504 aa_uue3e3 ep+0,0em+0,0 0,808463 10 12,3691	21522 ddb ep+1,0em-1,0 58,9095 58909 999,992
23554 aa_e1e1ss ep+0,0em+0,0 0,050343 10 198,637	23505 aa_uue3e3 ep+0,0em+0,0 1,07061 10 3,54047	21513 dddd ep+1,0em-1,0 67,066 66666 994,036
23555 aa_e1e1ss ep+0,0em+0,0 0,008754 10 1142,33	23506 aa_uue3e3 ep+0,0em+0,0 0,107551 10 9,29791	21514 dddd ep+1,0em+1,0 28,8606 24661 854,487
21540 aa_e2e2 ep+0,0em+0,0 75532,1 7553 0,0999972	23507 aa_uue3e3 ep+0,0em+0,0 0,199332 10 50,1706	24973 ddddbb ep+1,0em-1,0 0,001092 10000 9,15751e+06
21541 aa_e2e2 ep+0,0em+0,0 550664 55066 0,0999993	23508 aa_uuss ep+0,0em+0,0 0,00896 10 1115,32	20625 ddh ep+1,0em-1,0 75,8898 75890 1000,01
21542 aa_e2e2 ep+0,0em+0,0 551685 55168 0,0999991	23509 aa_uuss ep+0,0em+0,0 0,001939 10 5002,5	20626 ddh ep+1,0em+1,0 48,5522 48552 999,996
21543 aa_e2e2 ep+0,0em+0,0 1,42387e+06 141987 0,0997191	23510 aa_uuss ep+0,0em+0,0 0,002084 10 4798,46	21517 dsss ep+1,0em-1,0 134,545 68800 489,056
23576 aa_e2e2bb ep+0,0em+0,0 0,031069 10 321,864	23424 aa_uuuu ep+0,0em+0,0 0,03894 10 256,805	21518 dsss ep+1,0em+1,0 57,7479 51748 896,102
23577 aa_e2e2bb ep+0,0em+0,0 0,028705 10 348,371	23425 aa_uuuu ep+0,0em+0,0 0,012785 10 782,167	24981 dssbbb ep+1,0em-1,0 0,002137 10000 4,55166e+06
23578 aa_e2e2bb ep+0,0em+0,0 0,028893 10 346,105	23426 aa_uuuu ep+0,0em+0,0 0,013116 10 762,428	24982 dssbbb ep+1,0em+1,0 0,001108 10000 5,02527e+06
23579 aa_e2e2bb ep+0,0em+0,0 0,004264 10 2345,22	21101 aa ep+1,0em-1,0 43250,8 241254 4,89648	21116 e1a_e1a ep+0,0em-1,0 372192 18610 0,0500011
23580 aa_e2e2dd ep+0,0em+0,0 0,044878 10 222,826	21102 aa ep+1,0em+1,0 43267,2 237936 4,8995	21117 e1a_e1a ep+0,0em-1,0 5,39497e+06 263148 0,0498887
23589 aa_e2e2dd ep+0,0em+0,0 0,050182 10 193,275	21105 aaa ep+1,0em-1,0 5300,06 25500 4,98994	21118 e1a_e1a ep+0,0em+1,0 372426 18621 0,0499992
23570 aa_e2e2dd ep+0,0em+0,0 0,050545 10 197,844	21106 aaa ep+1,0em+1,0 5298,17 26091 4,92453	21119 e1a_e1a ep+0,0em+1,0 5,39207e+06 267003 0,0495177
23571 aa_e2e2dd ep+0,0em+0,0 0,008769 10 1140,38	21109 aaaa ep+1,0em-1,0 324,752 1624 5,00074	21624 e1a_e1bb ep+0,0em-1,0 235,778 235 0,9967
23560 aa_e2e2e2e2 ep+0,0em+0,0 0,653421 10 15,0734	21110 aaaa ep+1,0em+1,0 323,783 1619 5,00026	21625 e1a_e1bb ep+0,0em+1,0 729,568 729 0,999221
23561 aa_e2e2e2e2 ep+0,0em+0,0 0,379309 10 10,2765	21120 ae1_e1a ep+1,0em+0,0 0,371863 18393 0,0494618	21626 e1a_e1bb ep+0,0em+1,0 196,862 196 0,999621
23562 aa_e2e2e2e2 ep+0,0em+0,0 0,375528 10 10,2509	21121 ae1_e1a ep+1,0em+0,0 5,36047e+06 266224 0,0496643	21627 e1a_e1bb ep+0,0em+1,0 742,713 742 0,99904
23563 aa_e2e2e2e2 ep+0,0em+0,0 0,236644 10 42,2576	21122 ae1_e1a ep+1,0em+0,0 372274 18614 0,0500008	
23564 aa_e2e2e3e3 ep+0,0em+0,0 0,315328 10 3,1713	21123 ae1_e1a ep+1,0em+0,0 5,36372e+06 266186 0,0496271	
23565 aa_e2e2e3e3 ep+0,0em+0,0 0,6 51091 20 3,07177	21184 ae1_e1bb ep+1,0em+0,0 0,196,883 196 0,995515	
23567 aa_e2e2e3e3 ep+0,0em+0,0 2,55982 10 3,93514	21695 ae1_e1bb ep+1,0em+0,0 741,99 742 1,00001	
23572 aa_e2e2ss ep+0,0em+0,0 0,044853 10 222,891	21696 ae1_e1bb ep+1,0em+0,0 235,7 235 0,99703	
23573 aa_e2e2ss ep+0,0em+0,0 0,0		

