

## Cluster radioactive-decay using the Relativistic mean field theory within the preformed cluster model

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### Introduction

Cluster radioactivity is the spontaneous emission of clusters heavier than  $\alpha$ -particle. Since its first theoretical prediction [1] in 1980 and experimental confirmation [2] in 1984, this phenomenon is now established for some 26 decays with light to heavy ( $^{14}\text{C}$  to  $^{34}\text{Si}$ ) clusters from various actinides ( $^{221}\text{Fr}$  to  $^{242}\text{Cm}$ ). Theoretically, two types of models have been advanced, namely i) Unified fission models (UFM), such as the analytic super-asymmetric fission model (ASAFM) [1], and ii) the Preformed cluster models (PCM), like that of Gupta and collaborators based on collective potential energy surfaces [3]. The two models differ from each other for their non-inclusion or inclusion of the pre-formation/ spectroscopic factor(s) of the cluster(s) being born before penetrating the confining interaction barrier. Some effort has also gone in understanding it on the mean-field Hatree-Fock-Bogoliubov theory [4], treating it as an asymmetric fission process.

In this paper, based on PCM, for the first time we use the relativistic mean field (RMF) theory, which is already shown [5] to support the clustering effects in various heavy parents with observed cluster decays. For the present study, we have chosen the parents  $^{222}\text{Ra}$ ,  $^{226,228}\text{Th}$ ,  $^{230,232,234}\text{U}$ ,  $^{236,238}\text{Pu}$ , and  $^{242}\text{Cm}$  which decay, respectively, in to  $^{14}\text{C}$ ,  $^{18,20}\text{O}$ ,  $^{22,24,26}\text{Ne}$ ,  $^{28,30}\text{Mg}$ , and  $^{34}\text{Si}$  clusters, having always the doubly magic  $^{208}\text{Pb}$  as the daughter nucleus.

### Methodology

The decay constant  $\lambda$  (or the decay half-life time  $T_{1/2} = \ln 2/\lambda$ ), in PCM is defined as [3]

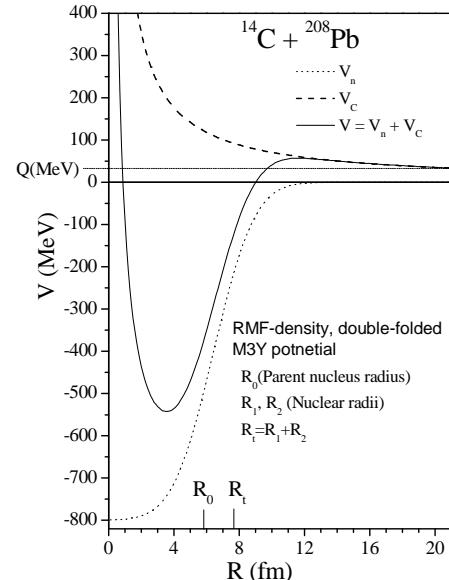
$$\lambda_{\text{PCM}} = v_0 P_0 P, \quad (1)$$

which in UFM is simply given by [1]

$$\lambda_{\text{UFM}} = v_0 P, \quad (2)$$

where  $v_0$  is the assault frequency with which the cluster hits the barrier.  $P_0$  is the pre-formation probability of the cluster, and  $P$  is the WKB penetrability of preformed cluster in  $R$ -motion. An empirical estimate of the pre-formation factor  $P_0^{(\text{emp})}$  ( $= \lambda_{\text{Expt}} / \lambda_{\text{UFM}}$ ) can also be obtained [3].

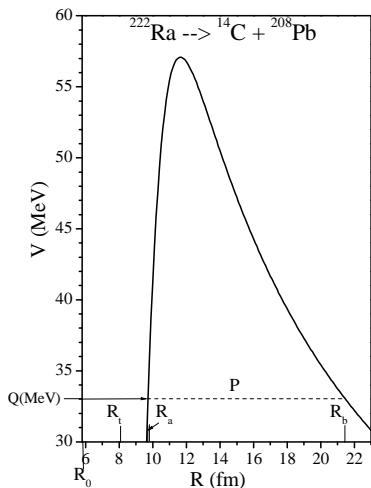
In order to obtain the nuclear interaction potential  $V_n(R)$ , the double folding procedure [6] is used to fold the density-dependent M3Y interaction potential (DDM3Y) with the RMF calculated nuclear densities of the cluster and daughter nuclei. Then, the total interaction potential  $V(R) = V_n(R) + V_C(R)$ , where  $V_C(R)$  is the Coulomb interaction potential. This allows us to calculate the penetration probability  $P$  of the cluster, and hence calculate  $\lambda_{\text{UFM}}$  and  $P_0^{(\text{emp})}$ .



