

Jet Production in Hadron-Hadron Collisions  
at High Energies



*By*  
Ali Zaman  
CIIT/FA09-PPH-001/ISB  
PhD Thesis  
*In*  
Physics

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Spring, 2015



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# Jet Production in Hadron-Hadron Collisions at High Energies

A thesis presented to

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In partial fulfillment  
of the requirement of the degree of

**PhD (Physics)**

By

Ali Zaman

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## at High Energies

A Post Graduate Thesis submitted to the Department of Physics as partial fulfillment of the requirement for the award of Degree of PhD in Physics

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at High Energies**

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To My Late Father

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**Ali Zaman**  
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## ABSTRACT

### Jet Production in Hadron-Hadron Collisions at High Energies

We investigated the effects of jet production on the following parameters: multiplicity, pseudorapidity, transverse momentum and transverse mass distributions of charged particles produced in hadron-hadron collisions at 1.8 TeV, centre of mass energy, using the Dubna version of HIJING model. These distributions are analyzed for the whole range and for six selected regions of the polar angle (angle of the secondary particles with respect to the beam axis) as a function of number of jets. The results for the charged particles multiplicity distributions were compared with experimental ones coming from the SPS and Tevatron experiments and the increase in the multiplicity of the charged particles influenced by multi-jet events is discussed. The results for pseudorapidity distributions are interpreted and discussed in connection to the increase observed in the multiplicity of charged particles as a result of its multi-jet dependence and are also discussed in comparison with the experimental results coming from the CDF Collaboration. The analysis of effect of the multi-jet events on the transverse momentum and transverse mass distributions is also discussed in connection to the increase in the multiplicity and pseudorapidity density of charged particles. We concluded that high multiplicity regions, the increased pseudorapidity density and the high  $p_T$  regions correspond mainly to the multi-jet events.

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## LIST OF ABBREVIATIONS

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<i>AA</i>	Nucleus-Nucleus
ALICE	A Large Ion Collider Experiment ( <a href="http://alice-collaboration.web.cern.ch">http://alice-collaboration.web.cern.ch</a> )
<i>AuAu</i>	Gold-Gold
BNL	Brookhaven National Laboratory ( <a href="http://www.bnl.gov">http://www.bnl.gov</a> )
CDF	Central Detector at Fermilab ( <a href="http://www-cdf.fnal.gov">http://www-cdf.fnal.gov</a> )
CERN	European Centre for Nuclear Research ( <a href="http://www.cern.ch">http://www.cern.ch</a> )
CMS	Centre-of-Mass System
<i>dAu</i>	Deuteron-Gold
DESY	Deutsches Elektronen-Synchrotron ( <a href="http://www.desy.de">http://www.desy.de</a> )
DGLAP	Dokshitzer-Gribov-Lipatov-Altarelli-Parisi
DIS	Deep-Inelastic Scattering
E735	Experiment735 at Tevatron Fermilab
$E_T$	transverse energy
<i>fm</i>	femto-meter ( $10^{-15}$ m)
FORTRAN	Formula Translation
GeV	Giga electron Volt ( $10^9$ eV)
H1	H1 ( <a href="http://www.desy.de">http://www.desy.de</a> )
HERA	Hadron-Electron Ring Accelerator ( <a href="http://www.desy.de">http://www.desy.de</a> )
HERWIG	Hadron Emission Reactions with Interfering Gluons ( <a href="http://hepwww.rl.ac.uk/theory/seymour/herwig/">http://hepwww.rl.ac.uk/theory/seymour/herwig/</a> )
HIJING	Heavy Ion Jet Interaction Generator ( <a href="http://www-nsdth.lbl.gov/~xnwang/hijing/">http://www-nsdth.lbl.gov/~xnwang/hijing/</a> )
HIJSET	a HIJING's subroutine
IHPR2(8)	HIJING parameter for Number of Jets

ISR	Intersecting Storage Ring ( <a href="http://www.cern.ch">http://www.cern.ch</a> )
KNO	Koba-Nielsen-Olesen
LAB	Laboratory (Fixed Target Experiment)
LEP	Large Electron–Positron Collider ( <a href="http://www.cern.ch">http://www.cern.ch</a> )
LHC	Large Hadron Collider ( <a href="http://www.cern.ch">http://www.cern.ch</a> )
LO	Leading-Order
LPHD	Local Parton-Hadron Duality
MC	Monte Carlo
MD	Multiplicity Distribution
MeV	Mega electron Volt ( $10^6$ eV)
$m_T$	Transverse Mass
NB	Negative Binomial
$N_{ch}$	Multiplicity of Charged Particles
$N_{\text{jet}}$	Number of Jets
NLO	Next-to-Leading Order
NMF	Nuclear Modification Factor ( $R_{AA}$ )
OPAL	Omni-Purpose Apparatus for LEP ( <a href="http://opal.web.cern.ch/Opal">http://opal.web.cern.ch/Opal</a> )
$pA$	Proton(or Hadron)-Nucleus
Pb–Pb	Lead-Lead
PDFs	Parton Distribution Functions
PETRA	Positron Electron Tandem Ring Accelerator ( <a href="http://www.desy.de">http://www.desy.de</a> )
PHOJET	PHOJET ( <a href="http://www-ik.fzk.de/~engel/phojet.html">http://www-ik.fzk.de/~engel/phojet.html</a> )
$pp$	Proton-Proton (or Hadron-Hadron)
pQCD	Perturbative Quantum Chromodynamics
$p_T$	Transverse Momentum

PYTHIA	PYTHIA ( <a href="http://home.thep.lu.se/~torbjorn/Pythia.html">http://home.thep.lu.se/~torbjorn/Pythia.html</a> )
QCD	Quantum Chromodynamics
QGP	Quark-Gluon Plasma
RHIC	Relativistic Heavy Ion Collider ( <a href="http://www.bnl.gov">http://www.bnl.gov</a> )
SLAC	Stanford Linear Accelerator Centre ( <a href="http://www-ssrl.slac.stanford.edu">http://www-ssrl.slac.stanford.edu</a> )
SM	Standard Model
SPEAR	Stanford Positron Electron Asymmetric Ring ( <a href="http://www-ssrl.slac.stanford.edu">http://www-ssrl.slac.stanford.edu</a> )
SPS	Super Proton Synchrotron ( <a href="http://www.cern.ch">http://www.cern.ch</a> )
TeV	Tera electron Volt ( $10^{12}$ eV)
TMD	Transverse-Momentum Dependent
UA5	UA5 (an experiment at SPS)
ZEUS	ZEUS ( <a href="http://www.desy.de">http://www.desy.de</a> )
$\eta$	Pseudorapidity

# Chapter 1      Introduction

Particle physics is aimed to address the study of the ultimate constituents of matter and the basic forces through which these constituents interact with each other.

The fundamental constituents of matter are the fermions (carrying spin  $\frac{1}{2}$ ) and the mediators of interactions between them are bosons (carrying integral spin). The four fundamental interactions in nature are the following. The strong interaction with gluons ( $g$ ) as mediator bosons and the particles that interact through this interaction are those which possess the color charge and these are the only quarks. The weak force with  $W$  ( $W^+$ ,  $W^-$ ) and  $Z^0$  bosons as mediators, leptons and quarks are the participating particles in this interaction, and this is the only force responsible for the neutrinos' interactions. The electromagnetic force having photon ( $\gamma$ ) as mediator boson, which is responsible for the interactions of electrically charged particles. The force of gravity whose mediator boson is the graviton which is not discovered yet, the objects possessing mass interact through this force. The effects of the gravity on the particles are negligible as compared to the effects of other three forces [1, 2].

In the standard model (SM) of particle physics the building blocks of the matter are the quarks and the leptons which are grouped in three generations on the basis of their masses interacting through the two forces; the electroweak force (which is the unified form of the electromagnetic and the weak force) and the strong force, and the gravity is not included in this framework [1, 2]. All the predictions of the SM has been completely tested and discovered experimentally during last  $\sim 50$  years, the last of this was the remarkable discovery of the Higgs boson at the large hadron collider (LHC) CERN in 2012. Figure 1.1 shows a schematic arrangement of fundamental particles and forces included in the SM framework.

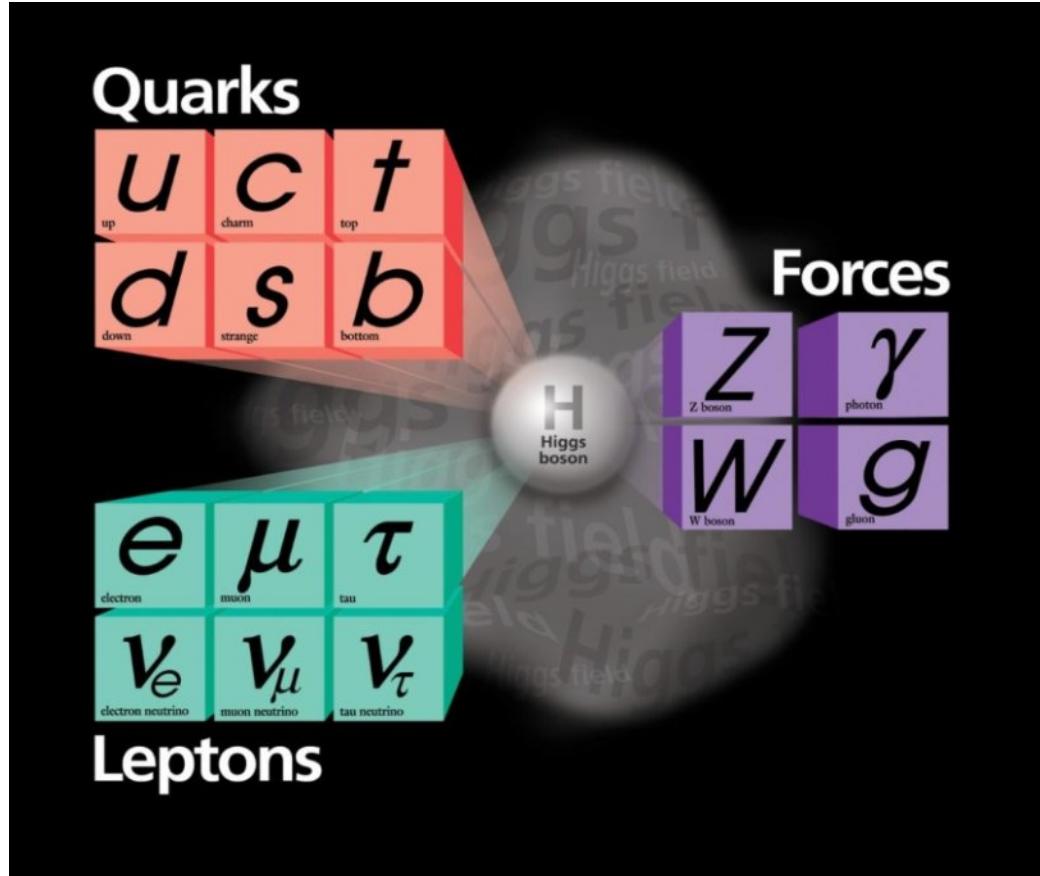


Figure 1.1 Fundamental particles and forces in the framework of SM of particle physics [3]

Physics of high energy hadronic collisions reveals the properties of strongly interacting matter like hadrons and their constituents, quarks which interact via gluons. In relativistic and ultrarelativistic hadronic interactions, the nucleons breakup at such high energies and lose their individual identity. During such interactions free quarks and gluons are produced at a very short time scale  $\sim 10^{-24}$  sec and thus a new state of strongly interacting matter; the quark-gluon plasma (QGP) is created [4, 5]. These free quarks hadronize by interacting with other quarks and anti-quarks to produce hadrons either combining in a doublet state of quark-antiquark pair  $q\bar{q}$  the mesons or in quark triplet state  $qqq$  termed as the baryons.

The theory of strongly interaction or the quantum theory of the color (chrome), the quantum chromodynamics (QCD), forbids the individual existence of quarks and they are confined in the hadrons. During the process of formation of hadrons from the quarks, these particles may assume the form of a cone, which is termed as jet production. By studying the properties of these jets we can get information about the properties of quarks [1, 2, 4, 5].

In the present work we study the effects of the jet production on different parameters of the charged particles produced in hadron-hadron collisions, at energy 1.8 TeV in the frame of centre-of-mass system (CMS), using Dubna version of the heavy ion jet interaction generator (HIJING) Monte Carlo model for event simulations.

### **Layout of this Thesis**

First chapter of this thesis is a general introduction. Second chapter is about brief description/review of the jets in high energy physics. The methodology is described in third chapter which includes the procedure of this research work and a general description of the HIJING Model. A detailed discussion of the results for different parameters of charged particles produced in pp collisions is presented in chapter 4. Finally conclusions are summarized in chapter 5.

## Chapter 2      Jets in High Energy Collisions

This chapter contains a brief description about the jets, their production, quenching and importance in high energy hadronic collisions.

### 2.1 Jets

The word jets employed (and first used by D. H. Perkins in 1954) to describe the collimation of the secondary hadrons produced in high energy collisions. A jet results from the fact that the average transverse momentum of the secondaries is of the order of a few  $\text{GeV}/c$ , being determined by the range of the strong interaction. In a high energy collision, the secondaries will generally carry large longitudinal momentum components and therefore emerge in a narrow cone [1].

In high energy hadronic collisions, jets are defined as a narrow cone of hadrons or other particles produced by the hadronization of quarks or gluons, collectively termed as partons. Due to the quantum chromodynamics (QCD) color confinement, particles with a color charge, like quarks, cannot exist in free state. Therefore, in a high energy collision, they form jets which fragment into hadrons before their direct detection. The process of the formation of colorless hadrons out of the colored partons (quarks and gluons) is known as hadronization. In a particle collider experiment, the process of hadronization occurs at high energy collisions where free quarks and gluons are created. Due to the color confinement, these quarks and gluons combine with quarks and antiquarks, which are created spontaneously from the vacuum and ultimately form the colorless hadrons. To determine the properties of the original quark, these jets must be measured and analyzed in a particle detector [1, 2, 4—9].

### 2.2 Importance of Jets

In particle physics jets are of great importance because these provide explanation and understanding about the observation of grouped/shower particles in a collider detector experiment. These jets are the experimental evidence of the existence of the quarks in the

hadrons, and properties of these jets reflect the properties of the quarks from which these jets are originated. Jet physics also provides the details about the hadronization of the colored partons: quarks or gluons and their fragmentation into colorless hadrons.

Jets are considered as a hard probe to get the information about the new states of the strongly interacting matter. So the study of the jet production in high energy hadron-hadron collisions is of great interest and importance. Within the frame of the quantum chromodynamics QCD - the theory of strong interaction, jets are believed to result from quarks and gluons with high transverse momentum ( $p_T$ ) [1, 6], and thus should carry information about the deconfined state of the strongly interacting matter [1, 2, 4—7], supposedly produced in such high energy interactions. First time it was proposed by Hagedorn that there should be some critical temperature for hadrons after which the hadrons transform to the system of free quarks and gluons [10]. Analyzing the energy spectrum of the hadrons he found the critical temperature to be around  $\sim 200$  MeV. In framework of the QCD this phenomena is called deconfinement.

Jets produced in high energy heavy ion interaction are important because the initial hard scattering is a natural probe for the QCD matter created in this high energy collision indicating its phase. When the formation of quark-gluon plasma (QGP) [4, 5, 11, 12] occurs by phase crossover of the QCD matter there is significant growth of the radiative energy loss in the medium. This energy loss in the medium quenches the outgoing jet [4, 11] effectively. Different phases of the strongly interacting QCD matter are shown in Figure 2.1.