Table 7: Monte-Carlo information which used in this analysis. From the left line, the process ID, process, beam polarization (ep for positrons, em for electrons), cross section in the unit of fb, number of Monte-Carlo events, integrated luminosity in the unit of fb⁻¹, are shown. This list is series of Table 6.

21600	e1a_elcc	ep+0.0em-1.0	2632.03	2000	0.742934
21601	e1a_elcc	ep+0.0em-1.0	14238.4	14238	0.999972
21602	e1a_elcc	ep+0.0em+1.0	2630.76	2630	0.999711
21603	e1a_elcc	ep+0.0em+1.0	14172	14172	1
21616	e1a_eldd	ep+0.0em-1.0	305.228	305	0.999253
21617	e1a_eldd	ep+0.0em-1.0	1207.73	1207	0.999396
21618	e1a_eldd	ep+0.0em+1.0	263.602	263	0.997716
21619	e1a_eldd	ep+0.0em+1.0	1210.08	1210	0.999934
21604	e1a_e1e1e1	ep+0.0em-1.0	7311.26	7311	0.999964
21605	e1a_e1e1e1	ep+0.0em-1.0	45047.7	43047	0.955587
21606	e1a_e1e1e1	ep+0.0em+1.0	7282.56	7282	0.999923
21607	e1a_e1e1e1	ep+0.0em+1.0	44999.4	43999	0.977769
21608	e1a_e1e2e2	ep+0.0em-1.0	7880.39	7880	0.99995
21609	e1a_e1e2e2	ep+0.0em-1.0	53812.4	53412	0.992559
21610	e1a_e1e2e2	ep+0.0em+1.0	7869.66	7869	0.999916
21611	e1a_e1e2e2	ep+0.0em+1.0	53765.8	50565	0.940468
21612	e1a_e1e3e3	ep+0.0em-1.0	13471.3	13471	0.999933
21613	e1a_e1e3e3	ep+0.0em-1.0	96603.4	94803	0.981363
21614	e1a_e1e3e3	ep+0.0em+1.0	13459.7	13459	0.999948
21615	e1a_e1e3e3	ep+0.0em+1.0	96607	95607	0.989649
21588	e1a_e1n2n2	ep+0.0em-1.0	52.0727	52	0.998604
21589	e1a_e1n2n2	ep+0.0em-1.0	21.8282	21	0.962058
21590	e1a_e1n2n2	ep+0.0em+1.0	33.307	33	0.990783
21591	e1a_e1n2n2	ep+0.0em+1.0	13.982	14	1.00129
21592	e1a_e1n3n3	ep+0.0em-1.0	52.0473	52	0.99908
21593	e1a_e1n3n3	ep+0.0em-1.0	21.8319	21	0.961895
21594	e1a_e1n3n3	ep+0.0em+1.0	33.3573	33	0.989289
21595	e1a_e1n3n3	ep+0.0em+1.0	13.9806	14	1.00139
21620	e1a_elss	ep+0.0em-1.0	305.28	305	0.999083
21621	e1a_elss	ep+0.0em-1.0	1203.61	1203	0.999493
21622	e1a_elss	ep+0.0em+1.0	263.322	263	0.998777
21623	e1a_elss	ep+0.0em+1.0	1210.02	1210	0.999983
21596	e1a_eluu	ep+0.0em-1.0	2697.07	2697	0.999974
21597	e1a_eluu	ep+0.0em-1.0	14270.7	14270	0.999951
21598	e1a_eluu	ep+0.0em+1.0	2631.22	2631	0.999916
21599	e1a_eluu	ep+0.0em+1.0	14186.3	14186	0.999979
21168	e1e1	ep-1.0em-1.0	1.72542e+07	25000	0.00144892
21169	e1e1	ep-1.0em+1.0	1.73374e+07	22500	0.00129777
21170	e1e1	ep+1.0em-1.0	1.72346e+07	24500	0.00141663
21171	e1e1	ep+1.0em+1.0	1.72517e+07	25000	0.00144913
21472	e1e1bb	ep-1.0em-1.0	57.2207	57221	1000.01
21473	e1e1bb	ep-1.0em-1.0	106.063	100000	942.636
21474	e1e1bb	ep-1.0em+1.0	58.9777	58978	1000.01
21475	e1e1bb	ep-1.0em+1.0	57.3099	57310	1000.01
21464	e1e1dd	ep-1.0em-1.0	73.3521	72532	989.098
21465	e1e1dd	ep-1.0em-1.0	123.983	100000	806.562
21466	e1e1dd	ep-1.0em+1.0	85.3261	84126	985.935
21467	e1e1dd	ep-1.0em+1.0	73.442	73442	1000
21452	e1e1e1e1	ep-1.0em-1.0	942.464	92200	97.8287