**Fig. 1** The RMF densities double folded M3Y potential  $V_n$ , Coulomb  $V_C$  and total interaction potential  $V$  as a function of the radial separation between the cluster and daughter nuclei.

## Results and Discussions

In Fig. 1, the total interaction potential  $V(R)$  between the preformed cluster  $^{14}\text{C}$  and daughter nucleus  $^{208}\text{Pb}$  is shown as a solid line. The strong attractive part, the nuclear potential  $V_n$  (the dotted line), is the double folded DDM3Y and the repulsive part is the Coulomb potential  $V_C$  (the dashed line). The total interaction potential  $V(R)$  is used for calculating the penetrability  $P$ , in the following.



**Fig. 2** Same as Fig. 1 for the total interaction potential  $V(R)$ , illustrating the penetration process of the cluster with an energy equal to  $Q$ -value of the decay.

Fig. 2 illustrates the decay path for WKB penetrability  $P$  through the total interaction potential  $V(R)$  for  $^{14}\text{C}$  cluster decay of  $^{222}\text{Ra}$  with an energy  $Q$ . For turning points  $R_a$  and  $R_b$ ,  $V(R_a) = V(R_b) = Q$ -value. The calculated  $P$  and the empirically estimated  $P_0^{(\text{emp})}$  are given in Table 1 for the measured cluster decays from different parent nuclei having the daughter  $^{208}\text{Pb}$  in each case. The  $P_0^{(\text{emp})}(C)$  for clusters is given in terms of the  $\alpha$ -particle  $P_0^{(\text{emp})}(\alpha)$ , i.e., as  $P_0^{(\text{emp})}(C)/P_0^{(\text{emp})}(\alpha)$ . It is relevant to mention here that for the  $\alpha$ -decays of all the parent nuclei mentioned above, we obtain very large  $P_0^{(\text{emp})}(\alpha)$  in comparison to the corresponding  $P_0^{(\text{emp})}(C)$  values for cluster decays. Note in Table 1 that the  $P_0^{(\text{emp})}(C)/P_0^{(\text{emp})}(\alpha)$  decreases as the size of the cluster increases, in the line with previous studies based on PCM [3].

**Table 1:** The WKB penetrability  $P$  and the ratio  $P_0^{(\text{emp})}(C)/P_0^{(\text{emp})}(\alpha)$  for various cluster decays  $^{14}\text{C}$ ,  $^{18,20}\text{O}$ ,  $^{22,24,26}\text{Ne}$ ,  $^{28,30}\text{Mg}$ , and  $^{34}\text{Si}$  with  $^{208}\text{Pb}$  as the daughter product of parents  $^{222}\text{Ra}$ ,  $^{226,228}\text{Th}$ ,  $^{230,232,234}\text{U}$ ,  $^{236,238}\text{Pu}$ , and  $^{242}\text{Cm}$ , respectively. The impinging frequency  $v_0 \sim 10^{21} \text{ s}^{-1}$  in each case. The  $Q$ -value is calculated by using the experimental binding energies [7].

Cluster Decay	$Q$ -value (MeV)	$P$	$P_0^{(\text{emp})}(C)/P_0^{(\text{emp})}(\alpha)$
$^{14}\text{C}$	33.050	$2.933 \times 10^{-25}$	$9.197 \times 10^{-07}$
$^{18}\text{O}$	45.727	$2.540 \times 10^{-29}$	$4.315 \times 10^{-07}$
$^{20}\text{O}$	44.723	$1.541 \times 10^{-31}$	$1.821 \times 10^{-10}$
$^{22}\text{Ne}$	61.388	$3.154 \times 10^{-29}$	$3.792 \times 10^{-10}$
$^{24}\text{Ne}$	62.311	$2.696 \times 10^{-28}$	$2.920 \times 10^{-13}$
$^{26}\text{Ne}$	59.465	$1.659 \times 10^{-32}$	$1.246 \times 10^{-13}$
$^{28}\text{Mg}$	79.670	$1.802 \times 10^{-26}$	$3.631 \times 10^{-16}$
$^{30}\text{Mg}$	76.824	$7.262 \times 10^{-30}$	$9.970 \times 10^{-17}$
$^{34}\text{Si}$	96.511	$1.090 \times 10^{-25}$	$3.101 \times 10^{-18}$

## Summary and Conclusions

The present study based on RMF formalism, using the double folded M3Y interaction, shows the importance of pre-formation factor  $P_0$  for the process of cluster radioactive-decay, which has so far been explored on the PCM based on Quantum Mechanical Fragmentation theory [3]. Though at present the factor  $P_0$  is adjusted only empirically, it will be highly interesting to see how this quantity can be treated within the RMF theory. Work in this direction is in progress.

## References

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