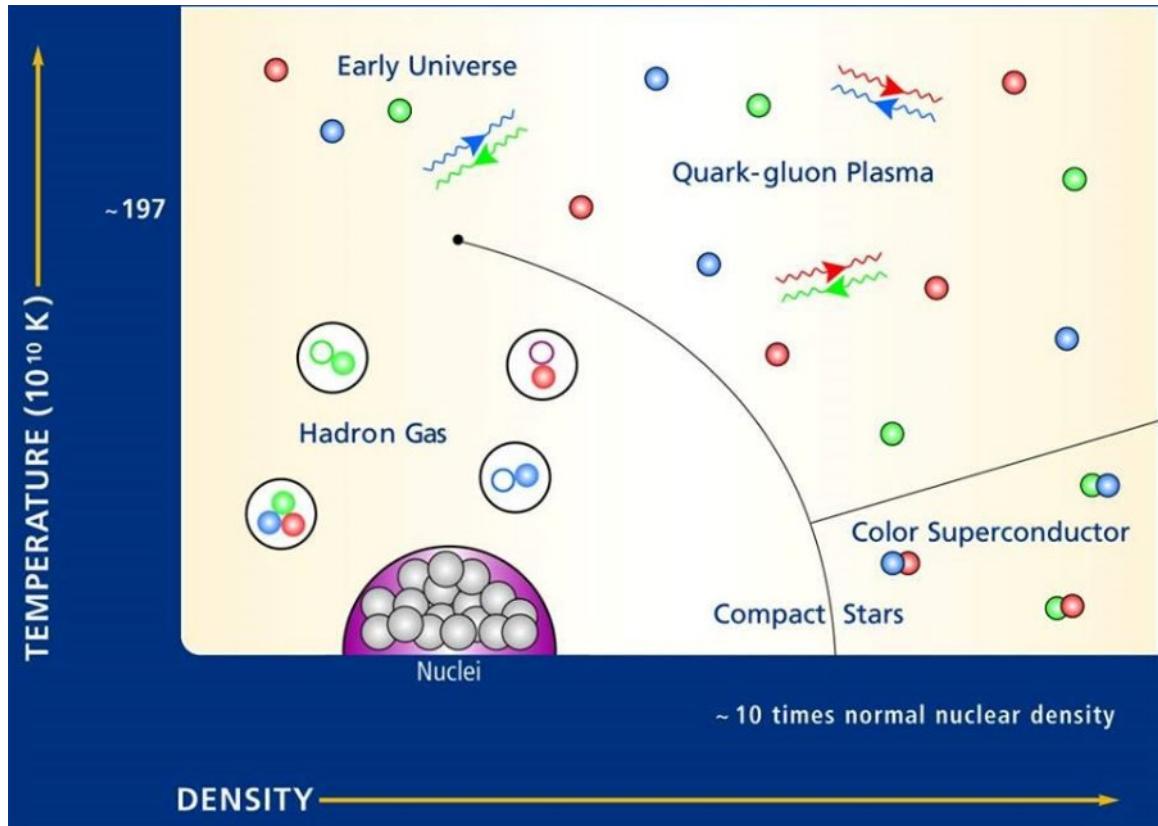


Figure 2.1 Phases of the strongly interacting matter [13]

## 2.3 Jet Production

Jet production occurs in high energy collisions during QCD hard scattering processes when the partons, quarks and gluons are created with high transverse momentum ( $p_T$ ). A pictorial view of a hard scattering event is shown in Figure 2.2 and the schematic of the different stages of the jet production in  $pp(\bar{p})$  interaction is presented in Figure 2.3, which describes the steps of the jet evolution from the hard scattering of quarks, hadronization process and finally their calorimetric measurements.

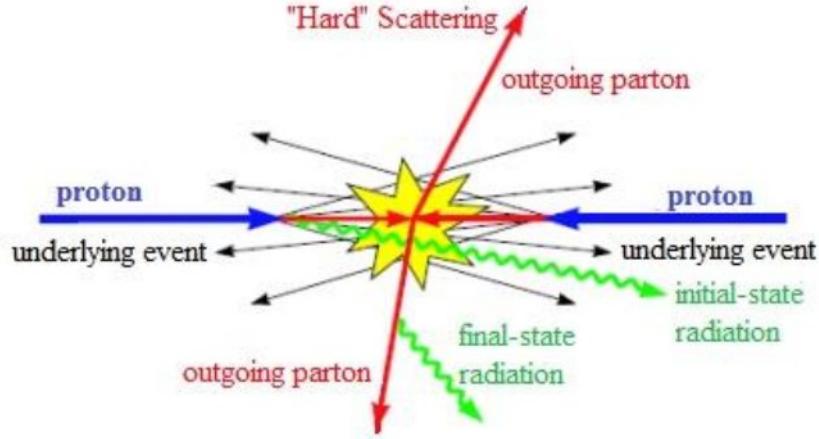


Figure 2.2 Hard scattering event in pp collision, a pictorial view [14, 16]

The jet production cross-section is used to describe the probability for the creation of a certain set of jets in a collision. This cross-section is described by the parton distribution functions (PDFs) and is the average of an elementary pQCD quark, antiquark, or gluon process. In a two particle scattering the process of production of the most frequent jet pair, the cross-section of jets production in a hadronic collision [14, 15] is given by the following equation.

$$\sigma_{ij \rightarrow k} = \sum_{i,j} \int dx_1 dx_2 d\hat{t} f_i^1(x_1, Q^2) f_j^2(x_2, Q^2) \frac{d\hat{\sigma}_{ij \rightarrow k}}{d\hat{t}} \quad (2.1)$$

where,  $x$  is the longitudinal momentum fraction;  $Q^2$  the transferred momentum;  $\sigma_{ij \rightarrow k}$  the perturbative QCD cross-section for the process  $ij \rightarrow k$ ;  $f_i^a(x_a, Q^2)$  the parton distribution function for finding particle species  $i$  in beam  $a$ , and  $\hat{\sigma}$ s are the elementary cross-sections.

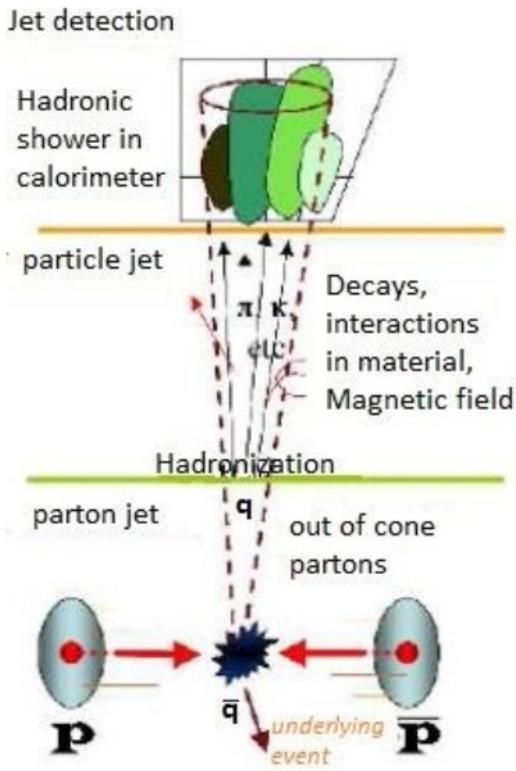


Figure 2.3 A schematic representation of the different stages of the jet production and its measurements [14]

## 2.4 Jet Fragmentation

In the perturbative QCD calculations there may be colored partons in the final state, but experimentally there observed only the colorless hadrons produced by these partons. To describe the experimental observation resulted from a given interaction in a detector, all of the exiting colored partons must undergo the process of parton showering firstly and then these produced partons combine to form hadrons. In a high energy collision, the process of formation of hadrons, soft QCD radiation, or both of these processes [8, 12], are termed as fragmentation or hadronization.

When a parton, produced in a hard scattering, exits the interaction, there will be an increase in the strong coupling constant with the separation. This results an increase in

the probability of the QCD radiation, which is shallow-angled with respect to the initial parton predominantly. So a parton will radiate gluons, which will be resulted in production of quark-antiquark ( $q\bar{q}$ ) pairs and so on. The generated each new parton is nearly collinear with its parent. By convolving the spinors with fragmentation functions  $P_{ji}\left(\frac{x}{z}, Q^2\right)$ , this can be described in a way similar to that of the PDFs evolution. Which can be described by Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) equation [17] given below,

$$\frac{\partial}{\partial \ln Q^2} D_i^h(x, Q^2) = \sum_j \int_x^1 \frac{dz}{z} \frac{\alpha_S}{4\pi} P_{ij}\left(\frac{x}{z}, Q^2\right) D_i^h(z, Q^2) \quad (2.2)$$

The parton showering results in the production of low energy partons successively, and thus it exits the pQCD validity region. When the parton showers are formed then to describe the length of time the phenomenological models should be applied. And then these colored partons are combined into their confined state i.e. the colorless hadrons.

## 2.5 Jet Finding Procedures

Due to the color confinement of the quarks and gluons their final state distribution cannot be directly measured, because the hard scattering final state contains colorless hadrons only. In the jet defining algorithms, the observed hadrons and the partons in the final state of the high energy hadronic interactions are associated to the local parton-hadron duality (LPHD) [18] correspondence. Satisfaction of the LPHD correspondence implies that jet production can be used as tool for mapping the observed long-distance hadronic final state onto underlying short-distance partonic states [19].

Jet finding algorithms define a functional mapping between the particles in terms of their kinematic descriptions (e.g. momentum etc.) and the jet configurations, represented by suitable jet variables.

$$\text{particles} \xrightarrow{\text{jet-algorithm}} \text{jets}$$

Ideally, a jet defining algorithm should be [19, 20]:

- Fully specified in terms of completely defining the procedure, the kinematical variables and the variety of corrections must be specified in a unique way.
- It should be well behaved theoretically i.e. the jet algorithm must be collinear and infrared safe, do not use any ad-hoc parameter.
- It should be detector independent in terms of the type, segmentation or size of the detector.
- The algorithm should be consistent so that it must have equal applicability for the theoretical and experimental level.

Every algorithm must satisfy the first two criteria as the LPHD can only be fulfilled if the algorithm obeys the infrared safety condition. That makes sure the insensitivity of outcome on the emitted collinear or soft partons. Probably, the last two criteria totally cannot be satisfied, as the experimental apparatus dependencies cannot be removed completely.

## 2.6 Jets Kinematics

Generally the interacting partons are not in the centre-of-mass system (CMS) frame of the collision system, as there is event to event variation in the fraction of momentum carried by the partons. The partonic centre-of-mass system is therefore boosted along the direction of the colliding hadron randomly, so that the jets can be described conveniently in terms of the following longitudinally boost-invariant variables [19]:

$$\text{Mass} \quad m = \sqrt{E^2 - p_x^2 - p_y^2 - p_z^2} \quad (2.3)$$

$$\text{Transverse momentum} \quad p_T = \sqrt{p_x^2 + p_y^2} \quad (2.4)$$

$$\text{Azimuthal angle} \quad \varphi = \tan^{-1}(p_y/p_x) \quad (2.5)$$

$$\text{Rapidity} \quad y = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \quad (2.6)$$

where  $E$  is total energy of secondary particles and  $p_z$  is their longitudinal momentum along z-axis.

For the relativistic limit, when  $p \gg m$ , conveniently the quantities which are directly measurable are: the transverse energy ( $E_T = E \sin \theta \approx p_T$ ), the azimuthal angle ( $\phi$ ) and the pseudorapidity  $\eta$  given by,

$$\eta = -\ln[\tan(\theta/2)] \quad (2.7)$$

where the polar angle  $\theta$  (with the beam axis) is given by,

$$\theta = \tan^{-1}(p_T/p_z) \quad (2.8)$$

## 2.7 Jet Algorithms

Jet algorithms can be classified in two fundamental classes: the recombination/sequential or clustering algorithms [21-25] and cone algorithms [26-29]. These algorithms use the assumptions that hadrons being associated with a jet should be ‘nearby’ each other. To define a jet, in cone jet algorithms are based on vicinity in real space including angles, while the sequential algorithms are based on vicinity in momentum space and thus known as  $k_T$  algorithms.

- The sequential or  $k_T$  algorithms are inspired by parton showering processes in QCD [14, 21, 22, 30]. These algorithms simulate the processes of the hadronization backward and group the pairs of particles in increasing order of  $p_T$  successively.
- The cone algorithms are designed for jets in the hadronic interactions. All particles are grouped inside a cone of radius  $R$  in  $\eta \times \phi$  space to form a single jet [26, 27, 31]. The radius of cone is defined as  $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$ , where  $\Delta\eta$  and  $\Delta\phi$  are the particle or parton separation in pseudorapidity and azimuthal angle (measured in radians) with respect to axis of the jet.

## 2.8 Experimental Observation of the Jets

First experimental observation of the jets, as an evidence of the quarks inside hadrons, was in electron-positron annihilation to hadrons at Stanford positron electron asymmetric ring (SPEAR), Stanford Linear Accelerator Centre (SLAC) [32—35] at beam energy  $\sim 7$  GeV in 1975 and then at positron electron tandem ring accelerator (PETRA), deutsches elektronen-synchrotron (DESY) [36—42] at beam energy  $\sim 30$  GeV in 1979. The angular distribution analysis of this quark initiated two-jet event showed that these hadron jets are associated with the spin  $1/2$  quarks constituents [1, 37—42]. This two-jet event, illustrated in Figure 2.4, can be regarded as a two step process, an electromagnetic process  $e^+e^- \rightarrow q\bar{q}$  to produce quark-antiquark pair and then fragmentation of this  $q\bar{q}$  pair to two hadronic jets [1, 36].

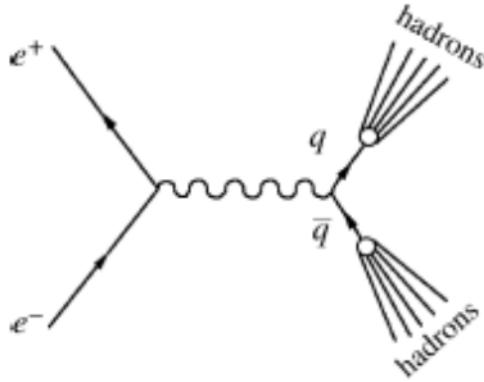


Figure 2.4 Production mechanism of two-jets in  $e^+e^-$  annihilation to hadrons [36]

The gluon-initiated jets were also observed in  $e^+e^-$  collider at PETRA which resulted by the emission of a high-momentum gluon by quark or antiquark before their fragmentation and then these three  $q\bar{q}$  pair and the gluon hadronize to form 3-jets of hadrons [1, 36, 41, 42]. A schematic of this three-jet event is shown in Figure 2.5.

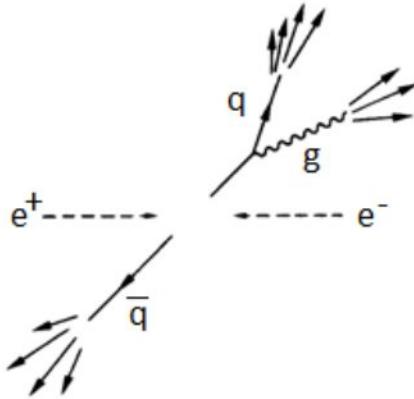


Figure 2.5 Production mechanism of a three-jet event in the process  $e^+e^- \rightarrow q\bar{q}g \rightarrow \text{hadrons}$  [1].

Such type of hadronic jets have been observed in different kind of interactions like electron-positron collider at large electron-positron collider (LEP) [43—45] and  $p\bar{p}$ ,  $pp$ ,  $pA$  and  $AA$  collisions at various range of colliding energies (at intersecting storage ring (ISR) [46], super proton synchrotron (SPS) [47], Tevatron Femilab [14, 48—50], relativistic heavy ion collider (RHIC) [51, 52] and the largr hadron collider (LHC) [14, 19, 53], which provided strong evidence about the existence of quarks inside the hadrons.

A schematic of different stages of the jet production in a  $pp/p\bar{p}$  collisions is shown in Figure 2.3 and following Figure 2.6 is an art picture of the jet production in hadron-hadron collisions. And Figure 2.7 interprets the kinematics of parton scattering during jet production at a proton-antiproton collider, where  $P_1$  and  $P_2$  are momenta of the colliding proton and antiproton respectively being carried by the interacting partons (quarks or gluons) and  $P_3$  and  $P_4$  are the observed 4-momenta of the outgoing partons being fragmented to two jets of secondary hadrons [1].