21453	e1e1e1e1	ep-1.0em-1.0	995.595	91400	91.8044
21454	e1e1e1e1	ep-1.0em+1.0	982.404	97400	99.1445
21455	e1e1e1e1	ep-1.0em+1.0	943.694	97800	103.635
21456	e1e1e2e2	ep-1.0em-1.0	1073.64	100000	93.1411
21457	e1e1e2e2	ep-1.0em-1.0	1106.71	99800	90.1772
21458	e1e1e2e2	ep-1.0em+1.0	1088.6	100000	91.8611
21459	e1e1e2e2	ep-1.0em+1.0	1088.97	99000	92.6125
21460	e1e1e3e3	ep-1.0em-1.0	941.685	98800	104.918
21461	e1e1e3e3	ep-1.0em-1.0	965.145	97800	101.332
21462	e1e1e3e3	ep-1.0em+1.0	948.774	99000	104.345
21463	e1e1e3e3	ep-1.0em+1.0	942.984	98200	104.138
20612	e1e1h	ep-1.0em-1.0	0.644995	10000	15504
20613	e1e1h	ep+1.0em-1.0	17.8919	17892	1000.01
20614	e1e1h	ep+1.0em+1.0	11.2894	11289	999.965
20615	e1e1h	ep+1.0em+1.0	0.645477	10000	15492.4
21468	e1e1ss	ep-1.0em-1.0	73.2531	73253	999.999
21469	e1e1ss	ep+1.0em-1.0	123.972	100000	806.634
21470	e1e1ss	ep-1.0em+1.0	85.4529	85500	767.674
21471	e1e1ss	ep+1.0em+1.0	73.152	71752	980.862
21173	e2e2	ep+1.0em-1.0	17077.6	99000	5.79707
21174	e2e2	ep-1.0em+1.0	12859.5	99400	7.72963
21493	e2e2bb	ep+1.0em-1.0	56.5071	56307	996.459
21494	e2e2bb	ep-1.0em+1.0	29.5793	28779	972.944
21485	e2e2dd	ep+1.0em-1.0	57.5377	57538	1000.01
21486	e2e2dd	ep-1.0em+1.0	30.2016	30202	1000.01
21477	e2e2e2e2	ep+1.0em-1.0	11.4311	11431	999.991
21478	e2e2e2e2	ep-1.0em+1.0	7.23464	100000	1382.24
21481	e2e2e3e3	ep+1.0em-1.0	23.1405	23140	999.978
21482	e2e2e3e3	ep-1.0em+1.0	14.6585	14658	999.966
20617	e2e2h	ep+1.0em-1.0	17.126	17126	1000
20618	e2e2h	ep-1.0em+1.0	10.9671	10967	999.991
21489	e2e2ss	ep+1.0em-1.0	57.6073	57607	999.995
21490	e2e2ss	ep-1.0em+1.0	30.1803	29980	993.363
21177	e3e3	ep+1.0em-1.0	17102.4	98800	5.77697
21178	e3e3	ep-1.0em+1.0	12852.9	99800	7.76478
21509	e3e3bb	ep+1.0em-1.0	56.1355	55535	989.303
21510	e3e3bb	ep-1.0em+1.0	29.4194	29219	993.188
21501	e3e3dd	ep+1.0em-1.0	57.2295	56830	993.015
21502	e3e3dd	ep-1.0em+1.0	30.0379	29838	993.345
21497	e3e3e3e3	ep+1.0em-1.0	11.4274	11427	999.965
21498	e3e3e3e3	ep-1.0em+1.0	7.21497	9800	1358.29
20621	e3e3h	ep+1.0em-1.0	17.0988	17099	1000.01
20622	e3e3h	ep-1.0em+1.0	10.9435	10944	1000.05
21505	e3e3ss	ep+1.0em-1.0	57.3548	57155	996.516
21506	e3e3ss	ep-1.0em+1.0	30.0052	30050	999.993
21228	n1e1du	ep-1.0em-1.0	86.3492	86349	999.998
21229	n1e1du	ep+1.0em-1.0	2467.16	100000	40.5324
21230	n1e1du	ep-1.0em+1.0	20.8701	20870	999.995
21216	n1e1e1n1	ep-1.0em-1.0	43.5841	43384	995.409
21217	n1e1e1n1	ep+1.0em-1.0	939.099	98800	105.207
21218	n1e1e1n1	ep-1.0em+1.0	27.4575	26898	978.166
21219	n1e1e1n1	ep+1.0em+1.0	43.6248	43625	1000
21220	n1e1e2n2	ep-1.0em-1.0	28.824	28424	986.123
21221	n1e1e2n2	ep+1.0em-1.0	822.5	98000	113.149
21222	n1e1e2n2	ep-1.0em+1.0	7.09688	10000	1409.07
21224	n1e1e3n3	ep-1.0em-1.0	28.6769	28477	993.029
21225	n1e1e3n3	ep+1.0em-1.0	823.729	97800	118.728
21226	n1e1e3n3	ep-1.0em+1.0	7.10283	10000	1407.89
21232	n1e1sc	ep-1.0em-1.0	86.1229	86123	1000
21233	n1e1sc	ep+1.0em-1.0	2470.34	100000	40.4803
21234	n1e1sc	ep-1.0em+1.0	20.9005	20701	990.455
21125	n1n1a	ep+1.0em-1.0	23969.4	238694	9.95828
21126	n1n1a	ep-1.0em+1.0	2878.85	27788	9.65247
21137	n1n1aa	ep+1.0em-1.0	1582.94	15829	9.99975
21138	n1n1aa	ep-1.0em+1.0	281.145	2811	9.9984
21149	n1n1aaa	ep+1.0em-1.0	69.1909	692	10.0013
21150	n1n1aaa	ep-1.0em+1.0	16.0647	161	10.022
21369	n1n1bb	ep+1.0em-1.0	85.7148	85715	1000
21370	n1n1bb	ep-1.0em+1.0	25.0179	25018	1000
21321	n1n1cc	ep+1.0em-1.0	81.3195	81319	999.994
21322	n1n1cc	ep-1.0em+1.0	24.5259	24526	1000
21361	n1n1dd	ep+1.0em-1.0	87.9093	87909	999.997
21362	n1n1dd	ep-1.0em+1.0	25.5486	25549	1000.02
21353	n1n1e2e2	ep+1.0em-1.0	44.7068	42707	955.269
21354	n1n1e2e2	ep-1.0em+1.0	12.8466	12847	1000.03
21357	n1n1e3e3	ep+1.0em-1.0	44.4163	43417	977.493
21358	n1n1e3e3	ep-1.0em+1.0	12.7892	12789	999.984
20593	n1n1h	ep+1.0em-1.0	60.8309	60831	1000
20594	n1n1h	ep-1.0em+1.0	21.6813	21681	999.986
21365	n1n1ss	ep+1.0em-1.0	87.6368	87637	1000
21366	n1n1ss	ep-1.0em+1.0	25.4646	25465	1000.02
21317	n1n1uu	ep+1.0em-1.0	81.2845	81094	997.533
21318	n1n1uu	ep-1.0em+1.0	24.5303	24330	991.835
21249	n2e2du	ep+1.0em-1.0	2268.24	98603	43.4698
21250	n2e2du	ep-1.0em+1.0	20.8833	19883	952.1
21237	n2e2e1n1	ep+1.0em-1.0	822.267	95800	116.507
21238	n2e2e1n1	ep-1.0em+1.0	7.11354	10000	1405.77
21239	n2e2e1n1	ep+1.0em+1.0	28.8352	28835	999.993
21241	n2e2e2n2	ep+1.0em-1.0	779.633	98800	126.726
21242	n2e2e2n2	ep-1.0em+1.0	19.3972	18197	938.125
21245	n2e2e3n3	ep+1.0em-1.0	755.228	97400	128.968
21246	n2e2e3n3	ep-1.0em+1.0	7.11024	9400	1322.04
21253	n2e2sc	ep+1.0em-1.0	2265.78	97000	42.8109
21254	n2e2sc	ep-1.0em+1.0	20.8933	20493	980.841
21129	n2n2a	ep+1.0em-1.0	4486.97	42870	9.95433
21130	n2n2a	ep-1.0em+1.0	2875.61	28756	9.99996
21141	n2n2aa	ep+1.0em-1.0	439.022	4390	9.9995
21142	n2n2aa	ep-1.0em+1.0	280.164	2802	10.0013
21153	n2n2aaa	ep+1.0em-1.0	25.1552	2502	10.0178
21154	n2n2aaa	ep-1.0em+1.0	16.0995	161	10.0003
21389	n2n2bb	ep+1.0em-1.0	59.3921	47792	804.686
21390	n2n2bb	ep-1.0em+1.0	24.9283	24928	999.988
21329	n2n2cc	ep+1.0em-1.0	54.498	54498	1000
21330	n2n2cc	ep-1.0em+1.0	24.5273	24327	991.834
21381	n2n2dd	ep+1.0em-1.0	60.6737	60474	996.709
21382	n2n2dd	ep-1.0em+1.0	25.509	25509	1000
21372	n2n2e1e1	ep-1.0em-1.0	16.1179	15718	975.189
21373	n2n2e1e1	ep+1.0em-1.0	38.3067	37307	973.903
21374	n2n2e1e1	ep-1.0em+1.0	21.4025	21403	1000.02
21375	n2n2e1e1	ep+1.0em+1.0	16.124	16124	1000
21377	n2n2e3e3	ep+1.0em-1.0	24.5789	24579	1000
21378	n2n2e3e3	ep-1.0em+1.0	12.7721	11772	921.697
20597	n2n2h	ep+1.0em-1.0	33.8395	33839	1000.01
20598	n2n2h	ep-1.0em+1.0	21.6474	21647	999.982
21385	n2n2ss	ep+1.0em-1.0	60.5318	56332	940.53
21386	n2n2ss	ep-1.0em+1.0	25.5038	24304	952.956
21325	n2n2uu	ep+1.0em-1.0	54.5125		