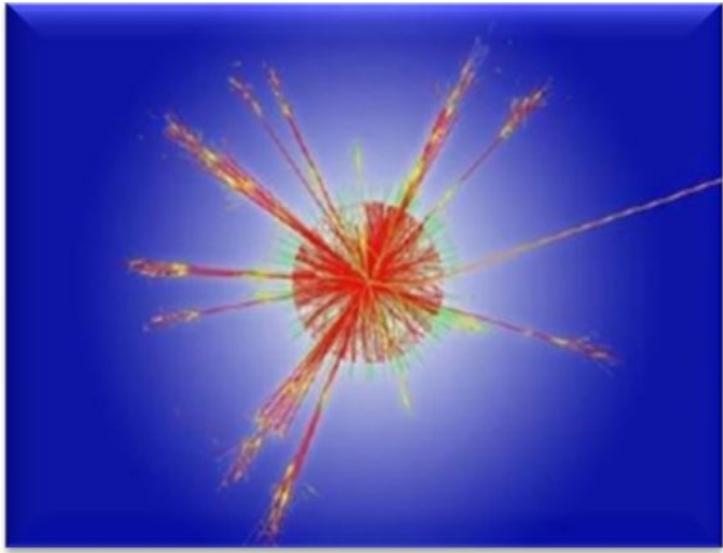


Figure 2.6 An art picture of jets in  $pp$ -collisions [54]

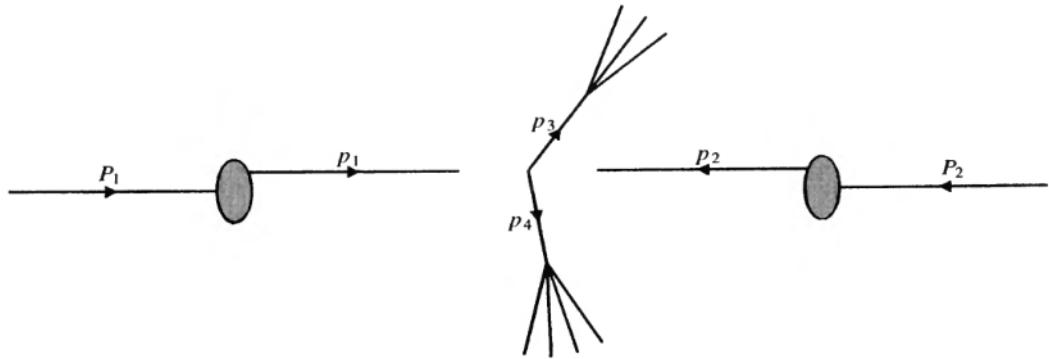


Figure 2.7 Schematics of parton-parton interaction for jet production in a  $pp/ p\bar{p}$  collision [1]

### Jets in $ep$ Collisions

The observation of jet production at hadron-electron ring accelerator (HERA) tested the theory of strong interactions, quantum chromodynamics (QCD), and extracted information on the parton content of the proton and of real or virtual photons [55]. QCD

predicts the production of partons with large transverse momentum, fragmenting into jets with similar four-momentum. The study of jet observables therefore allows the investigation of the underlying parton dynamics. Perturbative QCD predictions, however, also need the parton content of the proton and photon as input. Jet cross-section can thus be used to further constrain the partons density functions (PDFs) obtained by global fits.

The clustering of final state objects into a few jets is performed by applying a jet finding algorithm. The H1 [56] and ZEUS [57] collaborations presented the results obtained with the  $k_T$  algorithm. This algorithm has the advantage of being infrared and collinear safe and to be minimally sensitive to fragmentation and underlying event effects. Correction of reconstructed data is performed from detector to hadron level using a full detector simulation. Next-to-leading order (NLO) QCD predictions are corrected from parton to hadron level. This involves the fragmentation of partons into hadrons and secondary interactions between partons of the photon and proton remnants. Correction factors are obtained from leading-order (LO) Monte Carlo (MC) models where NLO effects are modeled by QCD cascades.

In LO two types of processes are distinguished. In direct processes the exchanged photon interacts as a whole with the proton and produces jets. In resolved interactions, the photon is treated as a source of partons, one of which produces a hard scattering with the proton, leaving behind a soft photon remnant. The concept of resolved photons is useful in photoproduction as well as in deep-inelastic scattering (DIS) when  $E_T^2 \gg Q^2$ , where  $E_T$  is the transverse energy of the partons produced in the hard interaction and  $Q^2$  is the virtuality of the exchanged photon. To separate direct and resolved enhanced event samples, the momentum fraction of the photon entering the hard scattering,  $x_\gamma$ , can be used. On hadron level, the variable  $x_\gamma^{jet}$ , which is correlated to the parton level  $x_\gamma$ , is calculated as  $x_\gamma^{jet} = \sum_{jets} E_T^{jet} e^{-\eta^{jet}} / 2E_\gamma$ , where  $E_T^{jet}$  and  $\eta^{jet}$  are the jet transverse energy and pseudorapidity and  $E_\gamma$  is the energy of exchanged photon.

Using QCD factorization, the direct and resolved cross-sections for producing  $N$  jets, integrated over phase space, can be expressed as [55],

$$\sigma_{direct}^{ep \rightarrow e+Njets+X} \int_{\Omega} d\Omega f_{\gamma/e}(y, Q^2) \sum_i f_{i/p}(x_p, \mu_p^2) \sigma^{\gamma i \rightarrow Njets} \quad (2.9)$$

$$\sigma_{resolved}^{ep \rightarrow e+Njets+X} \int_{\Omega} d\Omega f_{\gamma/e}(y, Q^2) \sum_{ij} f_{i/p}(x_p, \mu_p^2) f_{j/\gamma}(x_{\gamma}, \mu_{\gamma}^2) \sigma^{\gamma i \rightarrow Njets} \quad (2.10)$$

where  $f_{\gamma/e}$ ,  $f_{i/p}$  and  $f_{j/\gamma}$  are flux factors for photons originating from the electron and for partons originating from the proton and the photon, respectively, evaluated at given fractional momentum-energies and factorization scales. The partonic cross-sections  $\sigma^{\gamma i \rightarrow Njets}$  and  $\sigma^{ij \rightarrow Njets}$  can be calculated in LO and NLO as a function of strong coupling constant  $\alpha_S \mu R$ , where  $\mu R$  is the renormalization scale. The choice of renormalization and factorization scales will lead to some uncertainty in the predicted cross-sections. Different NLO calculations further differ mainly in their treatment of infrared and collinear divergences.

The H1 [56] and ZEUS [57] collaboration have measured jet production in  $ep$  collisions with real and virtual photons in a large kinematic range. They obtained cross-sections with high accuracy which falls over more than six orders of magnitude as a function of transverse energy. The obtained values of the strong coupling constant  $\alpha_S$  are in agreement with the current world average.

Next-to-leading order QCD calculations describe the jet cross-section in a better manner, with exceptions for forward jets at low momentum transfer  $Q^2$  and  $E_T^{jet}$  and for the direct to resolved ratio of enhanced components in dijet production events.

### Di-Jet in Photon-Photon Collisions

The omni-purpose apparatus for LEP (OPAL) collaboration studied di-jet production in interactions of quasi-real photons (carrying only a small four-momentum  $Q^2 \approx 0$ ) emitted by electron beams at  $e^+e^-$  collider at  $\sqrt{s_{ee}} = 161$  and 172 GeV centre-of-mass energies [58]. They used the cone jet algorithms for the reconstruction of jets. They studied the angular distribution of direct and double-resolved events and compared with the LO and NLO pQCD predictions. They measured cross-section for inclusive two-jet production as

a function of  $E_T^{jet}$  and  $|\eta^{jet}|$  and compared with the calculations of NLO pQCD. The cross-section for inclusive two-jet processes as a function of  $|\eta^{jet}|$  was also compared with the PHOJET and PYTHIA Monte Carlo predictions [59], calculated by using the parameterizations of the parton distributions of photons. The underlying event influences were also studied in order to reduce the modal dependence of the Monte Carlo predicted cross-section.

Inclusive one-jet and two-jet production cross-section in photon-photon collision was previously calculated at Tristan  $e^+e^-$  collider at  $\sqrt{s_{ee}} = 58$  GeV centre-of-mass energy [60] and at LEP  $e^+e^-$  collider at  $\sqrt{s_{ee}} = 130$  and 136 GeV centre-of-mass energy [61].

In the cone jet defining algorithms the total transverse energy  $E_T^{jet}$  of the jets is the scalar sum of the transverse energy of their components within the cone [61]. The transverse energy  $E_{Ti}$  of an  $i^{th}$  particle with respect to the  $z$  axis of the detector, is defined as  $E_{Ti} = E_i \sin \theta_i$ . For an acceptable cone jet, the value of  $E_T^{jet}$  should be greater than a minimum energy  $E_T^{\min}$  certainly. The cone jet algorithms results depend on  $E_T^{\min}$  and the cone size (radius of cone)  $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2}$  with pseudorapidity  $\eta = -\ln[\tan(\theta/2)]$  and azimuthal angle  $\phi$ .

The OPAL Collaboration also studied the jet's internal structure in photon-photon collisions at the hadronic level. The shape of a jet is characterized by the fractions of transverse energy of jet ( $E_T^{jet}$ ) which resides inside the inner cone of radius  $r$  being concentric with the jet defining cone [58]:

$$\psi(r) = \frac{1}{N_{jet}} \sum_{jets} \frac{E_T(r)}{E_T(r-R)} \quad (2.11)$$

where  $E_T(r)$  is the jet's transverse energy inside the inner cone with radius  $r$  and  $N_{jet}$  is the total number of jets. By definition,  $\psi(r=R) = 1$ .

## Multi-Jet Final States

Multi-jet production have been investigated in hadronic final states at HERA and Tevatron colliders, which will also play a central role for physics at the large hadron collider (LHC) [62]. The experimental data for such hadronic final states can be interpreted by perturbative calculation for multi-jet production and by the parton-shower Monte Carlo event simulations. PYTHIA [59] and HERWIG [28], based on the collinear evolution of jets in the initial-state are used to reconstruct the exclusive processes, excluding the finite- $k_T$  contribution that corresponds to implementation of the corrections to the transverse momentum ordering in the parton branching algorithm.

At the LHC, experimental analysis of such multi-jet final states relies on the realistic parton-showers Monte Carlo simulation. Investigation of production of multi-particles at the LHC qualitatively acquires some new features compared to the previous hadron collider experiments due to opening up of the large phase space for events characterization. That will bring in both potentially large radiative corrections and the new effects in the non-perturbative components of the processes being probed near boundaries of the phase-space [62].

F. Hautmann and H. Jung described the  $k_T$ -dependent Monte Carlo showers method [62], which is based upon transverse-momentum dependent (TMD) parton distribution and the matrix elements being defined in high-energy factorizations. This method is advantageous over the standard Monte Carlo generators mainly due to including the corrections to collinear-ordered shower, and inclusion of QCD coherence effects associated with finite-angle radiations from space-like parton that carries the soft longitudinal momentum arbitrarily. Sensitivity to these dynamical features is bound to be enhanced by the high-energy multi-scale kinematics. On the theoretical background of this  $k_T$ -showers method one can go to arbitrarily high transfer-momentum scale, and thus making it feasible for jet physics event simulation at the large hadron collider. The  $k_T$ -dependent shower method [62] can be fully used up to high transfer-momentum scale.

## 2.9 Jet Quenching

Among the other tools like hadronic radiations, electromagnetic radiations, dissociation of the quarkonium states etc. jet quenching is also an important probe to study the properties of QGP [4, 5]. Jet quenching is the result of the energy loss by jets in the medium at partonic level of interactions due to medium induced gluon radiations [4, 63—65]. In order to study the suppression of the high  $p_T$  jets, the nuclear modification factor (NMF) ( $R_{AA}$ ) is usually used. The NMF is defined as the ratio of the yield of particles in nucleus-nucleus collisions to that in the  $pp$  collisions and normalized to the  $N_{coll}$ .

$$R_{AA}(p_T) = \frac{1}{\langle N_{coll} \rangle_C} \times \frac{d^2 N_{AA}^C / dp_T d\eta}{d^2 N_{pp} / dp_T d\eta} \quad (2.12)$$

where  $d^2 N_{AA}^C / dp_T d\eta$  and  $d^2 N_{pp} / dp_T d\eta$  are the differential cross sections of secondary charged particles produced in central nucleus-nucleus and  $pp$ -interactions respectively at the same energy.  $\langle N_{coll} \rangle_c$  is a number of participant nucleons in the central nucleus-nucleus events [66].

Experimental measurements recorded at RHIC [67—71] and LHC [67, 72—83] strongly supports the existence of the QGP. Observation of the jet quenching has been reported by experiments at the RHIC [67, 84—93] and at the LHC [68, 82, 83, 94—105] by measuring the production of high  $p_T$  jets and some other observables. A large ion collider experiment (ALICE) Collaboration at the LHC has recently reported their results for the measurement of jet suppression in central lead-lead (Pb-Pb) collisions at  $\sqrt{s_{NN}} = 2.76$  TeV [67].

For  $pp$  collisions the jet is being determined by production of the high  $p_T$  hadrons and in general this is balanced by the production of another high  $p_T$  hadrons jet in the opposite direction. In case of the nucleus-nucleus ( $AA$ ) collisions, if the primary hard scattering occurs near the edge of the reaction region, the balancing jet has to encounter the dense and hot nuclear medium mostly and thus being quenched [4]. A schematic illustration of this effect is shown in Figure 2.8 below.

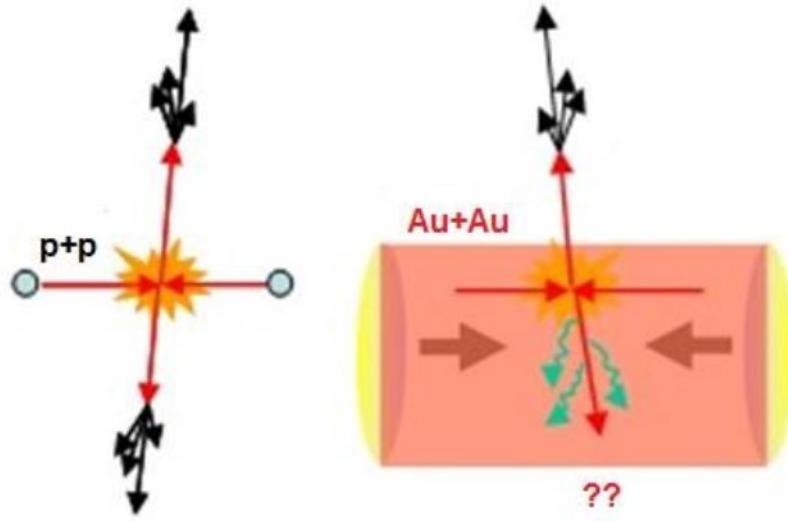


Figure 2.8 A pictorial representation of jet production in  $pp$  collisions (left) and jet production/quenching in nucleus-nucleus ( $AA$ ) (particularly gold-gold ( $AuAu$ )) collisions (right) [106]

The RHIC at brookhaven national laboratory (BNL) reported the study of azimuthal distribution of jet production in gold-gold ( $AuAu$ ), deuteron-gold ( $dAu$ ) and proton-proton ( $pp$ ) collisions at  $\sqrt{s} = 200$  GeV [4]. Considering the azimuthal angle of the near-side hadronic jet to be zero degree, the balancing (away-side) hadronic jet can be clearly observed, both in  $pp$  and  $dAu$  collisions, at  $180^\circ$ . For the case of  $dAu$  collisions, the balancing jet traverses the nuclear medium but there is no significant quenching effect as this  $dAu$  contains normal nuclear matter. Where as, in the case of  $AuAu$  collisions strong suppression of the balancing jet is clearly observed [4, 85, 107, 108]. These results are shown in Figure 2.9.

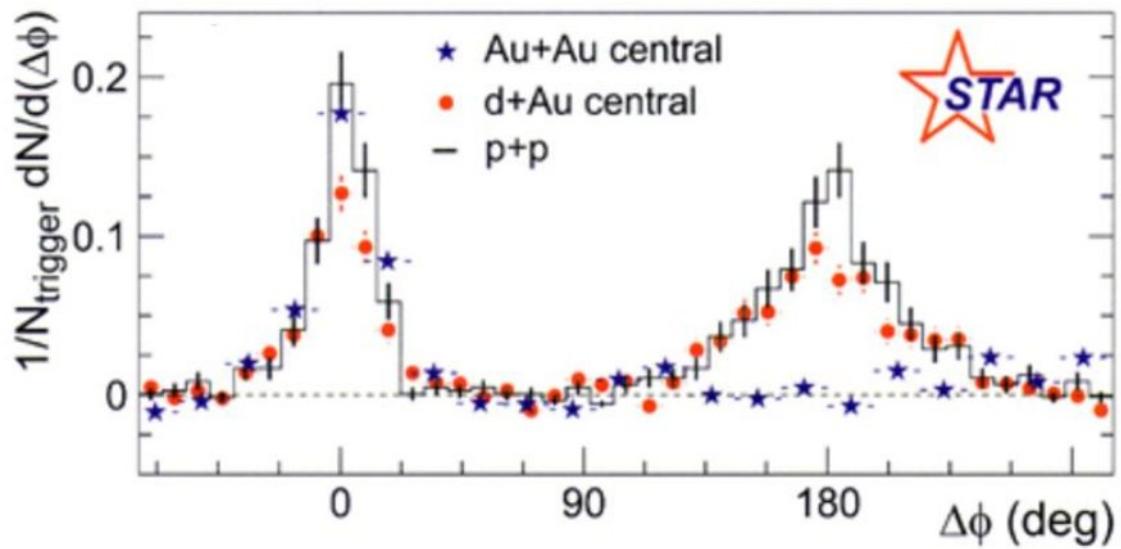


Figure 2.9 Azimuthal angular distributions of the hadrons produced in gold-gold (AuAu), deuteron-gold (dAu) and proton-proton (pp) collisions [4, 85, 107, 108]

## Chapter 3      The Method

In this chapter the methodological procedure for the study of effect of jet production on different parameters of charged particles produced in hadron-hadron collisions at high energy, is briefly described and a detailed and brief description of the HIJING Model, used for event simulation, is also given.