B Histograms of cut variables

B.1 $Z \rightarrow e^+e^-$ mode

Figures 17 - 28 show the histograms of cut variables. The blue lines in all histograms show the signal process $ZH \rightarrow e^+e^-\tau^+\tau^-$.

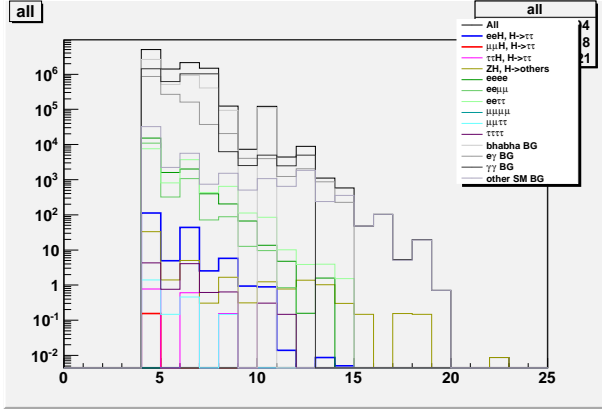


Figure 17: Number of tracks ≤ 8 .

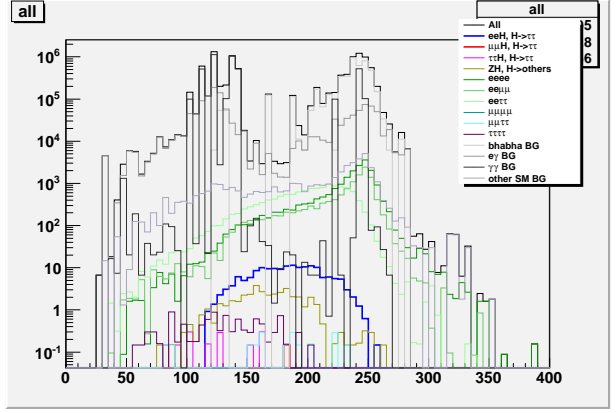


Figure 18: $115 \text{ GeV} < E_{\text{vis}} < 230 \text{ GeV}$.

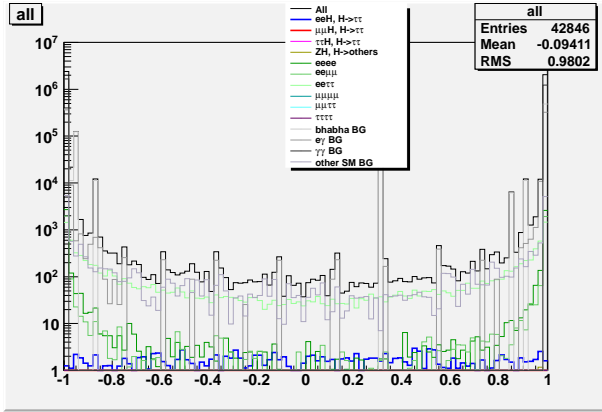


Figure 19: $|\cos \theta_{\text{miss}}| < 0.99$.

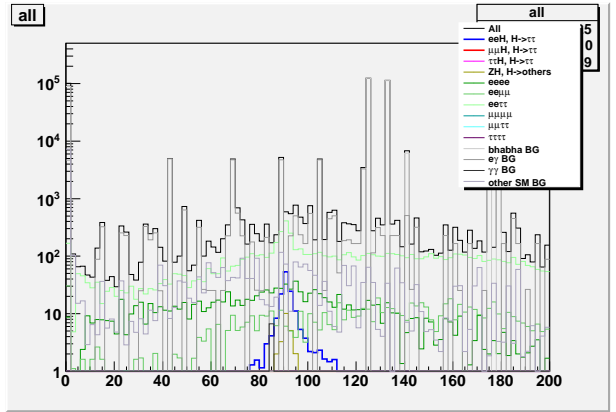


Figure 20: $81 \text{ GeV} < M_Z < 113 \text{ GeV}$.

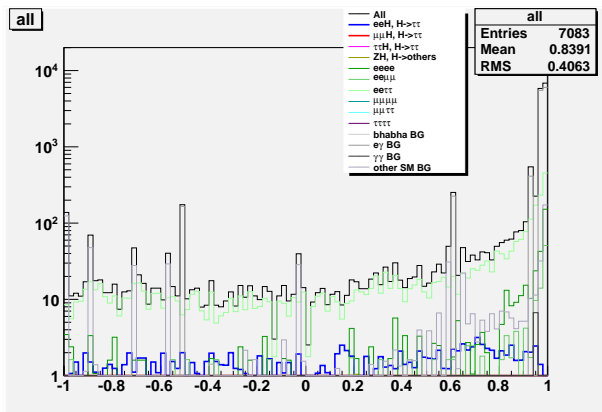


Figure 21: $\cos \theta_{e^-} < 0.92$.