### 3.1   Methodology

We studied the effects of the jet production on the following parameters; the multiplicity ( $N_{ch}$ ), pseudorapidity ( $\eta$ ), transverse momentum ( $p_T$ ) and transverse mass ( $m_T$ ) distributions of secondary charged particles produced in pp-interactions at 1.8 TeV in centre-of-mass system (CMS) frame as a function of different number of jets  $N_{jet}$ . We used the Dubna version of HIJING code, modified by V. V. Uzhinsky [109, 110], for simulation of 100,000 (one hundred thousands) events. These distributions for secondary charged ( $N_{ch}$ ) particles, including protons, charged  $\pi$  ( $\pi^\pm$ ) and charged K – mesons ( $K^\pm$ -meson) were considered. These distributions were considered for different number of jets ( $N_{jet}$ ) and for the whole range and for different regions of the polar angle. The Number of jets was  $N_{jet} = D$  i.e. default values of jets, 0, 1 and 2, and labeled as D, 0, 1 and 2 respectively, as shown in Table 3.1. In the HIJING Model, the parameter for number of jets has default values D which represents the maximum number of jet production; it can be turned off i.e. 0 jets and can be fixed to any number 1, 2, and so on. Different angular regions were selected for six ranges of angle theta  $\theta$  (in degrees): R1 (i.e. Region 1):  $\theta=0^\circ-2^\circ$ , R2:  $\theta=2^\circ-4^\circ$ , R3:  $\theta=4^\circ-6^\circ$ , R4:  $\theta=6^\circ-10^\circ$ , R5:  $\theta=10^\circ-30^\circ$  and R6:  $\theta=30^\circ-90^\circ$ . The reason for selection of these angular intervals R1-R6 was the statistical reliability of the data. We chose this selection of the polar angle regions from analyses of the angular distributions of the secondary charged particles.

Table 3.1 Values used for HIJING parameter for number of jet production, IHPR2(8) which can turned off and can set to any value IHPR2(8)<0 for its absolute values |IHPR2(8)|.

Values of HIJING parameter IHPR2(8)	Number of Jets ( $N_{jet}$ )
D=10 (Default Value)	Maximum number of jets
0	0
-1	1
-2	2

As a first step we analyzed the multiplicity distributions of the charged particles produced in  $pp$ -collisions at 1.8 TeV as a function of  $N_{jet}=D$ , 0, 1 and 2, for full phase space (whole range of the polar angle) and for selected six regions R1—R6 of polar angle. Then we compared our analysis of the multiplicity distributions of charged particles with the analysis by the two component method of the superposition of the two negative binomial (NB) (Pascal) distributions for the experimental multiplicity distributions of charged particles in  $pp\bar{p}$ -collisions at 900 GeV by UA5 collaboration and at 1.8 TeV by Tevatron [111].

Then in continuation and confirmation of the HIJING code results on the influence of the jets on charged particles multiplicities ( $N_{ch}$ ) in  $pp$ -collisions at 1.8 TeV, we carried out a detailed analysis of the pseudorapidity ( $\eta$ ), transverse momentum ( $p_T$ ) and transverse mass ( $m_T$ ) distributions of secondary charged particles produced in  $pp$ -collisions at 1.8 TeV CMS energy as a function of  $N_{jet}$  for the whole range and selected six regions R1—R6 of the polar angle. Concerning the jet dependence of the pseudorapidity of the charged particles we made a qualitative comparison of the HIJING results for the pseudorapidity with the pseudorapidity spectra of the charged particles from the central detector at Fermilab (CDF) collaboration.

The relation that defines the pseudorapidity  $\eta$  is given by equation (2.7) in chapter 2 section 2.6.

Or in terms of the momentum  $\vec{p}$ , the pseudorapidity  $\eta$  can also be written as

$$\eta = \frac{1}{2} \ln \left( \frac{|\vec{p}| + p_L}{|\vec{p}| - p_L} \right) \quad (3.1)$$

where  $p_L$  is the component of the momentum along the beam direction (longitudinal momentum). In the high energy limit where the particle is travelling close to the speed of light, or in the approximation that the mass of the particle is nearly zero, numerically pseudorapidity  $\eta$  is equal to the rapidity  $y$  that is defined by the equation (2.6) in chapter 2 section 2.6.

The transverse momentum is defined by the equation (2.4) in chapter 2 section 2.6, and can also be written as:

$$p_T = p \sin \theta \quad (3.2)$$

The total momentum is given by:

$$p^2 = p_x^2 + p_y^2 + p_z^2 \quad (3.3)$$

with  $p_z$  the longitudinal momentum parallel to the beam ( $z$ -) axis.

The transverse mass is defined by the relation:

$$m_T = \sqrt{m^2 + p_T^2} \quad (3.4)$$

## 3.2 The HIJING Model

The heavy ion jet interaction generator (HIJING), a QCD inspired, Monte Carlo model, written in FORTRAN 77, was developed by M. Gyulassy and Xin-Nian Wang with special emphasis on the role of multiple mini-jets and multi-particle production in hadron-hadron ( $pp$ ), hadron-nucleus ( $pA$ ) and nucleus-nucleus ( $AA$ ) interactions at collider energies. There are some special parameters in HIJING, like energy, frame (LAB: for fixed target experiment or centre of mass system (CMS): for colliding beam

experiment), types of the colliding hadrons or nuclei, their impact parameter and some other parameters regarding the production of jets and other multi-particles, which users have to specify or change. Particularly, HIJING can reproduce many inclusive spectrum, two particle correlations, and can also explain the dependence of the average  $p_T$  on the multiplicity [112—114].

Our choice to use the HIJING model for the analysis is based on the fact that this model is specially designed for the study of multi-particle and multi-jet production in all kind of high energy interactions like  $pp$ ,  $pA$  and  $AA$  which is one of the main advantages of this model over the others which are limited to only some particular hadronic interactions.

The concept of jet production and association of the jets with hard parton scattering is established very well for the hadronic collisions and these jets play an important role in many aspects of the  $pp/ p\bar{p}$  interactions at high energies. At hadron-hadron level of interaction, HIJING play an important role to deal with the interplay between low transverse momentum ( $p_T$ ) non-perturbative physics and the hard perturbative quantum chromodynamics (pQCD) process. HIJING model has been extensively tested for the  $pp$  interactions data for a large range of collision energy [112—114].

In experiments, jets are being identified as showers of the hadrons whose transverse energy  $E_T$  could be reconstructed from the events' calorimetry [115, 116]. However, for the smaller transverse energy  $E_T < 5GeV$  of a jet, it cannot be easily resolved from the underlying background [117], although it could be expected theoretically that the hard parton scatterings should continue for lower  $p_T$ . Usually these are referred to as minijets having too low transverse energy that cannot be experimentally resolved though the related parton scattering process could be calculated in the pQCD framework. Assuming independent production, the importance of the multiple minijets production in  $p\bar{p}$  interactions has been shown to account for the increased total cross section [118].

The HIJING model contains some main subroutines, data blocks and event options and parameters. It contains the following two subroutines being called by users in the program [110, 113].

The first one is the HIJSET subroutine which initializes the HIJING and must be called prior to any other subroutine. In this subroutine the colliding energy and the frame (in fixed target experiment i.e. LAB or in the collider experiment, centre-of-mass system CMS) of the collisions is specified. This also specifies the nature of the projectile and the target whether these are hadrons (protons, neutrons, kaons, pions and their antiparticles) or the nuclei along with their charge and mass numbers.

The second one is the HIJING subroutine which can be repeatedly called after the HIJSET being called one time. This specifies the collisions frame i.e. the LAB or the CMS frame, and minimum and maximum values of the impact parameter which are randomly but evenly selected for hadron-nucleus and nucleus-nucleus collisions. For the case of pp collisions the events are averaged over all impact parameters.

Details about the main data blocks an event options and parameters of the HIJING model can be found in References [110, 113].

## Chapter 4      Results and Discussions

The results obtained for different parameters of charged particles produced in  $pp$ -collisions at 1.8 TeV centre of mass energy using HIJING Model are presented and discussed in this chapter. The HIJING results for multiplicity and pseudorapidity distributions of charged particles are discussed in comparison with some available experimental results from SPS and Tevatron. The analysis presented here is based on the two papers in References [119, 120].

In order to study jet production or jet suppression and its effects on the different parameters of the charged particles produced in high energy collisions, it is useful to know the jet dependence of parameters like charged particles multiplicity, pseudorapidity and transverse momentum etc. in  $pp$ -collisions. Here we present an investigation of the jet dependence of the multiplicity, pseudorapidity, transverse momentum and transverse mass distributions of charged particles produced in  $pp$ -interactions at 1.8 TeV centre-of-mass energy using HIJING Monte Carlo model.

First we present the analysis of the charged multiplicity distributions as a function of  $N_{jet}=D$ , 0, 1 and 2, for whole range and selected six regions R1—R6 of the polar angle [119] and its comparison with analysis of SPS and Tevatron results by two component method [111]. The plots which show any spectra for  $N_{jet}=D$ , 0, 1 and 2 are obtained from the model and are not the experimental results.

### 4.1 The Multiplicity Distributions

Suppression of the jets [63, 64] in the high energy hadronic collisions is one of the clean signals on formation of the new states of strongly interacting matter, the quark gluon plasma (QGP), produced at extreme condition of high temperature and high baryon density. The jet quenching occurs due to the energy loss of jets at parton level [121]. To extract some information about this effect, the nuclear modification factor (NMF) is usually used as a function of the transverse momentum  $p_T$  [88, 122, 123]. The NMF is defined as

$$R_{AA}(p_T) = \frac{1}{\langle N_{coll} \rangle_C} \times \frac{d^2 N_{AA}^C / dp_T dy}{d^2 N_{pp} / dp_T dy} \quad (4.1)$$

where  $d^2 N_{AA}^C / dp_T dy$  and  $d^2 N_{pp} / dp_T dy$  are the differential cross sections of secondary charged particles produced in central nucleus-nucleus and pp-interactions respectively at the same energy.  $\langle N_{coll} \rangle_C$  is a number of participant nucleons in the central nucleus-nucleus events [66], which could be defined using the Glauber approximation [124]. To study the jet suppression effect in hot and dense matter it is necessary to get full information on the jet production in *pp*-interactions. It is of great importance to understand how jet production can change the characteristics of the secondary particles produced in *pp*-collisions. Apparently it is not simple question to get complete information on the jet production in *pp*-collisions at any energy. It will be very interesting to analyze the jet production in conditions of  $4\pi$  geometry measurements to see full picture of the interactions.

Modern simulation packages give possibilities to analyze the interactions under necessary conditions of  $4\pi$  geometry measurements. In this section we present the study of the jet production in ultrarelativistic *pp*-collisions using heavy ion jet interaction generator (HIJING) Monte Carlo model [112—114].

In paper, by Roberto Ugoccioni and Alberto Giovannini [111], the multiplicity distribution (MD) of the secondary charged particles produced in the  $p\bar{p}$  collisions at 900 GeV from UA5 collaboration [125, 126] is described by the weighted superposition of two negative binomial (NB) (Pascal) multiplicity distribution (see Figure 4.1).

The negative binomial Pascal multiplicity distribution for two-parameters can be expressed as:

$$P_n^{(Pascal)}(\bar{n}, k) = \frac{k(k+1)\dots(k+n-1)}{n!} \frac{\bar{n}^n k^k}{(\bar{n}+k)^{n+k}} \quad (4.2)$$

Where  $\bar{n}$  is the average value of the multiplicity and  $\frac{1}{k}$  is the measure of the deviation of the variance  $D^2 = \langle n^2 \rangle - \bar{n}^2$  from Poisson shape  $\frac{1}{k} + \frac{1}{n} - \frac{D^2}{\bar{n}^2}$ . Actually for the case of Poisson distribution where  $k \rightarrow \infty$ ,  $D^2 = \bar{n}$  and in case of geometric distribution where  $k = 1$ ,  $D^2 = \bar{n} + \bar{n}^2$ .

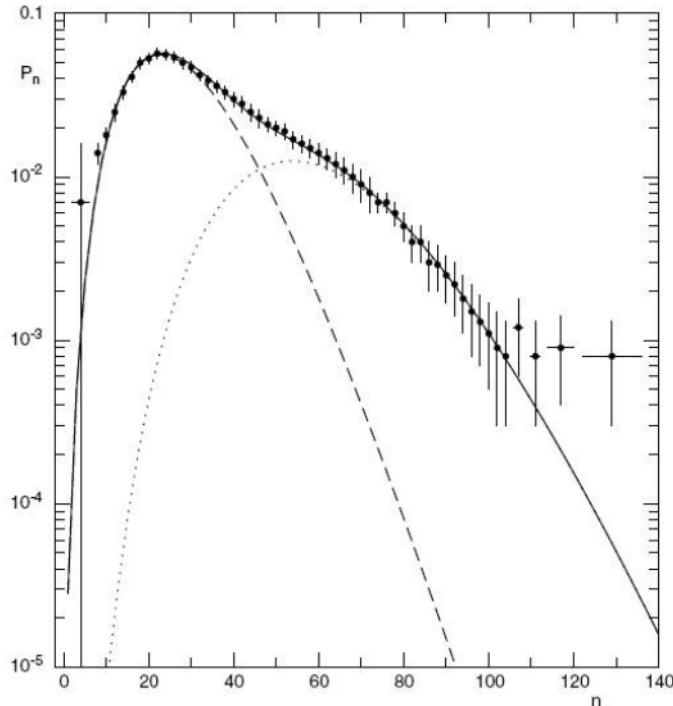


Figure 4.1 Multiplicity distribution for charged particles produced in the  $p\bar{p}$  reaction at 900 GeV obtained by the UA5 collaboration. The lines are the result of fitting [111].

The distribution shows two regions in the behavior of the multiplicity distribution:  $10 < n < 60$  and  $60 < n < 120$ ; semi hard and soft events. The multiplicity distribution of each class can be described well by the Pascal distribution, which itself could not reproduce the shoulder structure appeared in the UA5 results at 900 GeV. For Fermilab results they found for E735 data (Figure 4.2) that the soft component satisfies the Koba-Nielsen-Olesen (KNO) scaling [127, 128] and hard one does not.

According to the Polyakov and Koba-Nielsen-Olesen hypothesis, at extremely high energy  $s$  the probability  $P_n(s)$  of  $n$  particles production in a particular interaction must exhibit the following relation:

$$P_n(s) \sim \frac{1}{\langle n(s) \rangle} \psi(z) \quad (4.3)$$

where  $z = \frac{n}{\langle n(s) \rangle}$  is the scaled multiplicity with  $\langle n(s) \rangle$  as average values of the secondary particles multiplicity at the colliding energy  $s$ . According to this scaling hypothesis if  $P_n(s)$  for different values of  $s$  is rescaled by stretching the horizontal or vertical axis with average values  $\langle n(s) \rangle$  then the rescaled distributions will coincide. Which means that the multiplicity distributions get simply rescaled copies of the universal scaling function  $\psi(z)$ , and depend only on the  $z = \frac{n}{\langle n(s) \rangle}$  [127, 128].

They concluded that the weighted superposition mechanism of two negative binomial (Pascal) distributions describe well the multiplicity distributions in pp collisions. In hadronic collisions, the two components correspond to soft events and to semi-hard events respectively. Based on this mechanism, the knowledge of the features of multiplicity distributions up to 900 GeV centre of mass energy has been used to predict the characteristic behavior expected in the TeV energy range: the soft component satisfies KNO scaling, while the semi-hard one violates it strongly [111].

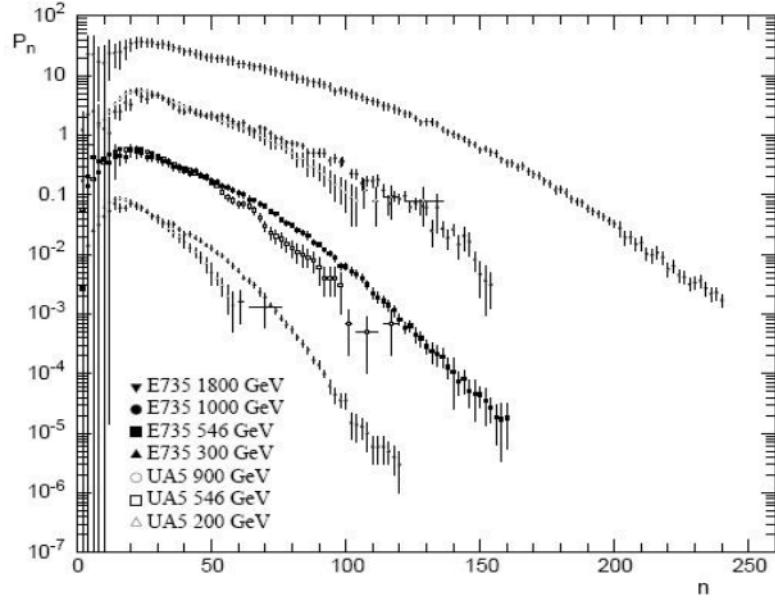


Figure 4.2 Multiplicity distribution of secondary charged particles in the  $p\bar{p}$  reactions at Tevatron energies obtained by the E735 [111, 129, 130].

## 4.2 Simulation Results for $N_{ch}$ in $pp$ -Interactions at 1.8 TeV

We have analyzed multiplicity distributions of the secondary charged particles produced in  $pp$ -collision at 1.8 TeV centre of mass system (CMS) energy. Dubna version of HIJING code (modified by V. V. Uzhinsky [109, 110]) is used for 100,000 (one hundred thousands) events. The multiplicity distribution of secondary charged ( $N_{ch}$ ) particles, including protons, charged  $\pi$  ( $\pi^\pm$ ) and charged  $K$  – mesons ( $K^\pm$ -meson) is considered. The  $N_{ch}$ -distributions were considered for different number of jets ( $N_{jet}$ ) and for different locations of jets i.e. different polar angle ranges. Number of jets was  $N_{jet} = D$  i.e. default values of jets, 0, 1 and 2 (and labeled as D, 0, 1 and 2 respectively). Different angular regions were selected for six ranges of angle theta  $\theta$  (in degree): 0-2 (R1 i.e. region 1), 2-4 (R2), 4-6 (R3), 6-10 (R4), 10-30 (R5) and 30-90 (R6).

Figure 4.3 shows the multiplicity distribution of secondary charged particles produced in  $pp$  interaction at 1.8 TeV. The model gives three regions in contrast to the experiment having two regions only (see Figure 4.1). It is connected with elastic

scattering and diffractive events in the model that result in the leading particle effect [131-135]. The first region corresponds to the values of multiplicity for  $N_{ch} < 15$ ; second one is for  $15 < N_{ch} < 80$  and third for  $N_{ch} > 80$ . Figure 4.3 shows that the first region is formed mainly due to the events with 0 jet (here we have sharp peak), second one is contributed by multi-jet events along with zero jet events and third region is contributed only due to multi-jet events. So the analyses demonstrate that jet production can change the behavior of  $N_{ch}$ -distribution in various regions of multiplicity differently. The model data demonstrate that multijet cases will influence essentially in high multiplicity area ( $N_{ch} > 120$ ). As we have mentioned above that second and the third regions were described by the weighted superposition of two negative binomial (NB) (Pascal) multiplicity distribution [111].

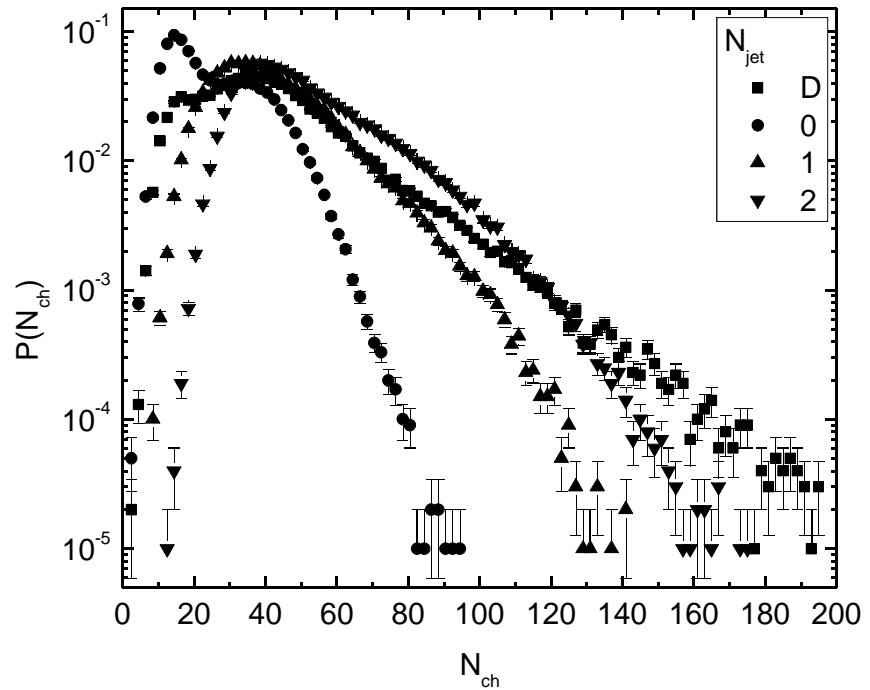


Figure 4.3 The multiplicity distribution of  $N_{ch}$  for  $N_{jet} = D, 0, 1$  and  $2$  for whole range of polar angle.

Now let us consider that how the jet production will influence the angular distributions of particles. Figures 4.4—4.9 demonstrate the  $N_{ch}$ —distributions for charged particles produced in pp-interaction at  $\sqrt{s}=1.8$  TeV. We have simulated 100,000 (one hundred thousands) events with  $N_{jet}=0, 1$  and  $2$ , for different regions of angles from R1 to R6.

Figure 4.4 shows that jet production do not influence essentially the multiplicity distribution. The result can be explained in the following way. Since the first angular region  $\theta = 0^\circ - 2^\circ$  - R1 mainly consists of particles with high longitudinal momentum but the jets are high  $p_T$  particles. This figure also indicates that the first peak in the Figure 4.3 is mainly due to the events with  $N_{jet}=0$ .

The Figures 4.5—4.9 (R2—R6) show that with increasing the polar angle of the particles the jet production changes essentially the multiplicity spectrum of the particles (as observed in Figure 4.3) in the regions  $15 < N_{ch} < 80$  and  $N_{ch} > 80$ .

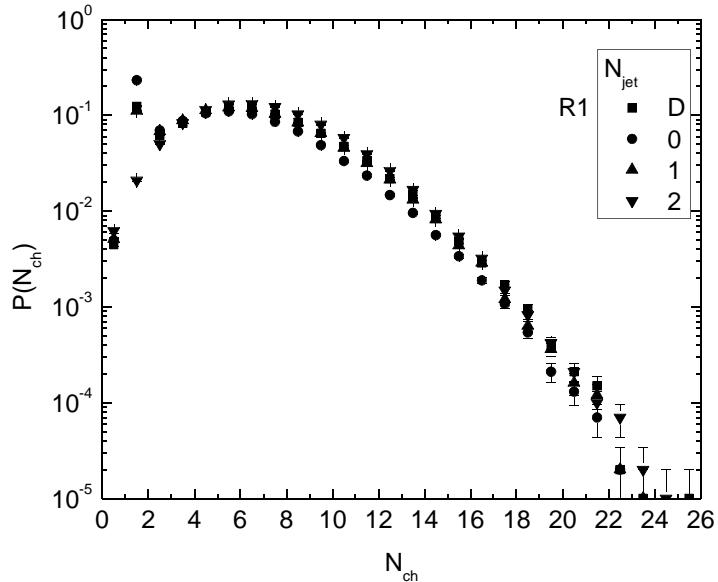


Figure 4.4 The multiplicity distribution of charged particles for  $N_{\text{jet}} = D, 0, 1$  and  $2$  in angular region R1 0-2 degree.

The Figure 4.5 for angular region R2  $\theta=2-4^\circ$  shows that jets influence the multiplicity in this region. Increasing the polar angle thus increases the  $p_T$  of particles contributing jets. It can also be seen that multiplicity is affected (increased) by 1, 2 and default jet events as compared to 0 jet events. This increasing effect in multiplicity can also be seen for next angular region R3  $\theta=4-6^\circ$  shown in Figure 4.6. But here 2 and default jet events has more increasing effect on multiplicity as compared to the 1 and 0 jet events. Figure 4.7 for angular region R4  $\theta=6-10^\circ$  shows a similar behavior as was observed in Figure 4.6 but with a more increase in multiplicity. This trend continued in the last two angular regions: Figure 4.8 for R5  $\theta=10-30^\circ$  and Figure 4.9 for R6  $\theta=30-90^\circ$ . Since these are also large  $p_T$  particles regions, therefore by increasing the polar angle the multiplicity with increasing number of jets is much more increased as compared to other regions. These angular regions also show that these have more contribution to change (increase) the multiplicity as is also evident in last two regions of Figure 4.3.

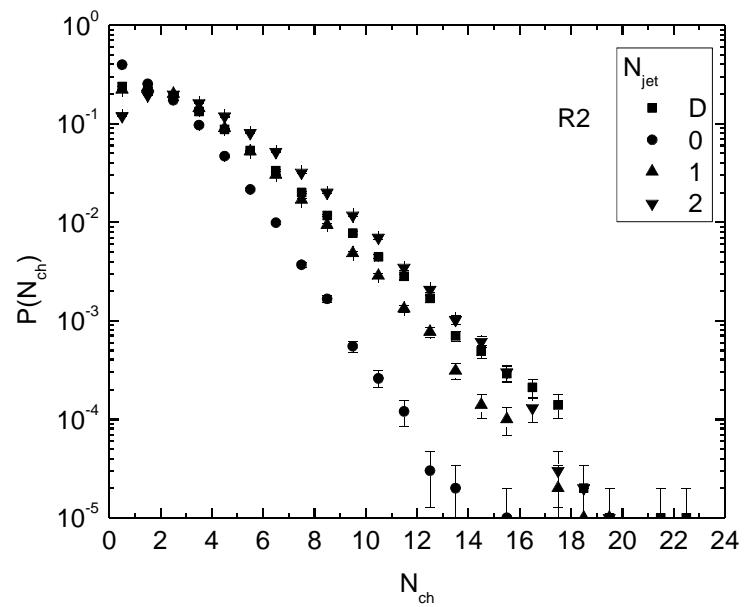


Figure 4.5 The multiplicity distribution of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in angular region R2 2-4 degree.

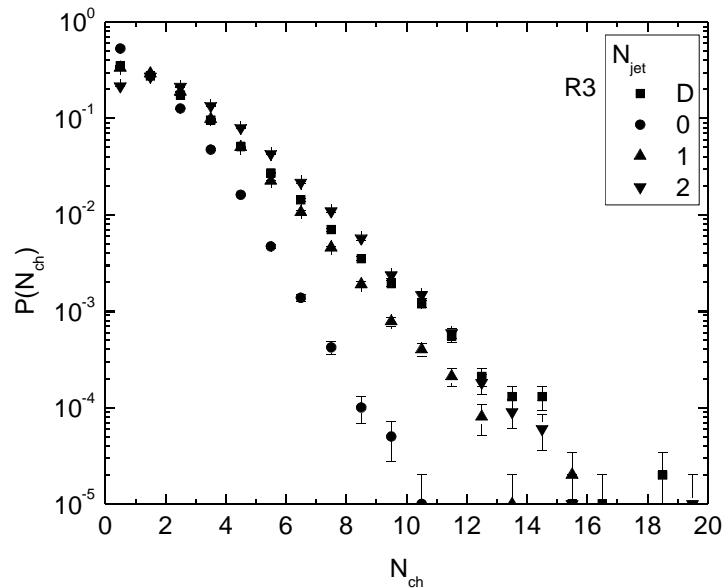


Figure 4.6 The multiplicity distribution of charged particles for  $N_{jet}= D$ , 0, 1 and 2 in angular region R3 4-6 degree.

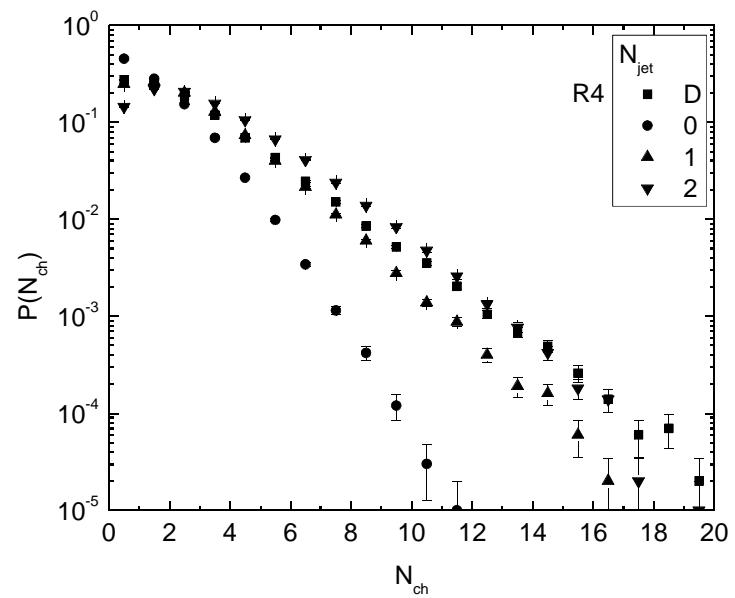


Figure 4.7 The multiplicity distribution of charged particles for  $N_{jet} = D, 0, 1$  and  $2$  in angular region R4 6-10 degree.

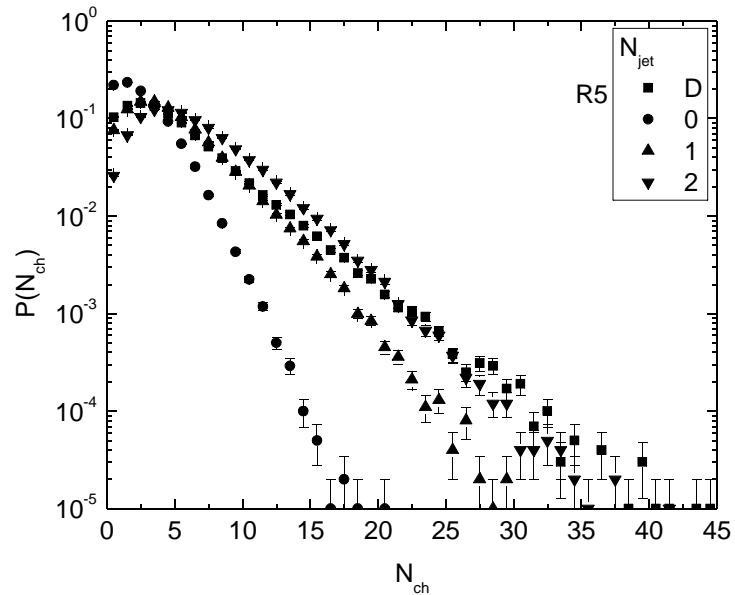


Figure 4.8 The multiplicity distribution of  $N_{ch}$  for  $N_{jet} = D, 0, 1$  and  $2$  in angular region R5 10-30 degree.

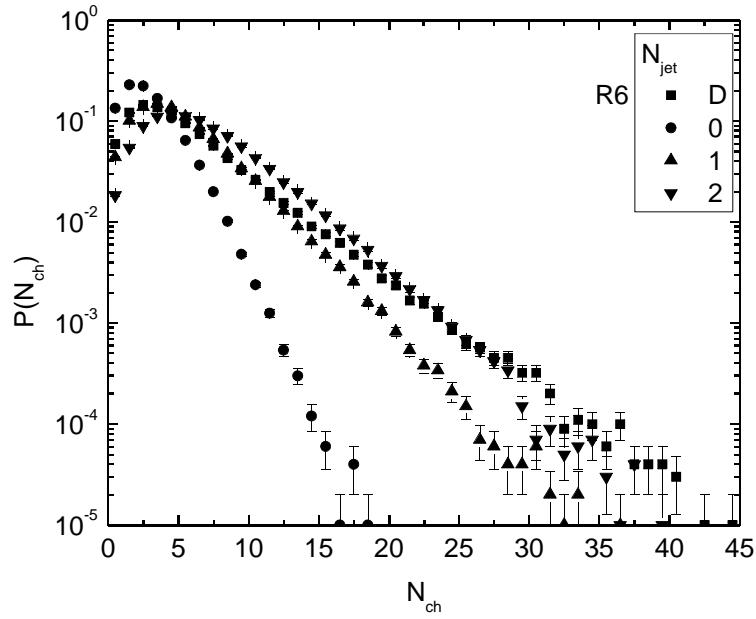


Figure 4.9 The multiplicity distribution of charged particles for  $N_{\text{jet}} = D, 0, 1$  and  $2$  in angular region R6 30-90 degree.