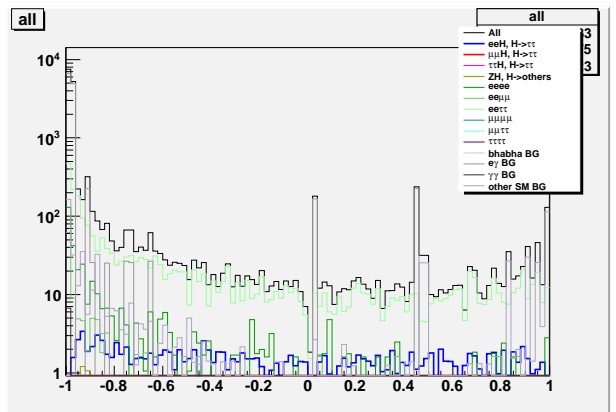


Figure 22: $\cos \theta_{e^+} > -0.92$.

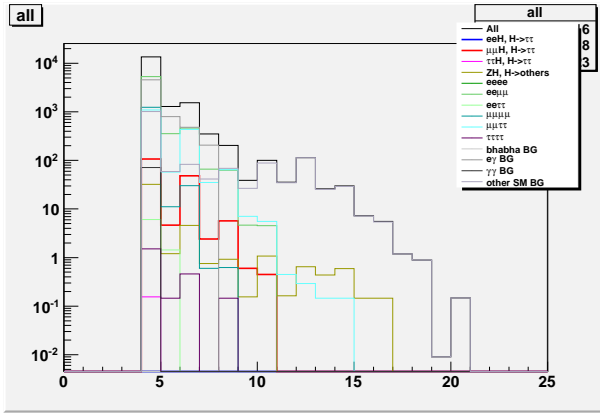


Figure 29: Number of tracks ≤ 8 .

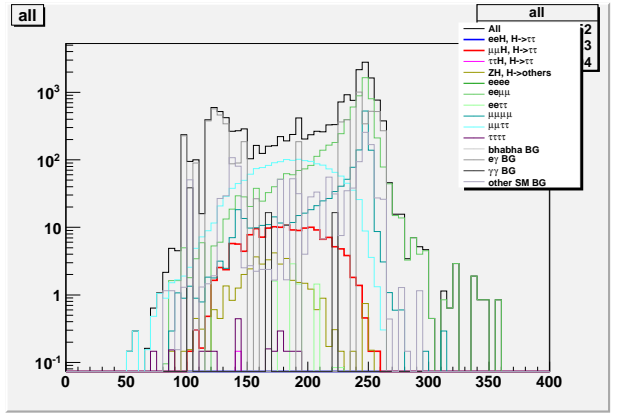


Figure 30: $115 \text{ GeV} < E_{\text{vis}} < 235 \text{ GeV}$.

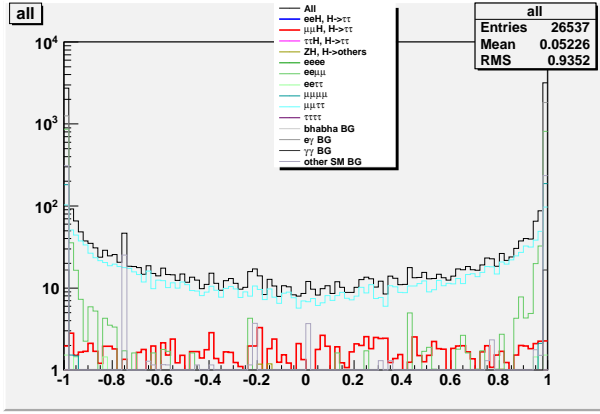


Figure 31: $|\cos \theta_{\text{miss}}| < 0.98$.

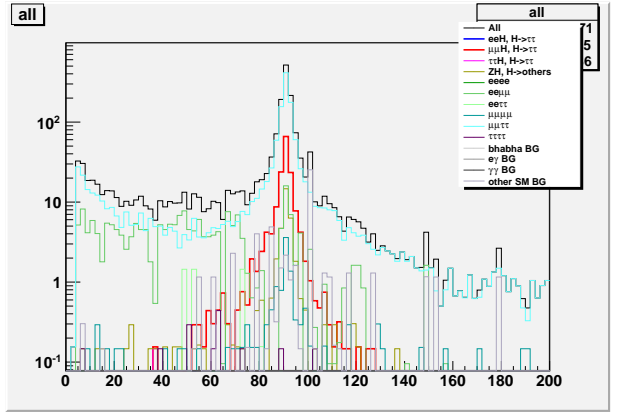


Figure 32: $72 \text{ GeV} < M_Z < 107 \text{ GeV}$.