For this section we conclude that the simulation data coming from the HIJING code show that there are three areas in multiplicity distributions of secondary charged particles:  $N_{\text{ch}} < 15$ ,  $15 < N_{\text{ch}} < 80$  and  $N_{\text{ch}} > 80$ . We identified the first area as a region dominating leading particles: elastic scattering region. The particles from this area correspond to the polar angle region 0-2 degree and without jets. The second region corresponds mainly to multi-jet events along with contribution from the zero jet events. The third area corresponds mainly to multi-jet (1, 2 or more jets) events. Analysis of the multiplicity distributions for other angular regions (2-90 degrees) also showed that the increase in the charged particles multiplicity is connected to the multi-jet events in the  $pp$  collisions at TeV energy scale. So we could conclude that for the HIJING simulation results for  $pp$  collisions at TeV energy scale, in the multiplicity distributions for full polar angle range first area corresponds mainly to leading particles, second area corresponds mainly to multi-jet events along with zero jet events and third area corresponds mainly to

multi-jet events as these areas has a similar description in the weighted superposition mechanism of two negative binomial multiplicity distributions for hadronic collisions where the two components correspond to soft and semi-hard events respectively.

### 4.3 Simulation Results for $\eta$ , $p_T$ and $m_T$ in $pp$ Interactions at 1.8 TeV

Now in the following three sections we present the study which is a continuation and confirmation of the HIJING code results, presented above, on the influence of the jets on charged particles multiplicities ( $N_{ch}$ ) in  $pp$ -collisions at 1.8 TeV [119], where we presented and discussed the increase observed in  $N_{ch}$  as a function of different number of jets for charged particles distributions in full phase space (whole polar angle rage) and for six different regions of the polar angle  $\theta$  (R1:  $\theta=0-2^\circ$ , R2:  $\theta=2-4^\circ$ , R3:  $\theta=4-6^\circ$ , R4:  $\theta=6-10^\circ$ , R5:  $\theta=10-30^\circ$  and R6:  $\theta=30-90^\circ$ ). The results of distributions of  $N_{ch}$  for zero and multi-jet events were found to be inconsistent with the experimental multiplicity distributions (MDs) of charged particles interpreted by fitting with the Pascal (negative binomial) distributions [111].

Lets discuss the results for the effects of jet production on pseudorapidity ( $\eta$ ), transverse momentum ( $p_T$ ) and transverse mass ( $m_T$ ) distributions of secondary charged particles as a function of  $N_{jet}=D$ , 0, 1 and 2 for the whole polar angle range and also for six selected regions of polar angle R1 to R6 [120]. The parameters pseudorapidity  $\eta$  and transverse momentum  $p_T$  are defined by equations (2.7) and (2.4) respectively in chapter 2, section 2.6, and transverse mass  $m_T$  is defined by the equation (3.4) in chapter 3 section 3.1. Here, we have studied the results for  $\eta$ -,  $p_T$ - and  $m_T$ -distributions of secondary charged particles for the whole polar angle range and for six regions in comparison with the reported results for change (increase) in multiplicity of  $N_{ch}$  in multi-jet events [119]. Moreover, these results are discussed in connection with the experimental results for pseudorapidity distributions of charged particles from the Collider Detector at Fermilab (CDF Collaboration) [136].

We have analyzed  $\eta$ -,  $p_T$ - and  $m_T$ -distributions of the secondary charged particles produced in  $pp$ -collisions at 1.8 TeV centre of mass energy. The Dubna version of the HIJING code (modified by Uzhinsky [109, 110]) is used for simulation of 100,000 events. These distributions of secondary charged particles, including protons, charged  $\pi$  ( $\pi^\pm$ ) and charged  $K$  – mesons ( $K^\pm$ -meson) are considered. These distributions are considered for different numbers of jets ( $N_{jet}$ ) for the whole range of the polar angle as well as in its different regions. The number of jets was  $N_{jet}=D$ , i.e. the default value of jets (maximum number) taken from the HIJING model, 0, 1 and 2 (and labeled as D, 0, 1 and 2 respectively). Different angular regions were selected for six ranges of the polar angle theta  $\theta$  (in degrees) from R1 to R6.

#### 4.4 The Pseudorapidity Distributions

The pseudorapidity distribution of charged particles (for example in the range  $0 < \eta < 8$ ) produced in  $pp$ -collisions at 1.8 TeV, as a function of number of jets  $N_{jet}=D$ , 0, 1 and 2, is shown in Figure 4.10. This figure shows some plateaus for the central pseudorapidity regions (in the area about  $0 < \eta < 4$ ).

The existence of plateaus in rapidity or pseudorapidity is very important for theoretical estimation. For example, J. D. Bjorken described the space-time evolution of the hadronic matter produced in the central rapidity region in extreme nucleus-nucleus collisions [137]. He found that quark-gluon plasma is produced at a temperature of the order of 200 MeV, which was in agreement with previous measurements [138]. The author also commented that the description relies on the existence of a flat central plateau and on the applicability of hydrodynamics.

Here in Figure 4.10, one can see that with increasing number of jets:

- the width of the distribution/plateaus is decreased,
- the pseudorapidity density in the central area is increased.

- the pseudorapidity spectrum for  $N_{jet}=2$  events are systematically higher than that of  $N_{jet}=0$  events, which shows that 2 (multi)-jet events lead to an increase in the pseudorapidity density.

The existence of the plateaus in the rapidity/pseudorapidity distributions is also important for the applicability of hydrodynamics. According to the Bjorken model [137], usually used to estimate the QGP parameters, the density of energy (transverse flow neglected) is given by the relation

$$\varepsilon_{BJ} = \frac{\text{Energy}}{\text{Volume}} = \frac{\frac{dE_T}{d\eta}}{\pi R_0^2 A^{2/3} c \tau_0} = \frac{m_T \frac{dN}{d\eta}}{\pi R_0^2 A^{2/3} c \tau_0} \quad (4.4)$$

where  $\pi R_0^2 A^{2/3}$  is the transverse size of the smallest nucleus;  $\tau_0 \sim 1 \text{ fm}/c$  is formation time and  $\frac{dE_T}{d\eta} m_T \frac{dN}{d\eta}$  is mean energy of the particle, multiplied by the number of particles;  $m_T = \sqrt{m^2 + p_T^2}$  is transverse mass (or energy). In this model if the mean free path is  $\sim 0.5 \text{ fm}$  then  $\varepsilon_{BJ} \sim 2 \text{ GeV/fm}^3$ .

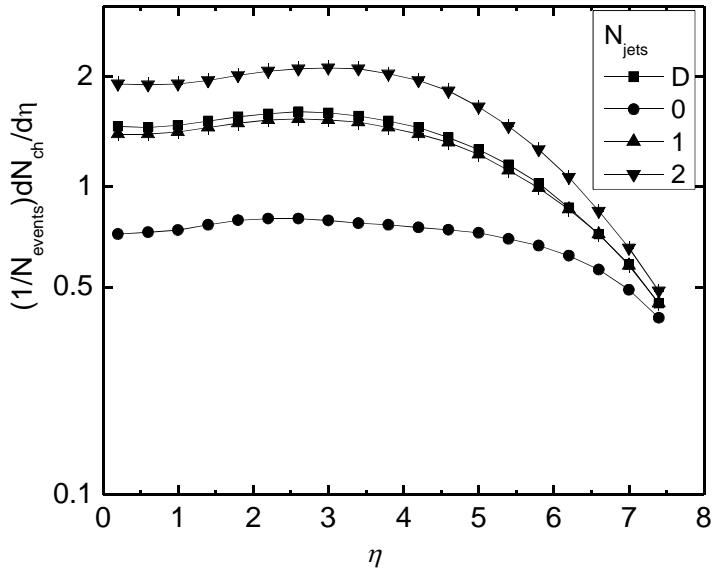


Figure 4.10 The  $\eta$ -distributions of charged particles produced in  $pp$  collisions at 1.8 TeV for  $N_{jet}=D, 0, 1$  and  $2$ .

In Figure 4.11 the data are presented for the corrected  $\eta$  distributions (corrected for geometric and kinematic acceptance, tracking efficiency etc.) of charged particles produced in proton-antiproton collisions at  $\sqrt{s}=1800$  and 630 GeV from the collider detector at Fermilab [136]. A measurement from the CERN SPS collider performed by UA5 at  $\sqrt{s}=546$  GeV is also shown in this figure. A qualitative comparison of these data with those from Figure 4.10 for the pseudorapidity region  $|\eta| \leq 3.5$  demonstrates that as the  $\eta$  spectra for CDF Tevatron data are much higher than those for the HIJING ( $N_{jet}=2$ ) data, this increase in pseudorapidity density is due to multi-jet events.

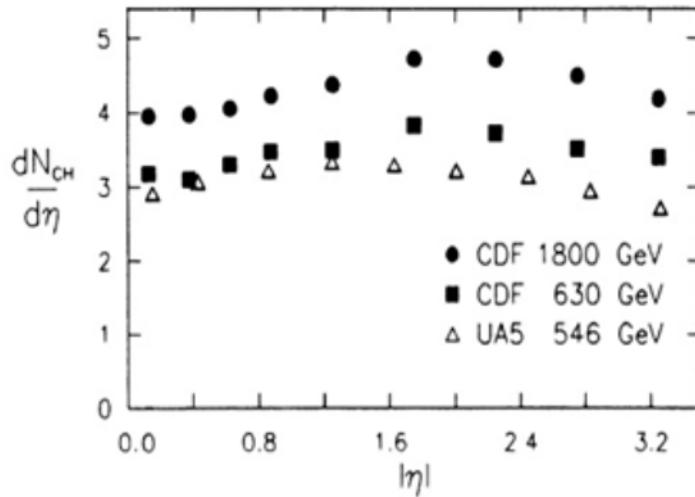


Figure 4.11 The pseudorapidity density measured by the CDF collaboration at 1800 and 630 GeV, and by the UA5 collaboration at 546 GeV [136].

As the polar angle for zero to 90 degrees correspond to the pseudorapidity region  $\sim 8$  to zero, so the pseudorapidity spectra for six regions of polar angle R1 to R6 are also included in Figure 4.10.

## 4.5 The Transverse Momentum Distributions

In Figure 4.12 and Figures 4.13 to 4.18 the transverse momentum  $p_T$  distributions of secondary charged particles produced in  $pp$ -interactions at 1.8 TeV as a function of number of jets  $N_{jet}=D$ , 0, 1 and 2, are presented, for the whole range and for the six selected regions (R1 to R6) of the polar angle. We can see that with increasing the number of jets from 0 to 1, 2 or with the default values of jets the transverse momentum is increased as the jets or multi-jet events contain high  $p_T$  particles.

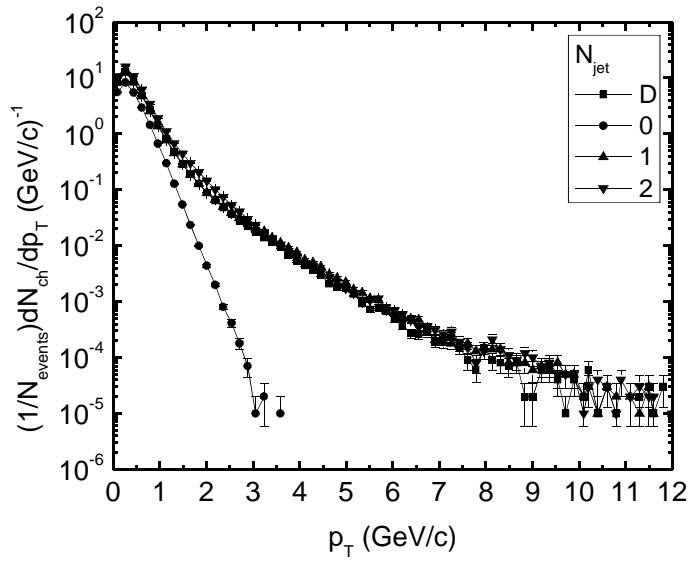


Figure 4.12  $p_T$  distribution of charged particles for  $N_{jet}=D$ , 0, 1 and 2 for the whole range of polar angle.

The shape of the distributions in the case of  $N_{jet} \geq 1$  is different in two areas of  $p_T$ :  $p_T < 2$  GeV/c and  $p_T > 2$  GeV/c. The slopes of the distributions in the first area are very close to that of the events with  $N_{jet}=0$  (slopes of the  $p_T$  distributions for the whole  $\theta$ -range and for regions R1-R6 are shown in Tables 4.1 and 4.2 and plotted in Figure 4.19). So we could say that particles with  $p_T < 2$  GeV/c are produced by the same dynamics in events with different  $N_{jet}$ , i.e. there is no jet dependence in the  $p_T < 2$  GeV/c region (or zero-jet events have no contribution to the  $p_T > 2$  GeV/c region). The particles with  $p_T > 2$  GeV/c are those produced by some special dynamics, different from the particles produced with  $p_T < 2$  GeV/c; namely, the jet dynamics (production and hadronization of the jets) from the HIJING code. In our previous study [119] we also observed two regions for the multiplicity distribution of charged particles. We concluded that the high multiplicity regions in the  $N_{ch}$ -distribution correspond to the multi-jet events. The results were in good agreement with those discussed by Ugoccioni and Giovannini [111].

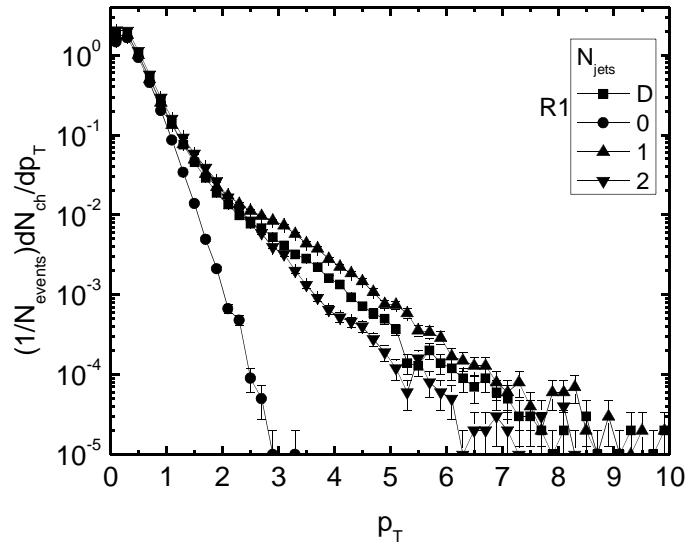


Figure 4.13  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R1  $\theta=0-2^\circ$ .

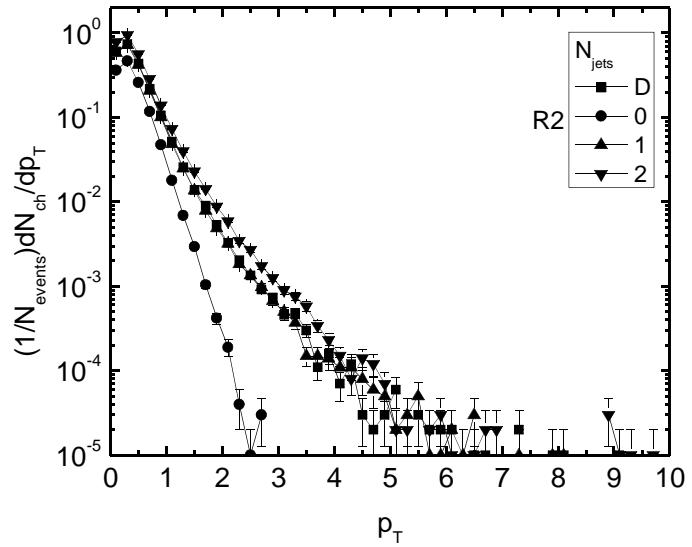


Figure 4.14  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R2  $\theta=2-4^\circ$ .

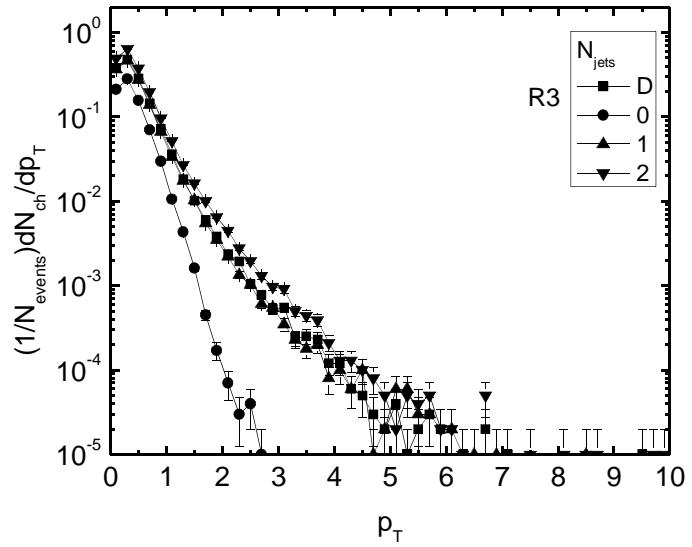


Figure 4.15  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R3  $\theta=4\text{--}6^\circ$ .