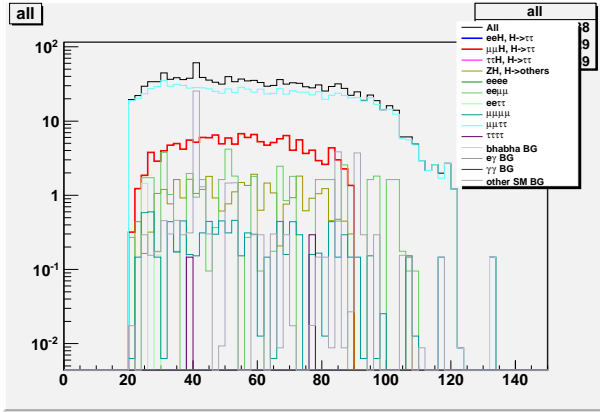


Figure 33: $E_{e^-} < 90 \text{ GeV}$.

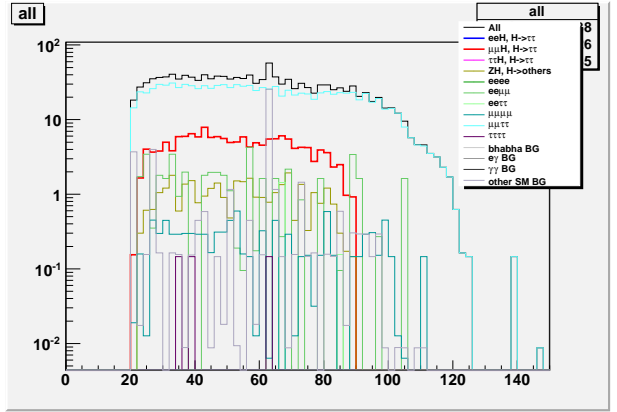


Figure 34: $E_{e^+} < 90 \text{ GeV}$.

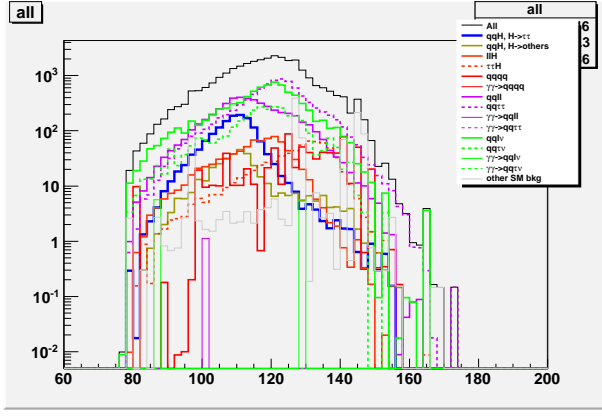


Figure 41: $80 \text{ GeV} < E_Z < 135 \text{ GeV}$.

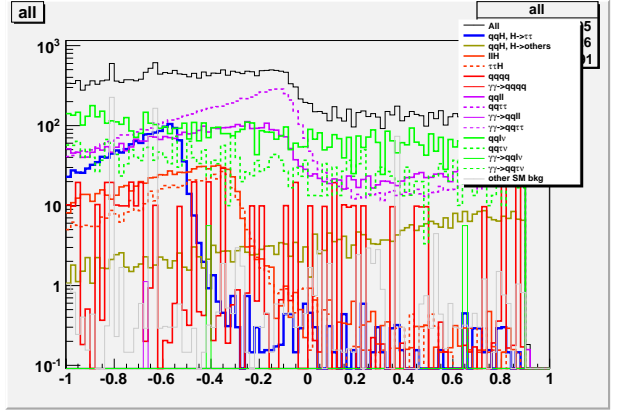


Figure 42: $\cos \theta_{\tau^+\tau^-} < -0.5$.

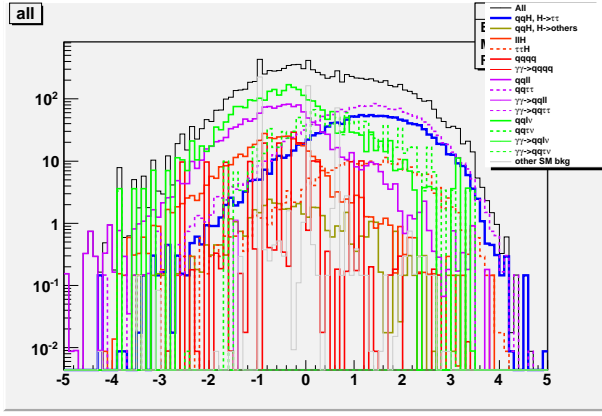


Figure 43: $\log_{10}(|d_0/\sigma(d_0)|)(\tau^-) + \log_{10}(|d_0/\sigma(d_0)|)(\tau^+) > -0.7$.