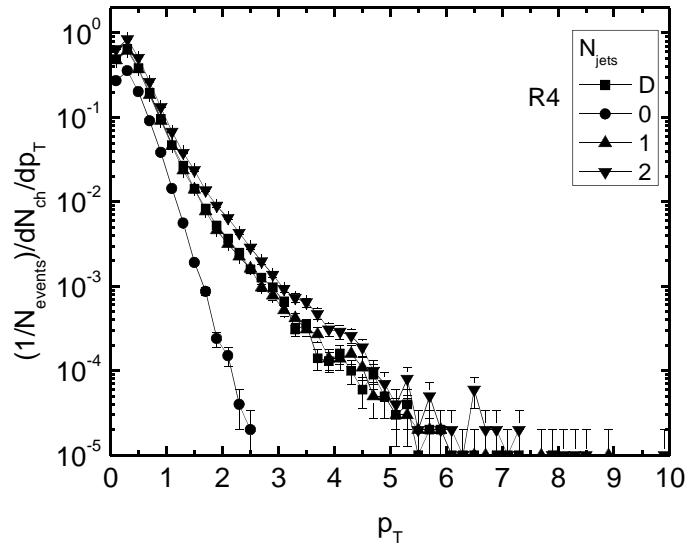


Figure 4.16  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R4  $\theta=6\text{--}10^\circ$ .

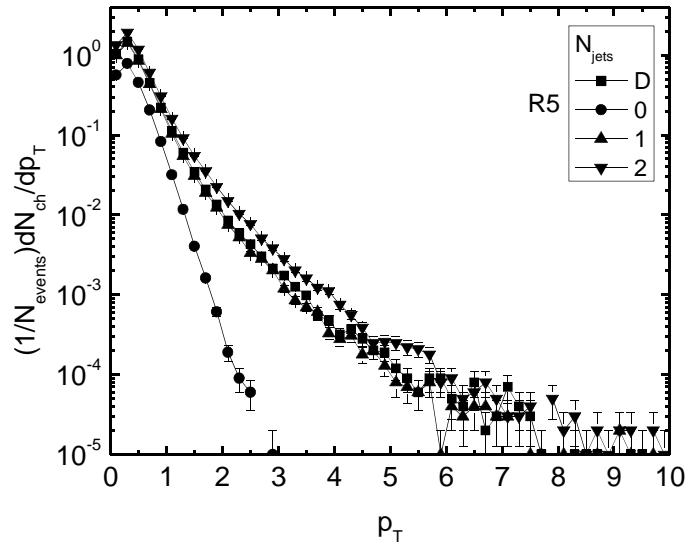


Figure 4.17  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R5  $\theta=10-30^\circ$ .

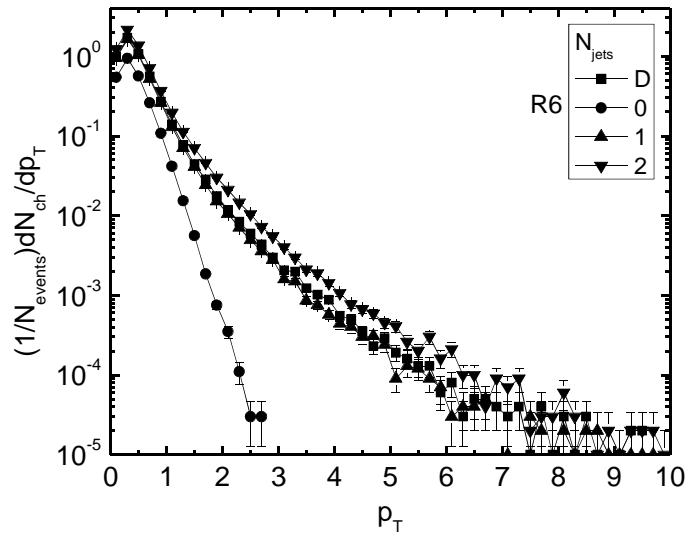


Figure 4.18  $p_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R6  $\theta=30-90^\circ$ .

Figures 4.13 to 4.18 demonstrate how the increase in values of the  $p_T$  spectra depends on the polar angle of the produced charged particles (as  $p_T \propto p \sin \theta$ ). This shows the dependence of the variation in the  $p_T$  spectra with respect to the polar angle (the angular regions R1—R6) and its dependence on  $N_{jets}$ .

The slopes parameters obtained by using the exponentially decaying fit function  $e^{-bx}$  with  $b$  as the slope parameter, for transverse momentum distributions for the whole range and for selected six regions R1—R6 of polar angle in the  $p_T$  regions  $p_T < 2\text{GeV}/c$  and  $2\text{GeV}/c < p_T < 3\text{GeV}/c$  are listed in Tables 4.1 and 4.2 respectively.

Table 4.1 Slopes of the  $p_T$  spectra for the whole range and selected regions R1—R6 of the polar angle for  $p_T < 2\text{GeV}/c$

Polar Angle $\theta$	$N_{jet}=D$	$N_{jet}=0$	$N_{jet}=1$	$N_{jet}=2$
whole range	$3.10 \pm 2.61\text{E-}4$	$3.80 \pm 2.72\text{E-}4$	$3.13 \pm 2.62\text{E-}4$	$3.03 \pm 2.48\text{E-}4$
R1 $\theta=0^\circ-2^\circ$	$3.25 \pm 7.07\text{E-}4$	$3.61 \pm 5.33\text{E-}4$	$3.30 \pm 7.15\text{E-}4$	$3.23 \pm 6.88\text{E-}4$
R2 $\theta=2^\circ-4^\circ$	$3.28 \pm 1.02\text{E-}3$	$3.80 \pm 9.25\text{E-}4$	$3.31 \pm 1.02\text{E-}3$	$3.19 \pm 9.64\text{E-}4$
R3 $\theta=4^\circ-6^\circ$	$3.20 \pm 1.32\text{E-}3$	$3.81 \pm 1.16\text{E-}3$	$3.24 \pm 1.32\text{E-}3$	$3.15 \pm 1.21\text{E-}3$
R4 $\theta=6^\circ-10^\circ$	$3.20 \pm 1.15\text{E-}3$	$3.81 \pm 1.06\text{E-}3$	$3.21 \pm 1.15\text{E-}3$	$3.11 \pm 1.06\text{E-}3$
R5 $\theta=10^\circ-30^\circ$	$3.18 \pm 7.67\text{E-}4$	$3.80 \pm 6.9\text{E-}4$	$3.21 \pm 7.63\text{E-}4$	$3.07 \pm 7.22\text{E-}4$
R6 $\theta=30^\circ-90^\circ$	$3.07 \pm 7.55\text{E-}4$	$3.71 \pm 6.55\text{E-}4$	$3.11 \pm 7.47\text{E-}4$	$3.08 \pm 7.23\text{E-}4$

Table 4.2 Slopes of the  $p_T$  spectra for the whole range and selected regions R1—R6 of the polar angle for  $2\text{GeV}/c < p_T < 3\text{GeV}/c$

Polar Angle $\theta$	$N_{jet}=D$	$N_{jet}=0$	$N_{jet}=1$	$N_{jet}=2$
whole range	$1.87 \pm 0.01$	$4.61 \pm 0.01$	$1.77 \pm 0.02$	$1.95 \pm 0.01$
R1 $\theta=0^\circ-2^\circ$	$1.17 \pm 0.06$	$3.99 \pm 0.05$	$0.76 \pm 0.14$	$1.68 \pm 0.02$
R2 $\theta=2^\circ-4^\circ$	$1.98 \pm 0.04$	$4.64 \pm 0.07$	$1.99 \pm 0.04$	$1.93 \pm 0.03$
R3 $\theta=4^\circ-6^\circ$	$1.96 \pm 0.05$	$4.58 \pm 0.06$	$1.93 \pm 0.05$	$1.97 \pm 0.04$
R4 $\theta=6^\circ-10^\circ$	$1.77 \pm 0.04$	$4.44 \pm 0.06$	$1.88 \pm 0.05$	$2.10 \pm 0.03$
R5 $\theta=10^\circ-30^\circ$	$1.67 \pm 0.04$	$4.14 \pm 0.07$	$1.79 \pm 0.03$	$1.89 \pm 0.02$
R6 $\theta=30^\circ-90^\circ$	$1.85 \pm 0.03$	$4.22 \pm 0.05$	$1.86 \pm 0.03$	$1.84 \pm 0.02$

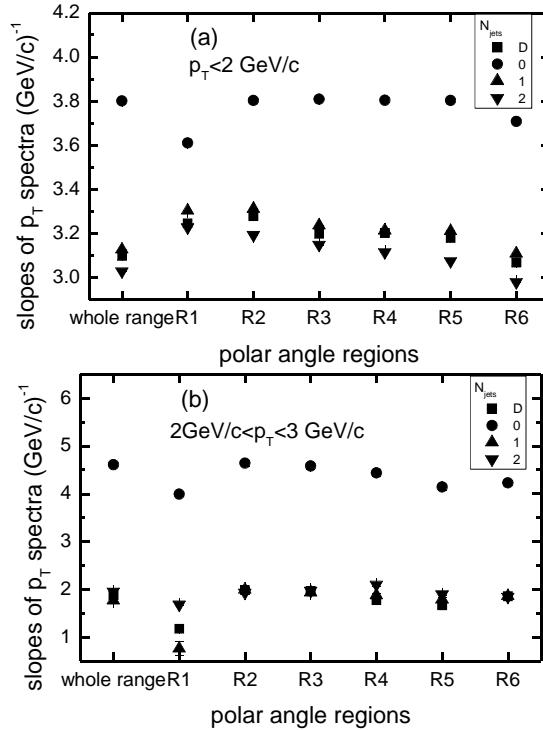


Figure 4.19 Slopes of the  $p_T$  spectra for the whole range and selected regions R1-R6 of the polar angle, (a) for  $p_T < 2 \text{ GeV}/\text{c}$  and (b) for  $2 \text{ GeV}/\text{c} < p_T < 3 \text{ GeV}/\text{c}$

In Figure 4.19 ((a) and (b)), plots are shown for the slopes of the  $p_T$  spectra for the whole range and selected six regions R1-R6 of the polar angle for  $p_T < 2 \text{ GeV}/\text{c}$  and for  $2 \text{ GeV}/\text{c} < p_T < 3 \text{ GeV}/\text{c}$  as a function of  $N_{\text{jets}}$ . This supports the analysis described above for the  $p_T$  spectra.

## 4.6 The Transverse Mass Distributions

We now consider the transverse mass  $m_T$  distributions of secondary charged particles produced in  $pp$ -interactions at 1.8 TeV as a function of number of jets  $N_{jet}=D$ , 0, 1 and 2, for the whole range and the six selected regions (R1 to R6) of the polar angle. It is well known that the  $m_T$  distributions are more sensitive to the temperature of the systems. Figure 4.20 shows the  $m_T$  distributions of secondary charged particles produced in  $pp$ -interactions at 1.8 TeV for  $N_{jet}=D$ , 0, 1 and 2 for the whole polar angle range. With increasing the number of jets from 0 to 1, 2 or the default value of jets, an increase in the transverse mass is observed and here the increase in the case of multi-jet events is more than for the transverse momentum distributions as transverse mass is  $m_T = \sqrt{m^2 + p_T^2}$ .

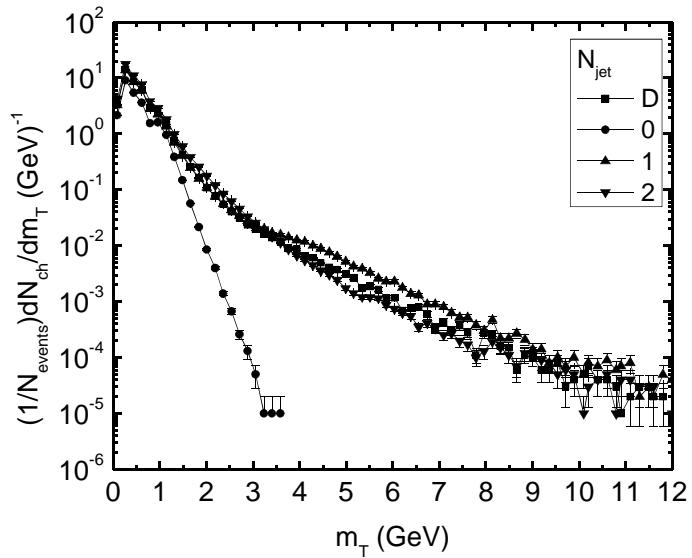


Figure 4.20  $m_T$  distribution of charged particles for  $N_{jet}=D$ , 0, 1 and 2 for the whole range of polar angle.

Transverse mass distributions of secondary charged particles for  $pp$ -collisions at 1.8 TeV, for the six selected regions (R1—R6) of polar angle, are shown in Figures 4.21 to 4.26. An increase in  $m_T$  similar to that in  $p_T$  is observed in all regions except for the angular region R1  $\theta=0-2^\circ$ , where multi-jet events have a higher increment for  $m_T$  which may be due to the elastic scattering events in  $pp$ -interactions. The region R1 may also be affected by the leading particle effect [131-135] with particles containing high longitudinal and low transverse momentum, as was observed in our previous study in the case of  $N_{ch}$  distribution for the same polar angle region and also in the low  $N_{ch}$  region for multiplicity distributions for full phase space [119]. We can see that the slopes of the distributions depend on the polar angle of the particles and the number of jets for the high  $p_T$  particles ( $p_T > 2$  GeV/c).

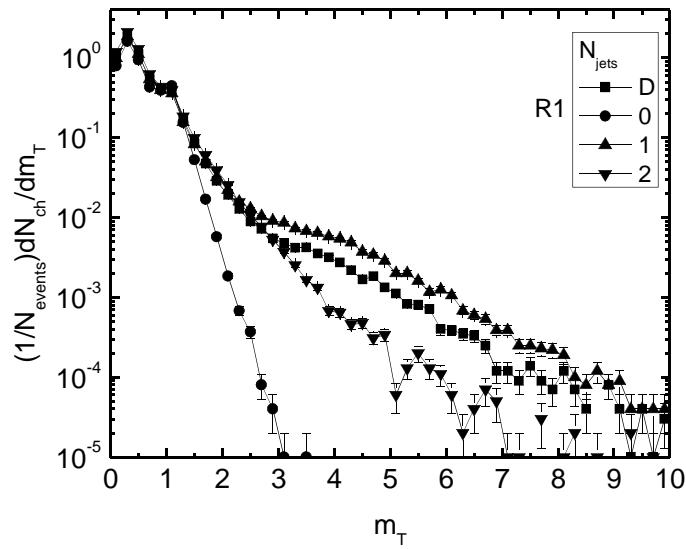


Figure 4.21  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R1  $\theta=0-2^\circ$ .

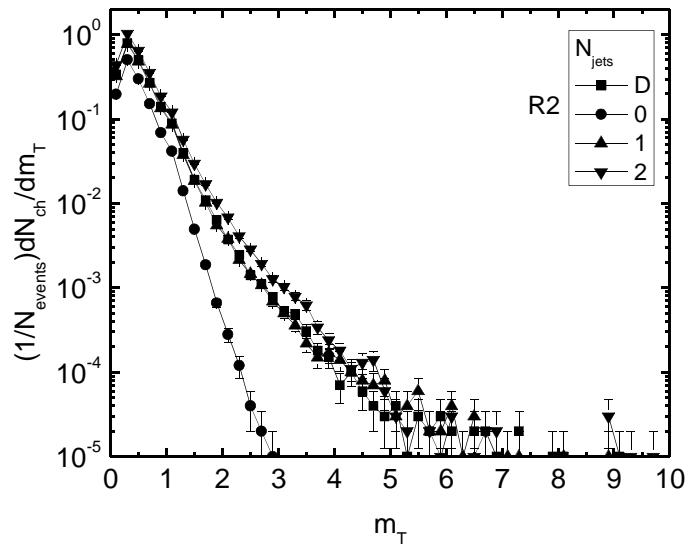


Figure 4.22  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R2  $\theta=2-4^\circ$ .