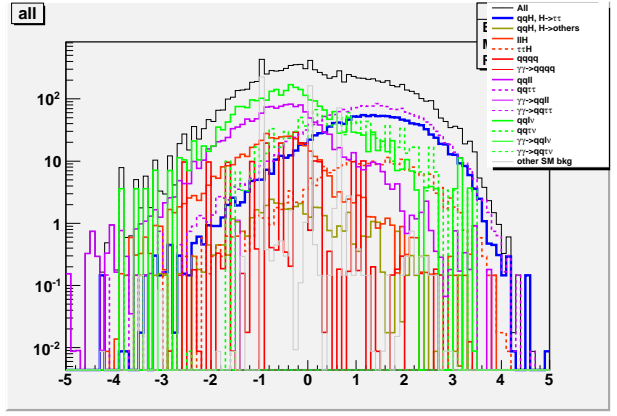


Figure 44: $\log_{10}(|z_0/\sigma(z_0)|)(\tau^-) + \log_{10}(|z_0/\sigma(z_0)|)(\tau^+) > -0.1$.

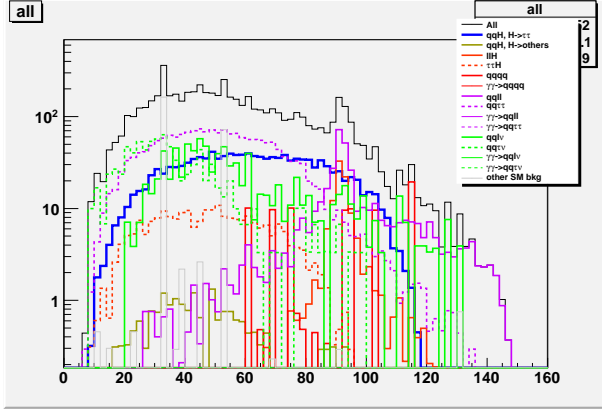


Figure 45: $M_{\tau^+\tau^-} < 115 \text{ GeV}$.

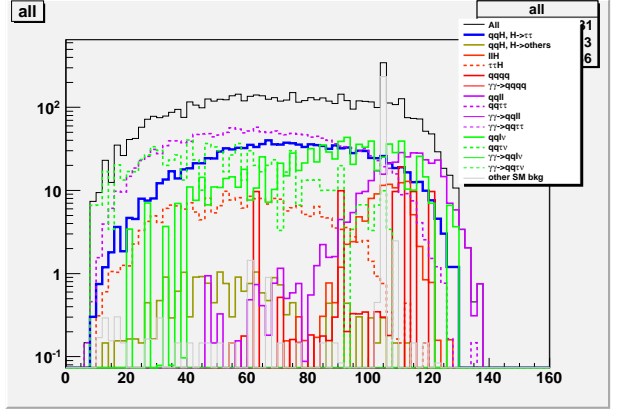
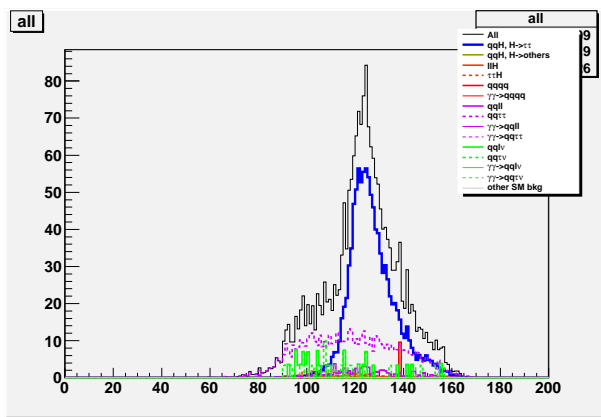
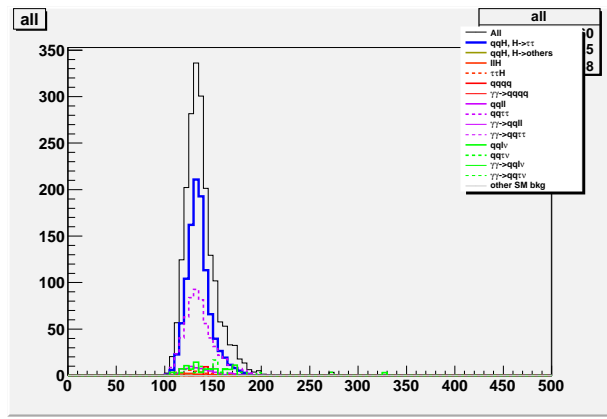
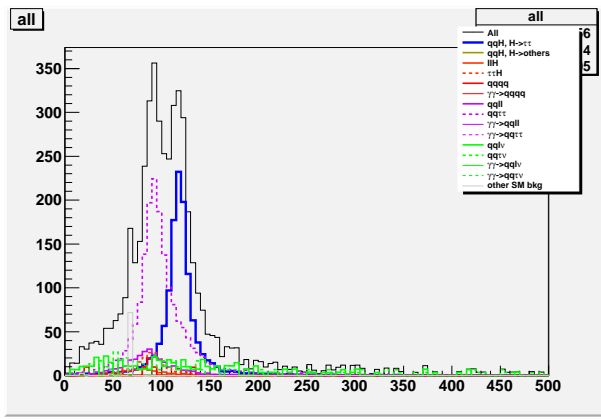


Figure 46: $E_{\tau^+\tau^-} < 125 \text{ GeV}$.



References

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