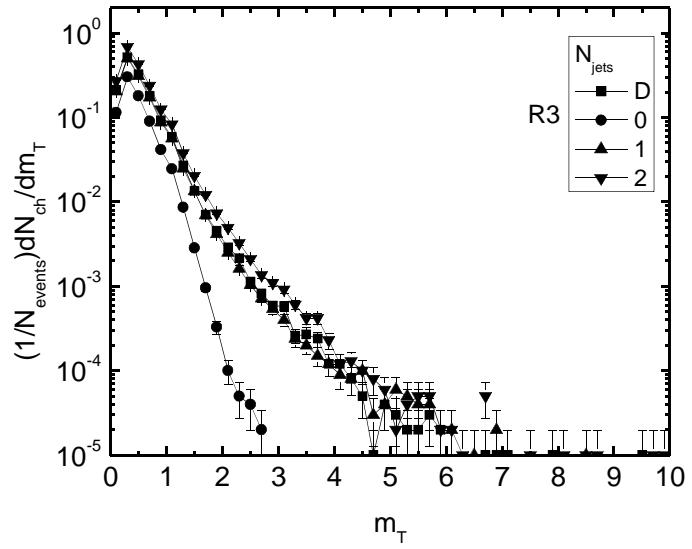


Figure 4.23  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R3  $\theta=4-6^\circ$ .

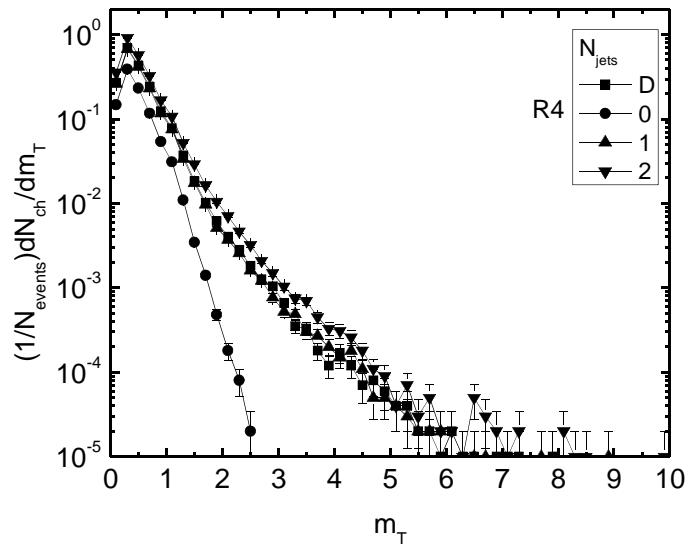


Figure 4.24  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R4  $\theta=6-10^\circ$ .

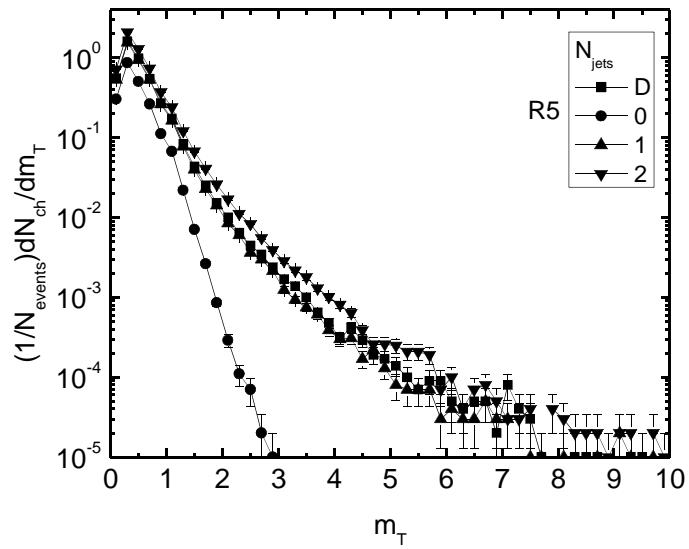


Figure 4.25  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R5  $\theta=10-30^\circ$ .

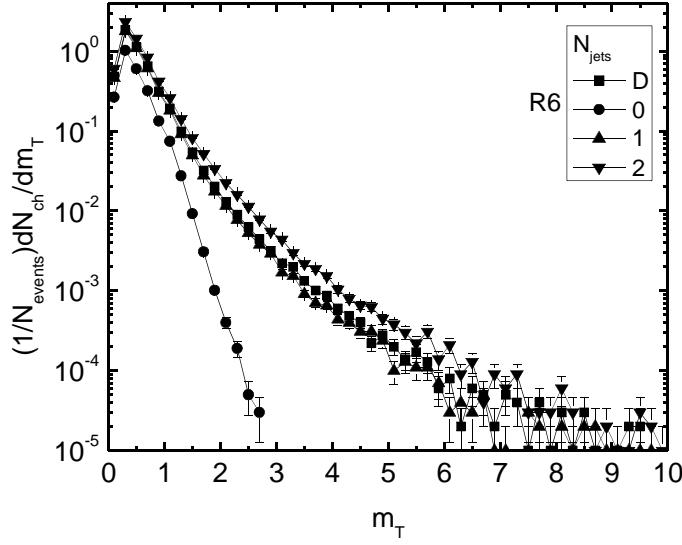


Figure 4.26  $m_T$  distributions of charged particles for  $N_{jet}=D$ , 0, 1 and 2 in the angular region: R6  $\theta=30-90^\circ$ .

Tables 4.3 and 4.4 show the slope parameters of transverse mass distributions for the whole range and for selected six regions R1—R6 of polar angle in the  $m_T$  regions  $m_T < 2\text{GeV}$  and  $2\text{GeV} < m_T < 3\text{GeV}$  respectively. These slopes parameters are obtained by using the exponentially decaying fit function  $e^{-bx}$  with  $b$  as the slope parameter.

Table 4.3 Slopes of the  $m_T$  spectra for the whole range and selected regions R1-R6 of the polar angle for  $m_T < 2\text{GeV}$

Polar Angle $\theta$	$N_{jet}=D$	$N_{jet}=0$	$N_{jet}=1$	$N_{jet}=2$
whole range	$3.10 \pm 2.61\text{E-}4$	$3.80 \pm 2.72\text{E-}4$	$3.13 \pm 2.62\text{E-}4$	$3.03 \pm 2.48\text{E-}4$
R1 $\theta=0^\circ-2^\circ$	$3.25 \pm 7.07\text{E-}4$	$3.61 \pm 5.33\text{E-}4$	$3.30 \pm 7.15\text{E-}4$	$3.23 \pm 6.88\text{E-}4$
R2 $\theta=2^\circ-4^\circ$	$3.28 \pm 1.02\text{E-}3$	$3.80 \pm 9.25\text{E-}4$	$3.31 \pm 1.02\text{E-}3$	$3.19 \pm 9.64\text{E-}4$
R3 $\theta=4^\circ-6^\circ$	$3.20 \pm 1.32\text{E-}3$	$3.81 \pm 1.16\text{E-}3$	$3.24 \pm 1.32\text{E-}3$	$3.15 \pm 1.21\text{E-}3$
R4 $\theta=6^\circ-10^\circ$	$3.20 \pm 1.15\text{E-}3$	$3.81 \pm 1.06\text{E-}3$	$3.21 \pm 1.15\text{E-}3$	$3.11 \pm 1.06\text{E-}3$
R5 $\theta=10^\circ-30^\circ$	$3.18 \pm 7.67\text{E-}4$	$3.80 \pm 6.9\text{E-}4$	$3.21 \pm 7.63\text{E-}4$	$3.07 \pm 7.22\text{E-}4$
R6 $\theta=30^\circ-90^\circ$	$3.07 \pm 7.55\text{E-}4$	$3.71 \pm 6.55\text{E-}4$	$3.11 \pm 7.47\text{E-}4$	$3.08 \pm 7.23\text{E-}4$

Table 4.4 Slopes of the  $m_T$  spectra for the whole range and selected regions R1-R6 of the polar angle for  $2\text{GeV} < m_T < 3\text{GeV}$

Polar Angle $\theta$	$N_{\text{jet}}=D$	$N_{\text{jet}}=0$	$N_{\text{jet}}=1$	$N_{\text{jet}}=2$
whole range	$1.87 \pm 0.01$	$4.61 \pm 0.01$	$1.77 \pm 0.02$	$1.95 \pm 0.01$
R1 $\theta=0^\circ-2^\circ$	$1.17 \pm 0.06$	$3.99 \pm 0.05$	$0.76 \pm 0.14$	$1.68 \pm 0.02$
R2 $\theta=2^\circ-4^\circ$	$1.98 \pm 0.04$	$4.64 \pm 0.07$	$1.99 \pm 0.04$	$1.93 \pm 0.03$
R3 $\theta=4^\circ-6^\circ$	$1.96 \pm 0.05$	$4.58 \pm 0.06$	$1.93 \pm 0.05$	$1.97 \pm 0.04$
R4 $\theta=6^\circ-10^\circ$	$1.77 \pm 0.04$	$4.44 \pm 0.06$	$1.88 \pm 0.05$	$2.10 \pm 0.03$
R5 $\theta=10^\circ-30^\circ$	$1.67 \pm 0.04$	$4.14 \pm 0.07$	$1.79 \pm 0.03$	$1.89 \pm 0.02$
R6 $\theta=30^\circ-90^\circ$	$1.85 \pm 0.03$	$4.22 \pm 0.05$	$1.86 \pm 0.03$	$1.84 \pm 0.02$

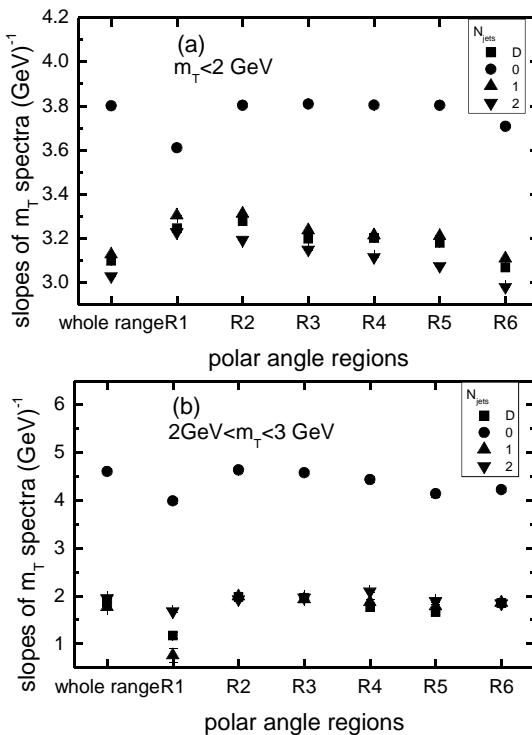


Figure 4.27 Slopes of the  $m_T$  spectra for the whole range and selected regions R1-R6 of the polar angle, (a) for  $m_T < 2\text{GeV}$  and (b) for  $2\text{GeV} < m_T < 3\text{GeV}$

Figure 4.27 ((a) and (b)) shows the plots of slopes of the  $m_T$  spectra for the whole range and selected six regions R1-R6 of polar angle for  $m_T < 2\text{GeV}$  and for  $2\text{GeV} < m_T < 3\text{GeV}$  as a function of number of jets. Very similar behavior to Fig. 4.19 is seen here. Event selection with  $N_{jet}=0$  affects the  $m_T$  distribution only up to  $m_T \sim 3\text{GeV}$ , as for  $m_T > 3\text{GeV}$  events with  $N_{jet} > 0$  are contributing.

For the above discussed three sections (4.4 to 4.6) we conclude the analysis of the effects of jet production on the pseudorapidity, transverse momentum and transverse mass distributions of secondary charged particles produced in  $pp$ -collisions at 1.8 TeV using the HIJING code. These distributions were analyzed for the whole range and for selected six regions of the polar angle as a function of different number of jets.

Some plateaus are observed in the central area of pseudorapidity. The existence of these plateaus is very important for the applicability of hydrodynamics. With increasing the number of jets the widths of the distributions decreased and the pseudorapidity density in the central area increased.

It was observed that with increasing the number of jets from 0 to 1, 2 or the default value of jets, the transverse momentum increased as the jets or multi-jet events contain high  $p_T$  particles.

The behavior of the  $p_T$ -distributions in the case of  $N_{jet} \geq 1$  is different in two areas of  $p_T$ :  $p_T < 2\text{ GeV}/c$  and  $p_T > 2\text{ GeV}/c$ . The slopes of the distribution in the first area are very close to that for events with  $N_{jet}=0$ . We can therefore say that particles with  $p_T < 2\text{ GeV}/c$  are produced by the same dynamics in events with different  $N_{jet}$ . The particles with  $p_T > 2\text{ GeV}/c$  are those produced by some special dynamics, different from the particles with  $p_T < 2\text{ GeV}/c$ . We may conclude that along with the multi-jet events, zero-jet events affect the  $p_T$  spectra only up to  $3\text{ GeV}/c$  and for  $p_T > 3\text{ GeV}/c$  only the multi-jet events contribute. This is caused by the jet dynamics (production and hadronization of the jets) from the HIJING code. We also observed, in a previous study, similar results for the

multiplicity distribution of charged particles. We concluded that the high multiplicity regions in the  $N_{ch}$  distribution correspond to multi-jet events.

## Chapter 5      Conclusions

Here we summarize the conclusions.

We studied the effects of jet production on the multiplicity, pseudorapidity, transverse momentum and transverse mass distributions of charged particles produced in  $pp$ -collisions at 1.8 TeV, using the HIJING code. These distributions were analyzed for the whole range and for six selected regions (R1—R6) of the polar angle as a function of different number of jets.

The HIJING results show that there are three areas in multiplicity distributions of charged particles:  $N_{ch} < 15$ ,  $15 < N_{ch} < 80$  and  $N_{ch} > 80$ . We identified the first area as a region dominating leading particles: elastic scattering region. The particles from this area correspond to the polar angle region R1 and without jets. The second region is contributed by multi-jet events along with zero jet events. The third area corresponds to multi-jet (1, 2 or more jets) events. Analysis of the multiplicity distributions for other angular regions (R2—R6) also showed that the increase in the charged particles multiplicity is connected to the multi-jet events.

We conclude that the high  $N_{ch}$  areas correspond to the multi-jet events. Our results were consistent with the analysis of weighted superposition mechanism of two negative binomial multiplicity distributions for hadronic collisions where the two components correspond to soft and semi-hard events respectively.

Some plateaus are observed in the central area of pseudorapidity. The existence of these plateaus is very important for the applicability of hydrodynamics. With increasing the number of jets the widths of the distributions decreased and the pseudorapidity density in the central area increased. From comparison of HIJING results with that of CDF we conclude that increase in the pseudorapidity density is due to multi-jet events.

It was observed that with increasing the number of jets (and the polar angle) the transverse momentum is increased as the jets or multi-jet events contain high  $p_T$  particles.

The behavior of the  $p_T$ -distributions for  $N_{jet} \geq 1$  is different in two areas of  $p_T$ :  $p_T < 2$  GeV/c and  $p_T > 2$  GeV/c. The slopes of the distribution in the first area are very close to that for events with  $N_{jet}=0$ . We can therefore say that the particles with  $p_T < 2$  GeV/c are produced by the same dynamics in events with different  $N_{jet}$ . The particles with  $p_T > 2$  GeV/c are those produced by some special dynamics, different from the particles with  $p_T < 2$  GeV/c.

We may conclude that along with the multi-jet events, zero-jet events affect the  $p_T$  spectra only up to 3 GeV/c and for  $p_T > 3$  GeV/c only the multi-jet events contribute. This is caused by the jet dynamics from the HIJING code. Analysis of transverse mass ( $m_T$ ) distribution also showed a similar behavior to that of  $p_T$  distribution.

On the basis of this analysis we will continue further to study the effects of jet production/suppression in other hadronic collisions; hadron-nucleus and nucleus-nucleus collisions at the TeV energy scale.

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## List of Publications of Ali Zaman

This Thesis is particularly based on the first two papers.

1. Ali Zaman, Mais Suleymanov, Muhammad Ajaz and Kamal Hussain Khan, “Effect of the Jet Production on Pseudorapidity, Transverse Momentum and Transverse Mass Distributions of Charged Particles Produced in  $pp$ -Collisions at Tevatron Energy”, Chinese Physics C, Vol. **39**, No. 7, 073001, 2015
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19. Ali Zaman, "Jets in High Energy Hadronic Collisions: Jet Production in Hadron-Nucleus and Nucleus-Nucleus Collisions at Relativistic and Ultrarelativistic Energies", LAP Lambert Academic Publishing GmbH & Co. KG, Germany, 2011. ISBN # 9783843380935

### **Publications with the ALICE Collaboration (LHC CERN Switzerland)**

1. ALICE Collaboration, "Centrality dependence of  $\psi(2S)$  suppression in p-Pb collisions at 5.02 TeV", JHEP **06** (2016) 50
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